



UNIVERSITÉ  
DE GENÈVE



# EXTRACTING CLUSTER INFORMATION FROM SMALL-SCALE CMB

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Sayan Saha

TEXT

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## WORK DONE IN COLLABORATION WITH



Louis Legrand



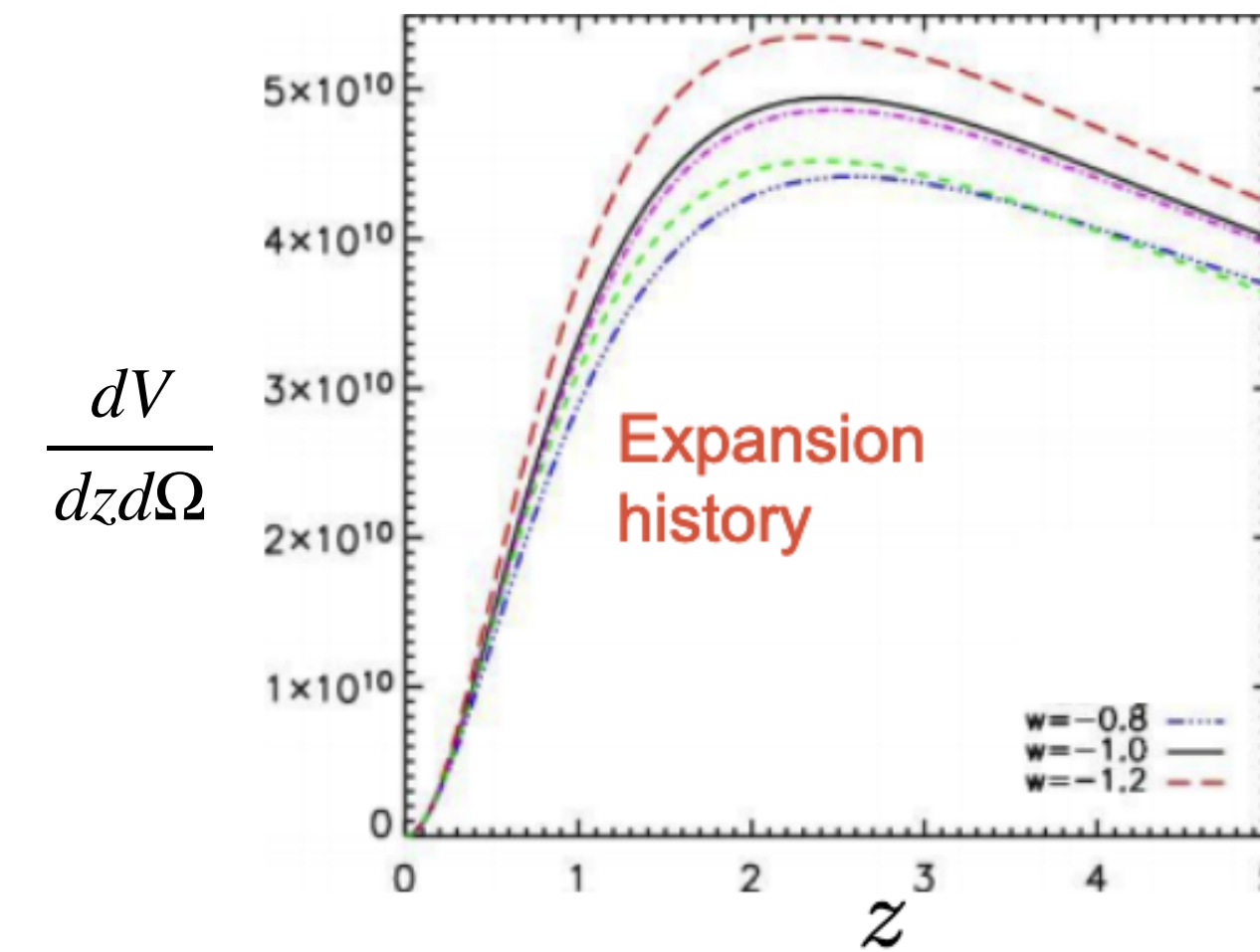
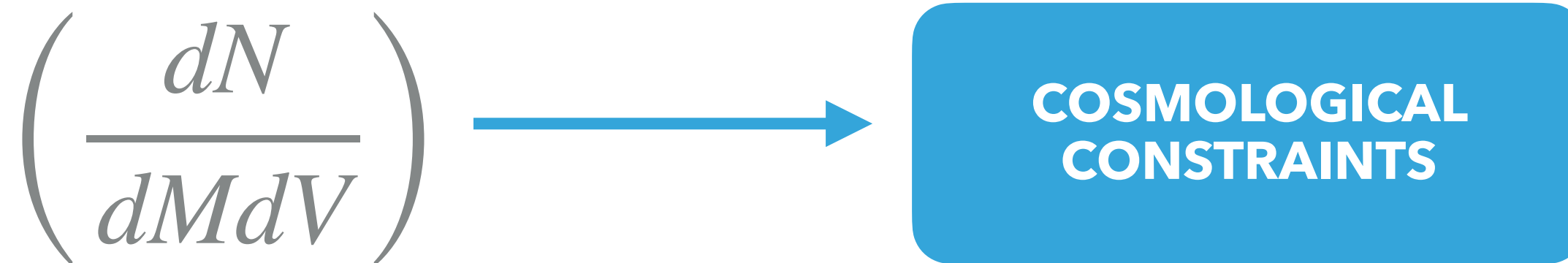
Julien Carron

# OUTLINE

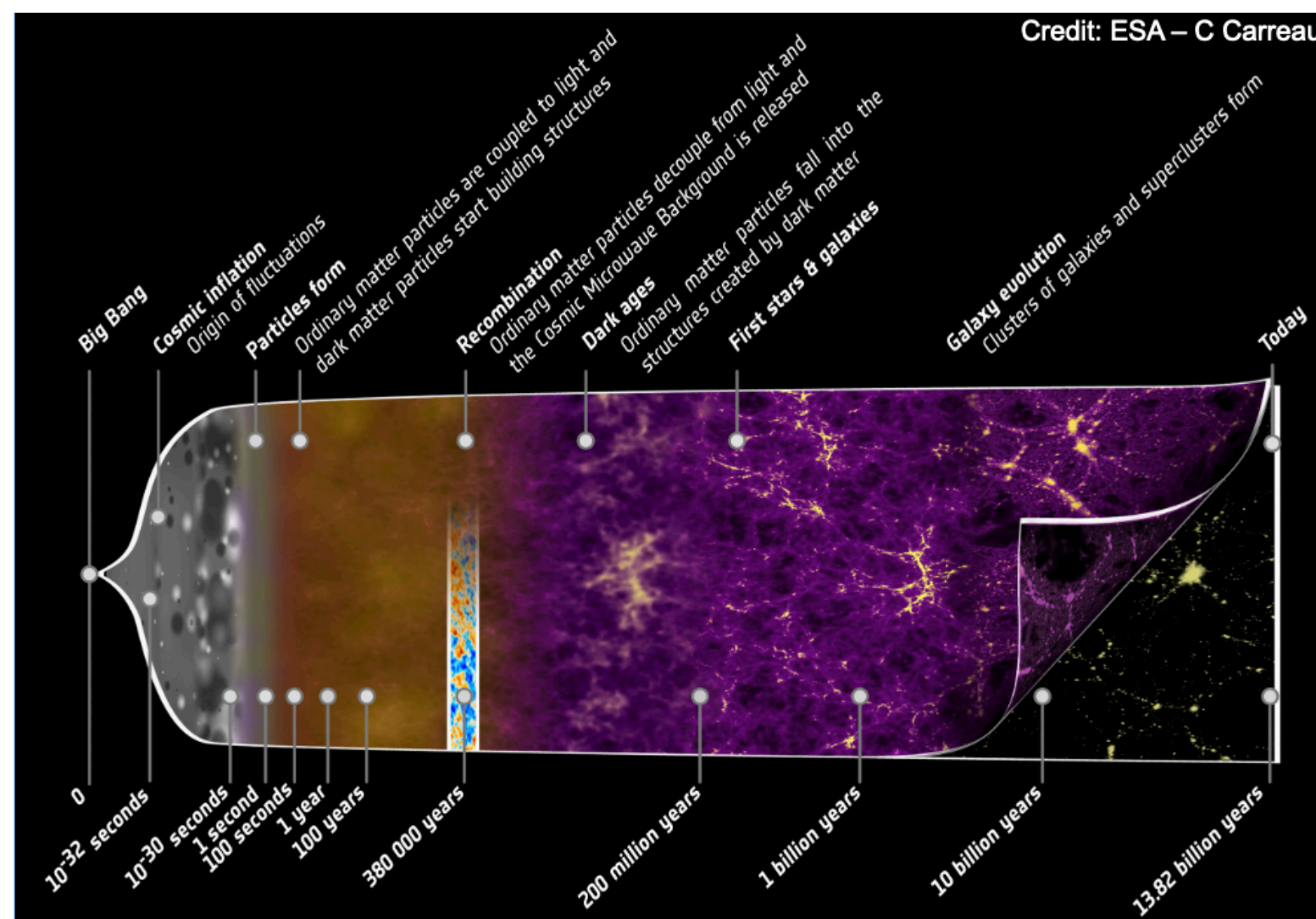
- ▶ **Motivation**
- ▶ Theoretical Model
- ▶ Analysis
- ▶ Conclusion

# MOTIVATION BEHIND COSMOLOGY WITH CLUSTERS

- ▶ Cluster abundances Cosmology



Credit: Koyama & Maartens, 2006



- ▶ This history sets bounds on how small and how large a collapsed object can be.
- ▶ Uncertainties in cluster mass measurements affects our understanding of the cosmic expansion history

## HOW MASS OF CLUSTERS COMES TO THE PICTURE?

- ▶ The gravitational lensing signature is directly sensitive to the mass of clusters.



galaxy cluster SMACS 0723  
Credits: NASA, ESA, CSA, and STScI

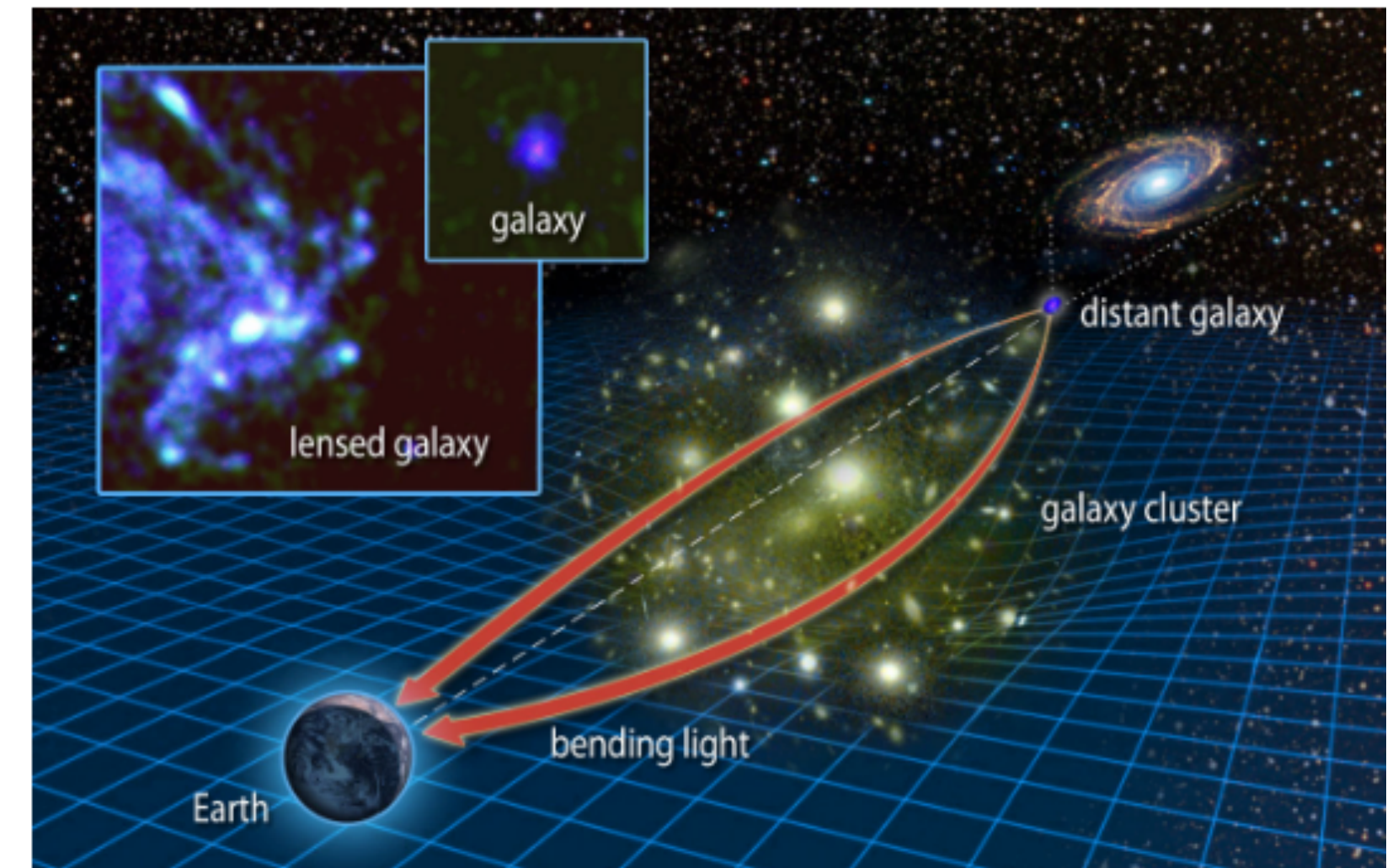


Image credit: Karen Teramura

- ▶ The mass profile of the clusters can be studied through:
  1. Strong Lensing distortions of Galaxies
  2. Weak Lensing distortions of Galaxies
  3. CMB Lensing by the galaxy clusters

# OUTLINE

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## CLUSTER MODEL (NFW PROFILE)

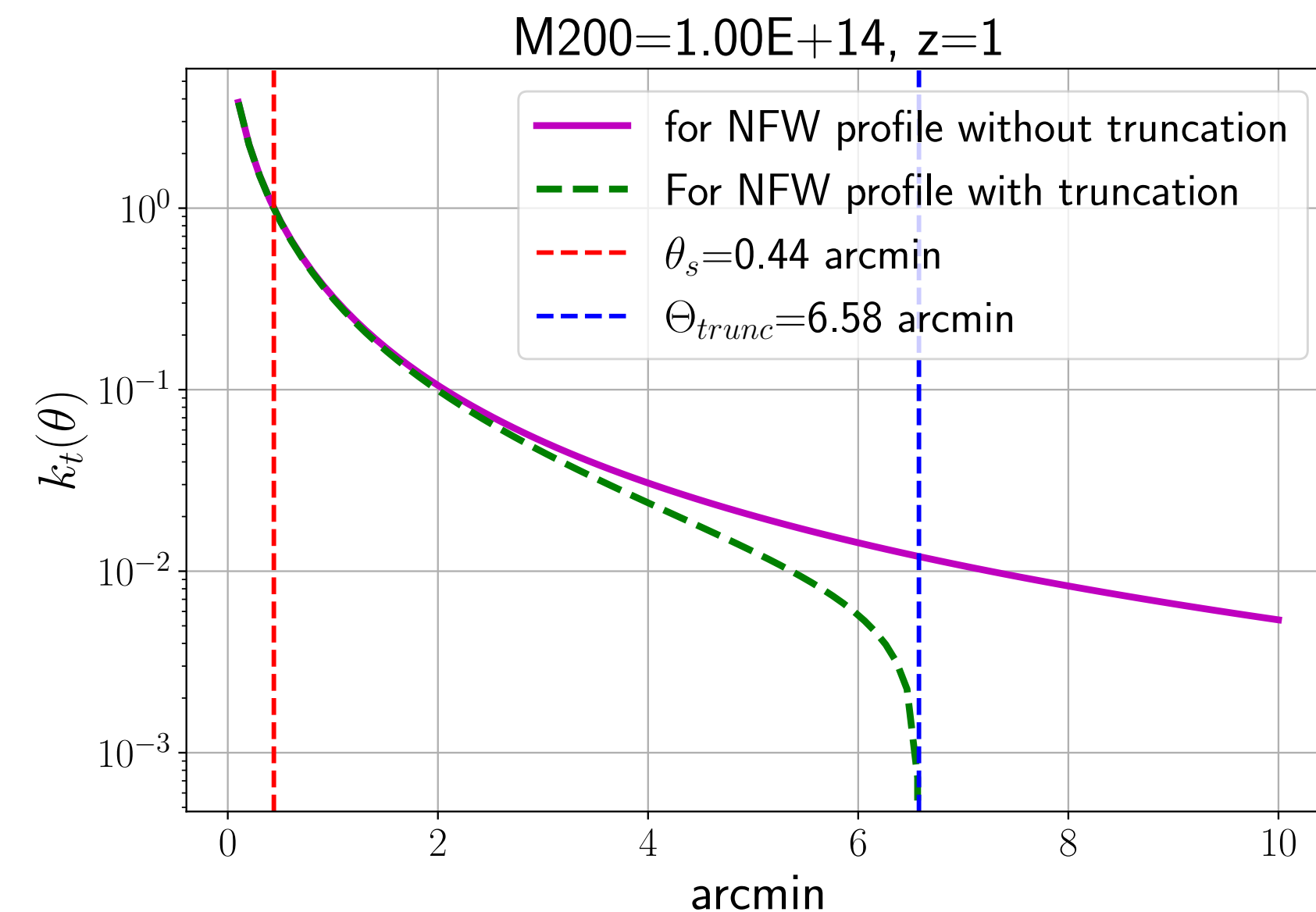
- ▶ The halo density profile

$$\rho(r) = \begin{cases} \frac{\rho_0}{\left(\frac{r}{r_s}\right)\left(1 + \frac{r}{r_s}\right)^2} & \text{if } r < R_{\text{trunc}} \\ 0 & \text{if } r > R_{\text{trunc}} \end{cases},$$

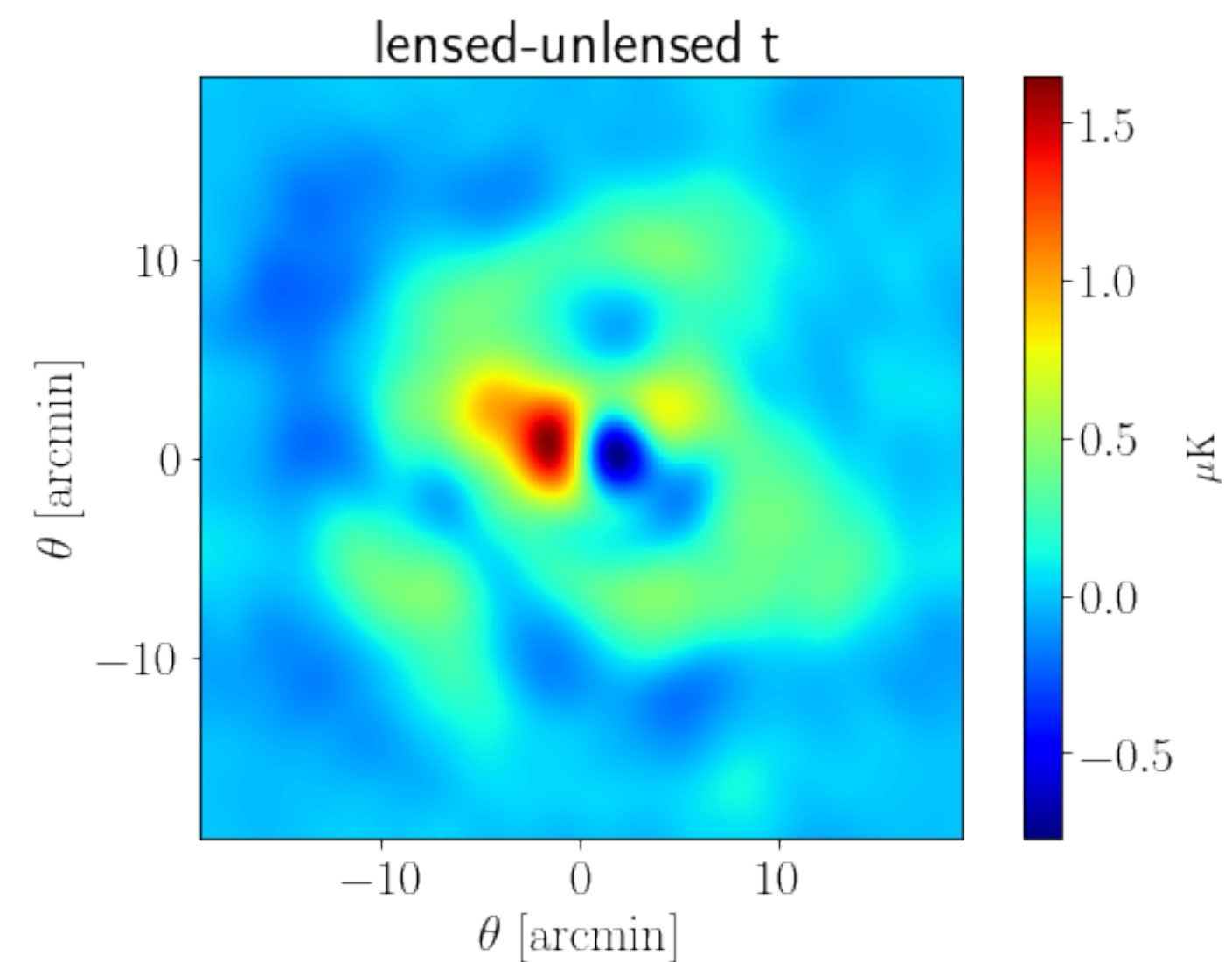
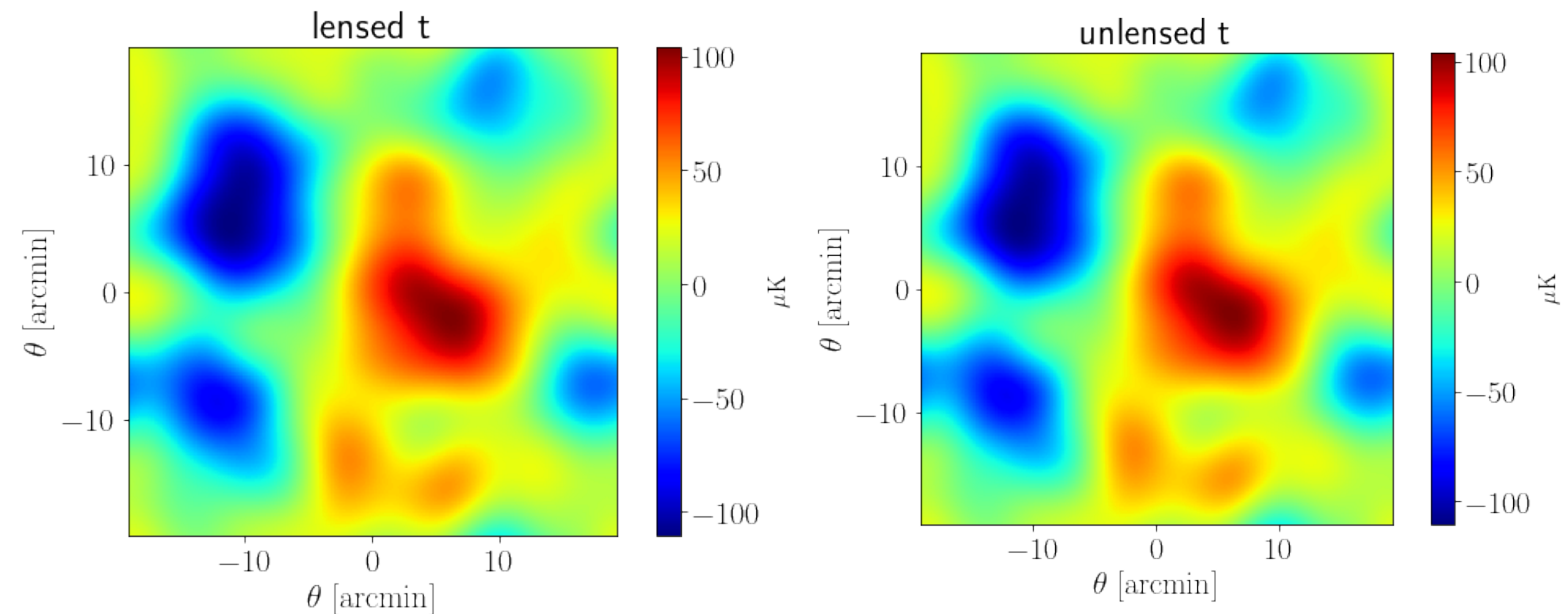
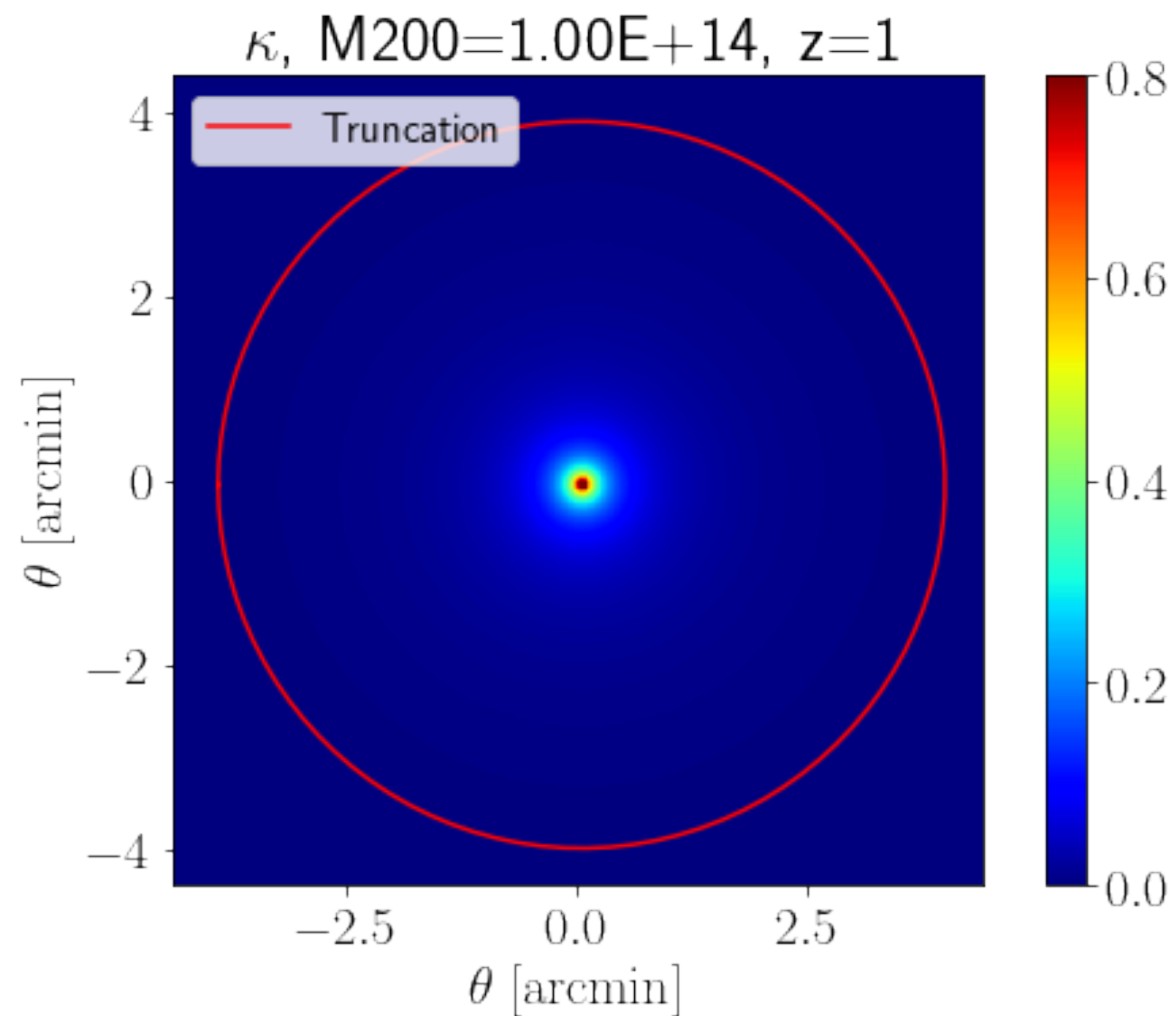
$$\kappa_{cl} = \frac{2\rho_s r_s}{\Sigma_{crit}(z)} g(x), \text{ where } x = \frac{r}{r_s} = \frac{\theta}{\theta_s}$$

- ▶ The convergence profile is

$$\kappa_{cl}(r) = \frac{\Sigma_{cl}(r)}{\Sigma_{crit}(z)}$$



# CMB LENSING BY NFW PROFILE





## THE TEMPLATE FUNCTION

- ▶  $\kappa_{cl}(\theta) = \kappa_0 \kappa_t(\theta, \theta_s)$
- ▶  $\kappa_t(\theta = \theta_s) = 1$  and  $\kappa_{cl}(\theta = \theta_s) = \kappa_0$ .

We need an estimator for  $\kappa_0$

$$\kappa_0 \theta_s^2 \propto \frac{M_{200}}{\sum_{crit}(z) d_A(z)}$$

$$\frac{\sigma_M}{M} = \frac{\sigma_{\kappa_0}}{\kappa_0}$$

# OUTLINE

- ▶ Motivation
- ▶ Theoretical Model
- ▶ Analysis

## MINIMUM VARIANCE ESTIMATOR OF $\kappa_0$

$$\hat{\kappa}_0 = \frac{\int d^2\vec{l} \frac{\kappa^t(\vec{l})\hat{\kappa}(\vec{l})}{N_{\vec{l}}}}{\int d^2\vec{l} \frac{|\kappa^t(\vec{l})|^2}{N_{\vec{l}}}}$$

With the inverse variance,

$$\frac{1}{\sigma^2} = \int d^2l \frac{|\kappa_l^t|^2}{N_l}$$

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$\hat{\kappa}_l$  = convergence estimated from data  
 $N_l$  = Noise of the estimation  
 $= C_l^{\kappa\kappa} + N_0^\kappa + N_1^\kappa$

With the inverse variance,

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We employ The Maximum a Posterior (MAP) Estimator by Carron et al 2017

We maximize the log posterior:

$$\ln p(\phi | X^{dat}) = \ln p(X^{dat} | \phi) - \frac{1}{2} \sum_L \frac{\phi_L^2}{C_L^{\phi\phi}}$$

Using Gradients:

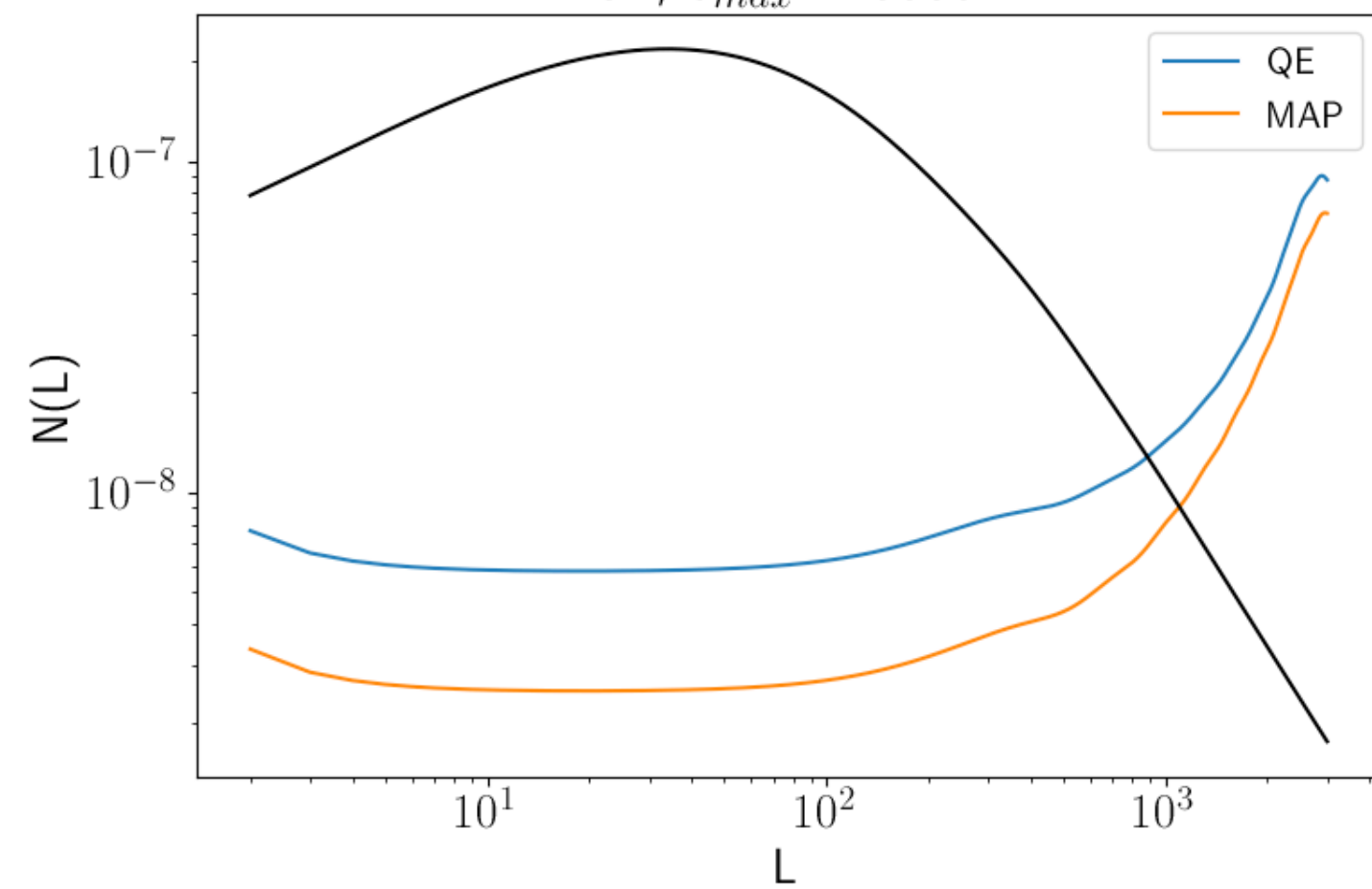
$$g_\phi = \frac{\delta \ln p(X^{dat} | \phi)}{\delta \phi} = g^{QD} - g^{MF} + g^{PR}$$

We use these  $g_\phi$ 's iteratively to reach the maximum

# IMPROVEMENT OVER QUADRATIC ESTIMATOR

The noise of the estimator

S4,  $\ell_{max} = 3000$

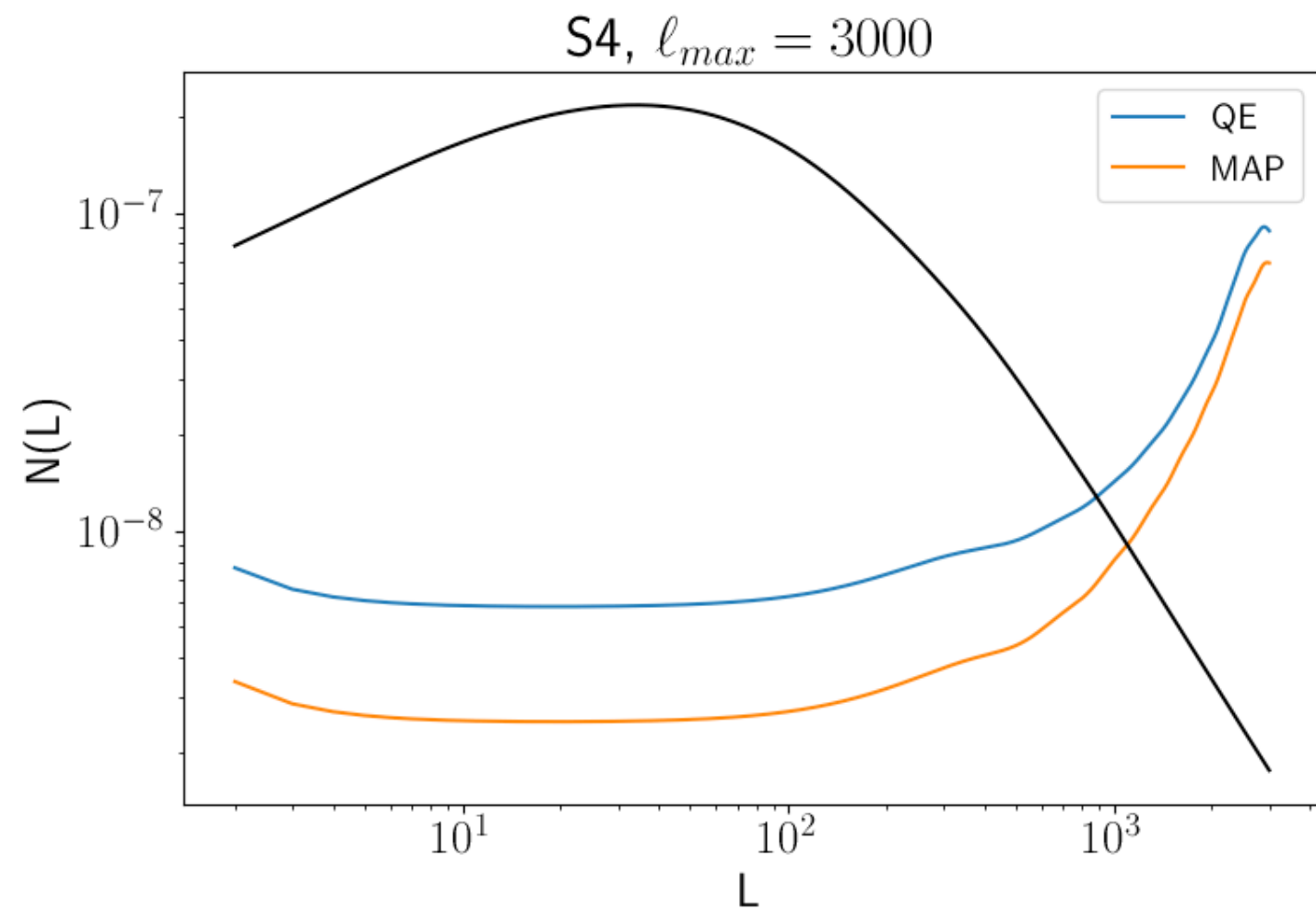


$$\Delta_T = \Delta_p / \sqrt{2} = 1 \mu K\text{-arcmin}$$

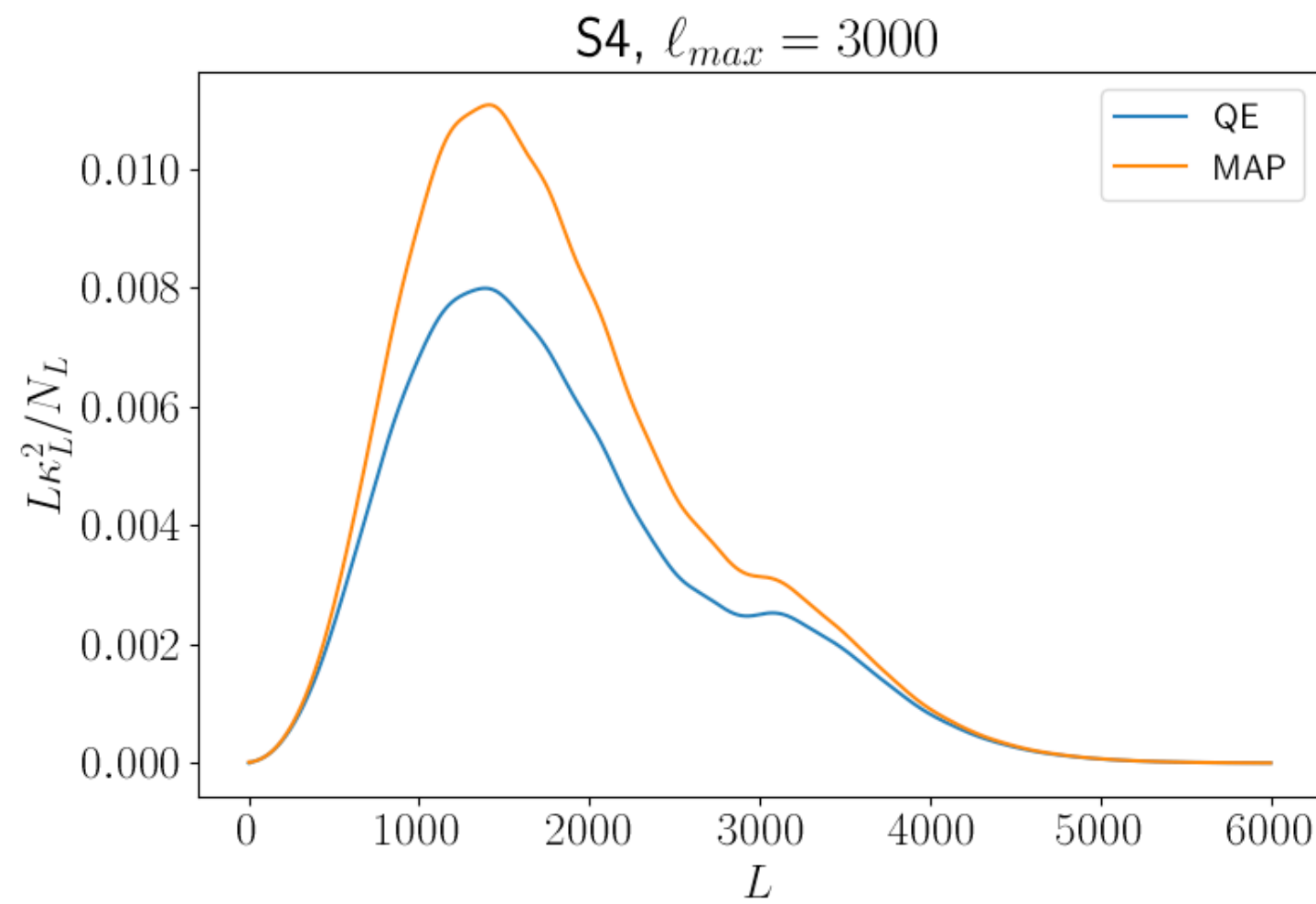
Beam = 1 arcmin

# IMPROVEMENT OVER QUADRATIC ESTIMATOR

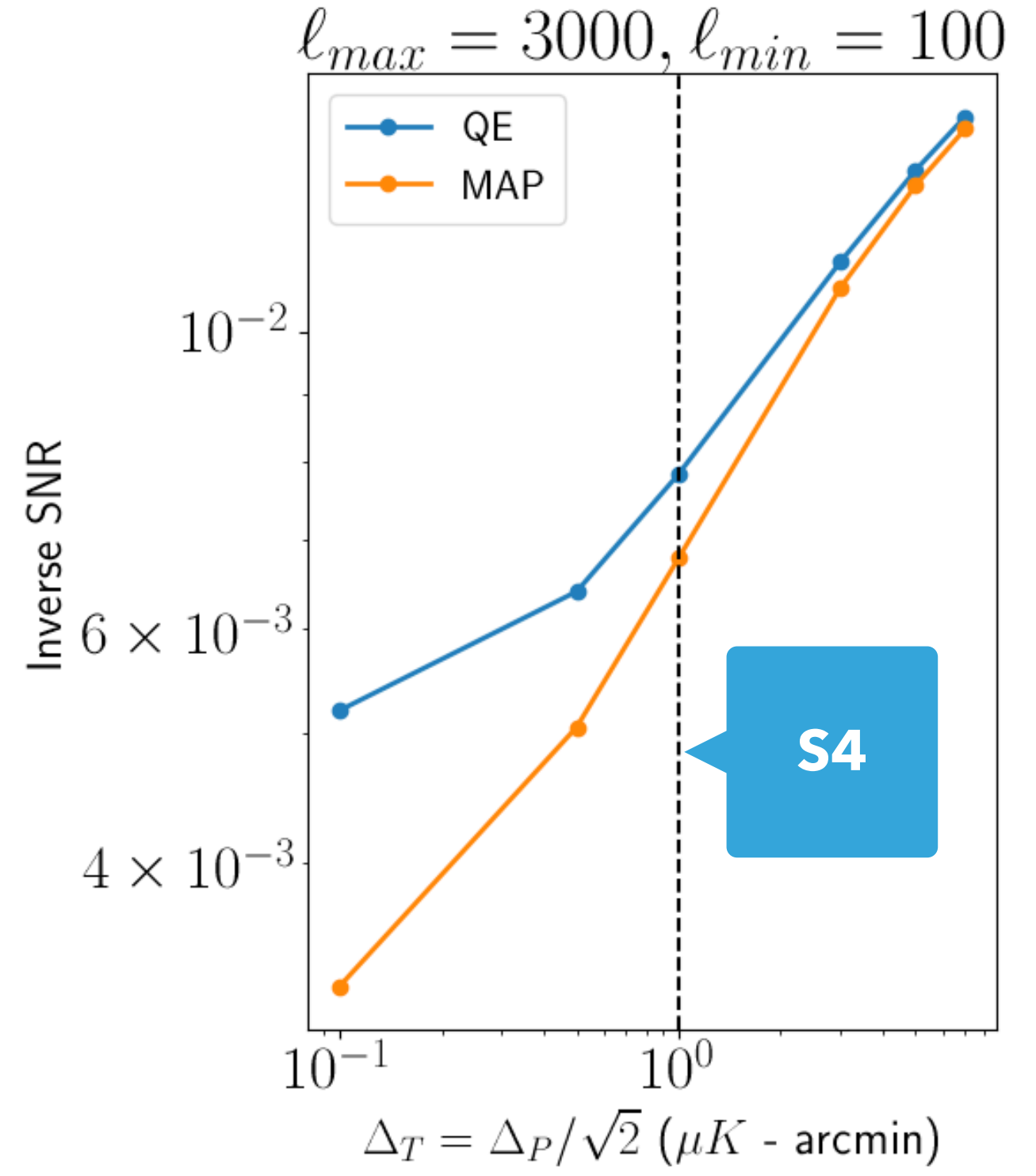
The noise of the estimator



The contribution in  $\frac{1}{\sigma^2} = \int d^2l \frac{|\kappa_l^t|^2}{N_l}$  comes from certain scales



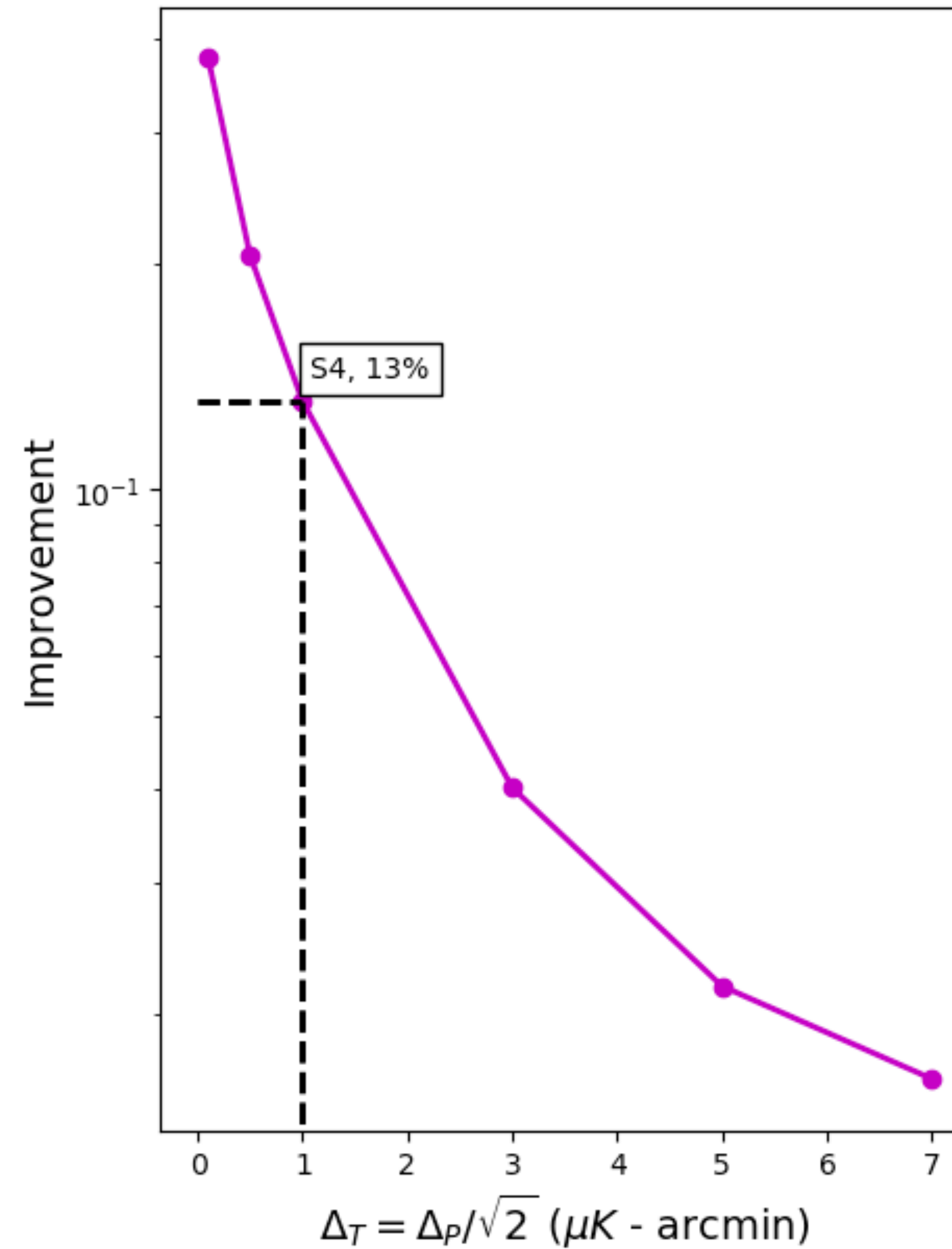
Inverse SNR for  $10^5$  clusters



$$\Delta_T = \Delta_P / \sqrt{2} = 1 \mu K\text{-arcmin}$$

Beam = 1 arcmin

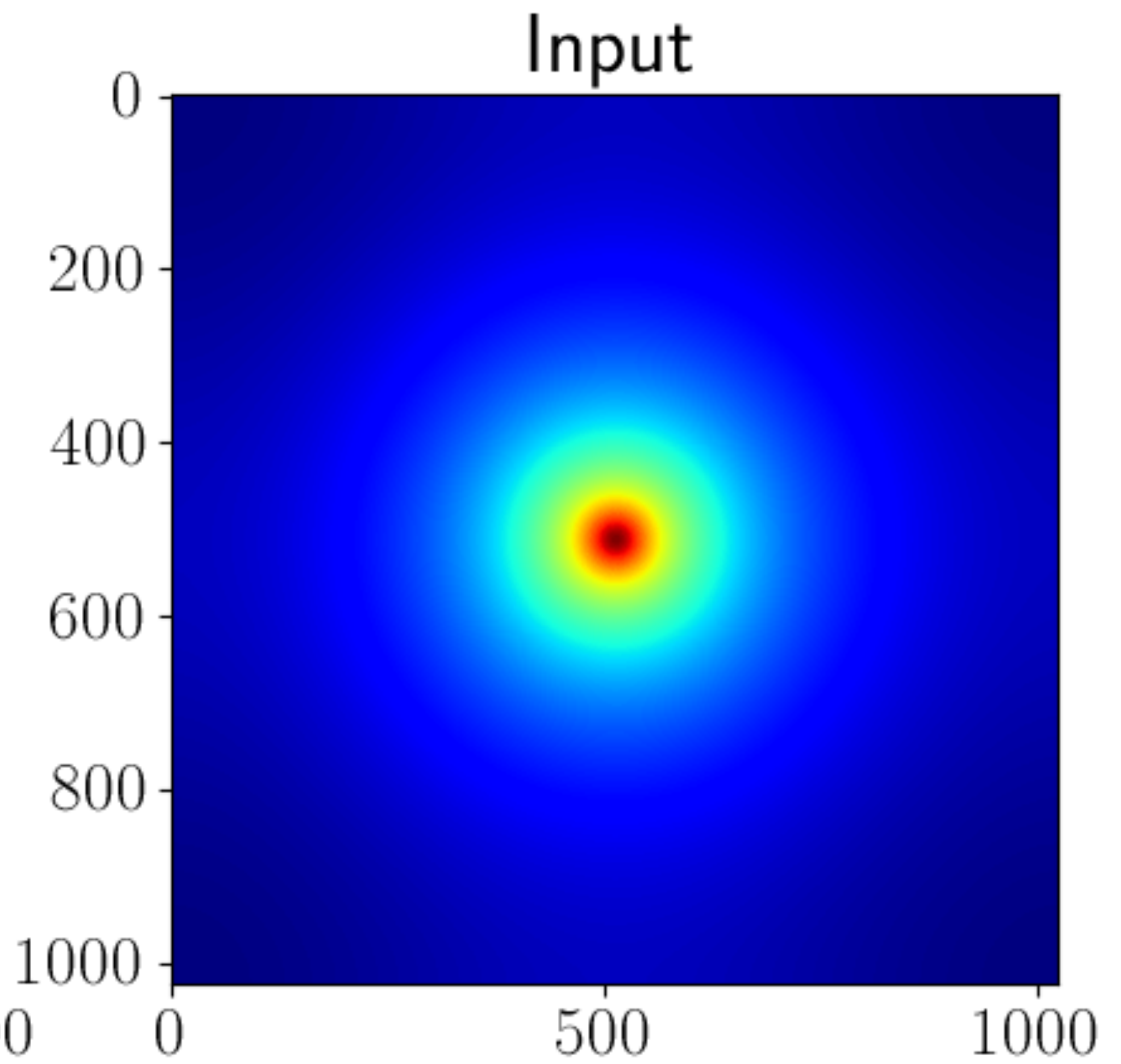
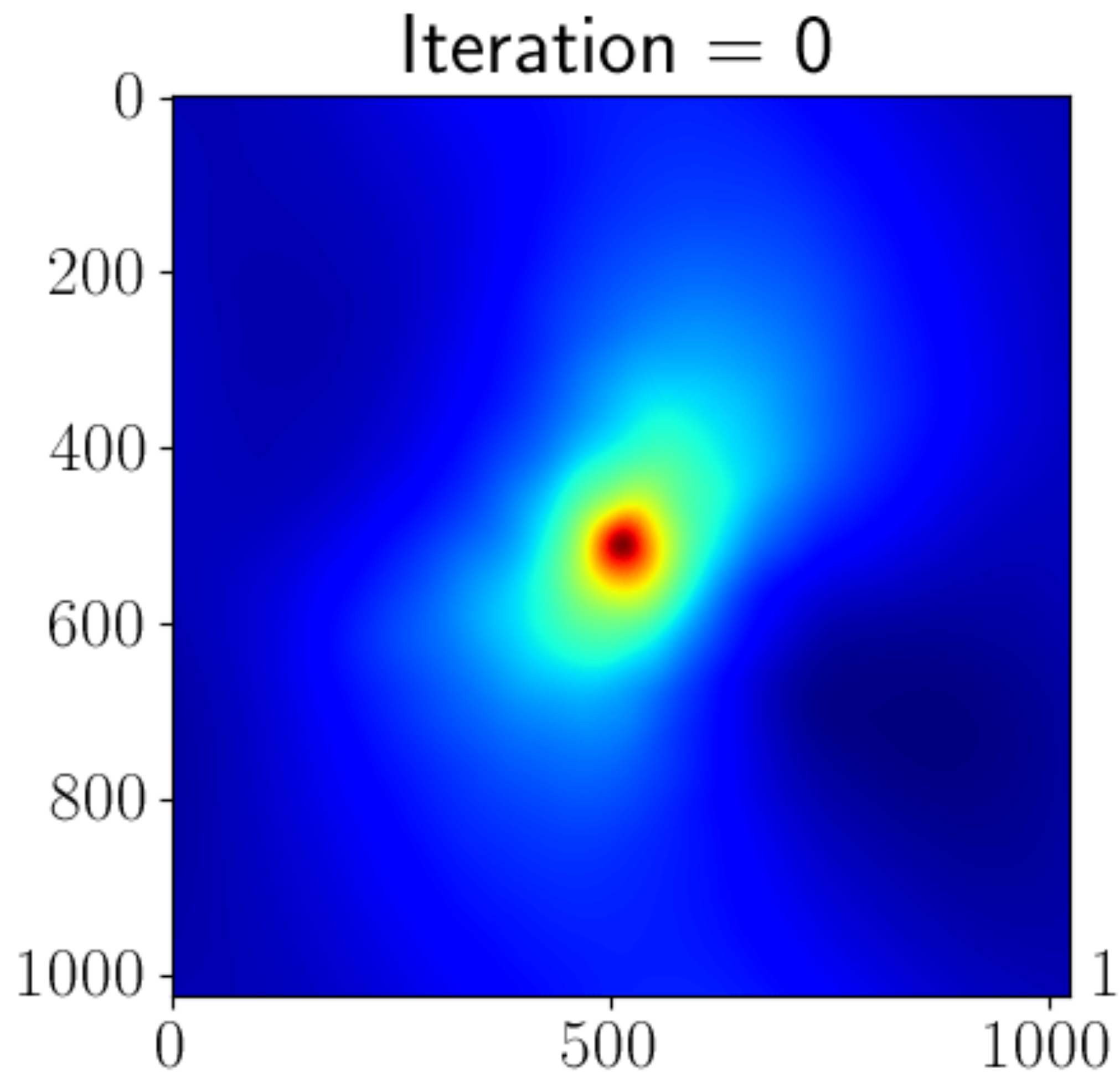
# IMPROVEMENT OVER QUADRATIC ESTIMATOR



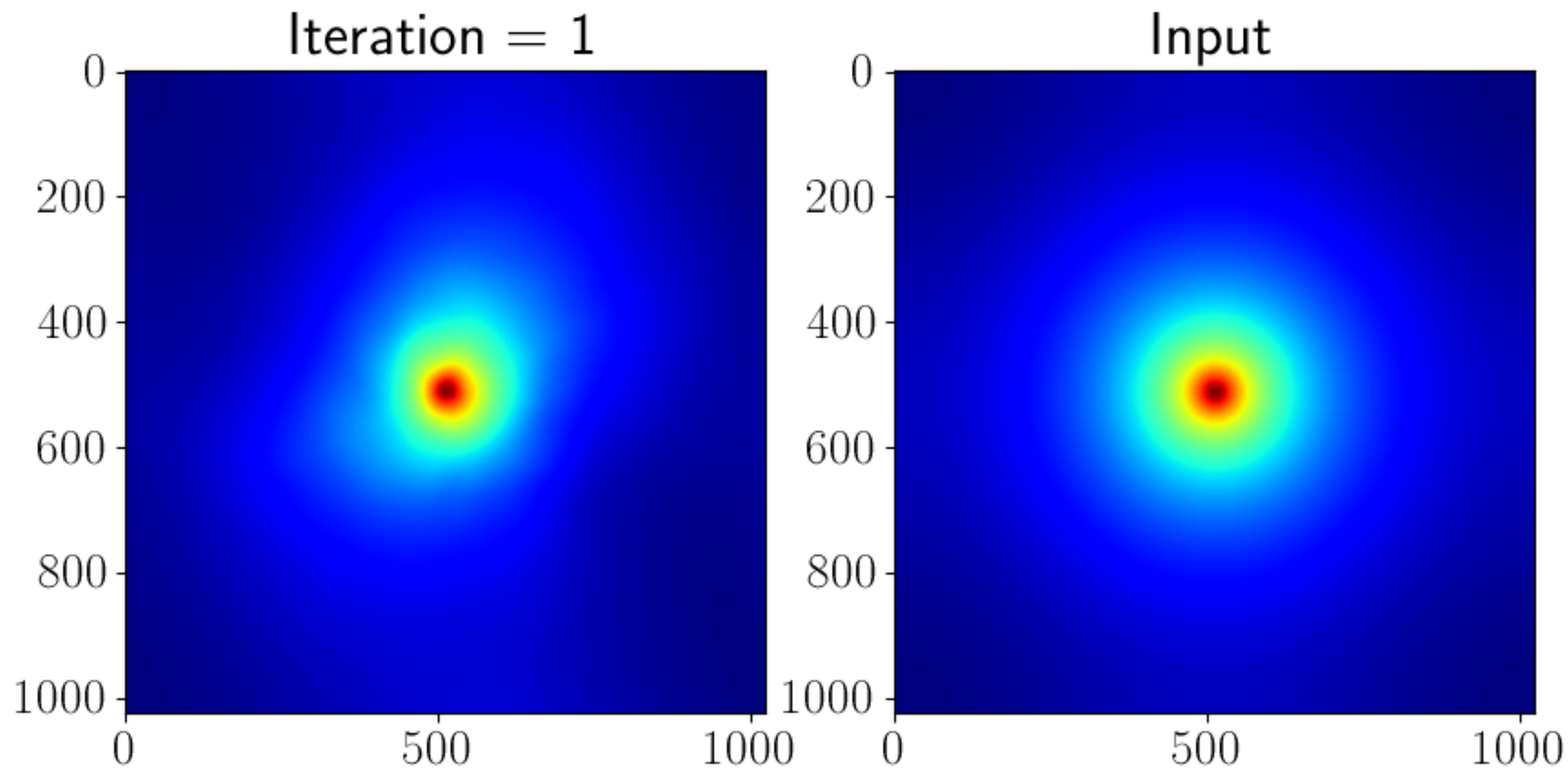


# AND THE MAGIC OF MAP ESTIMATOR...

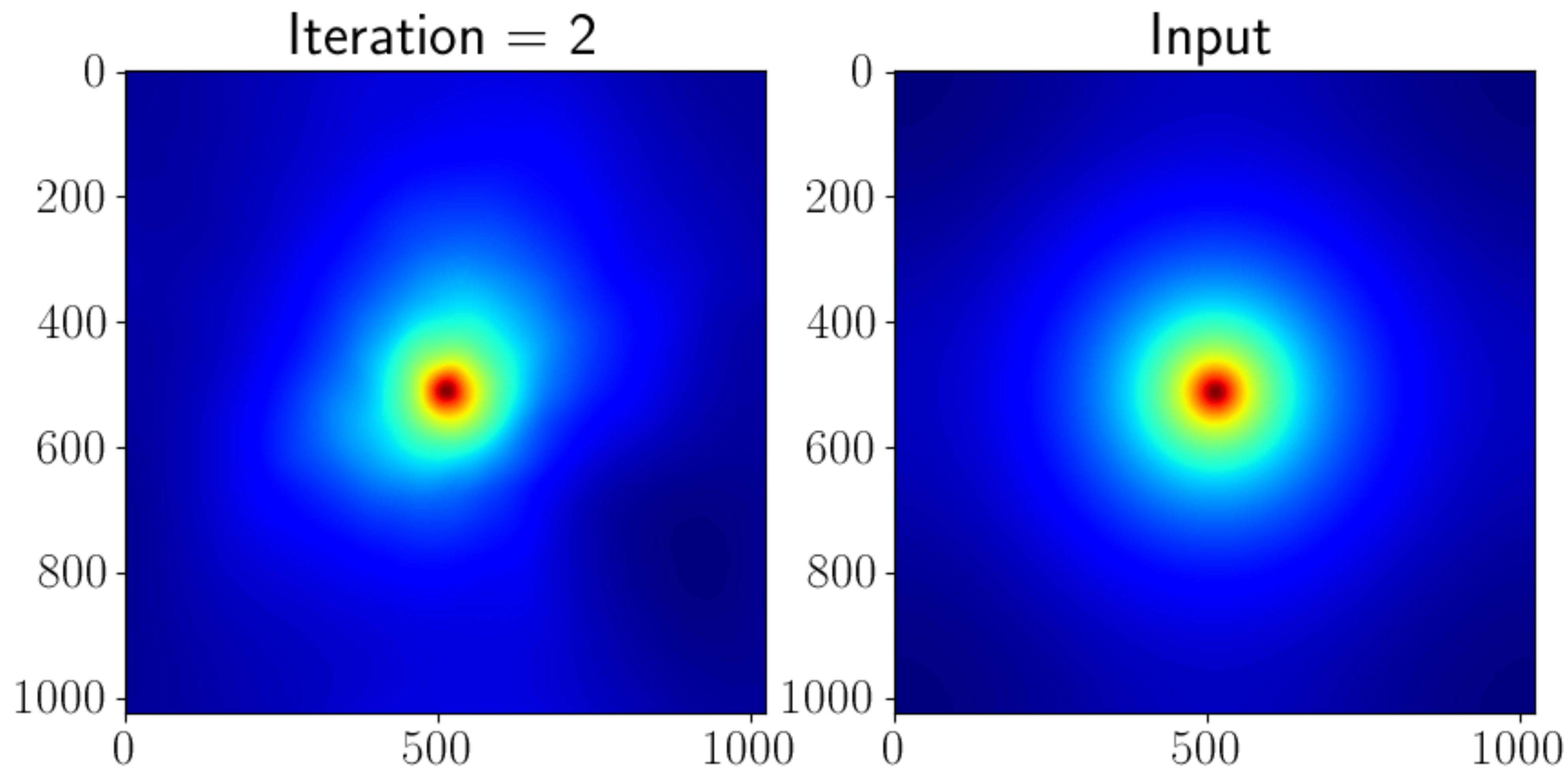
QE



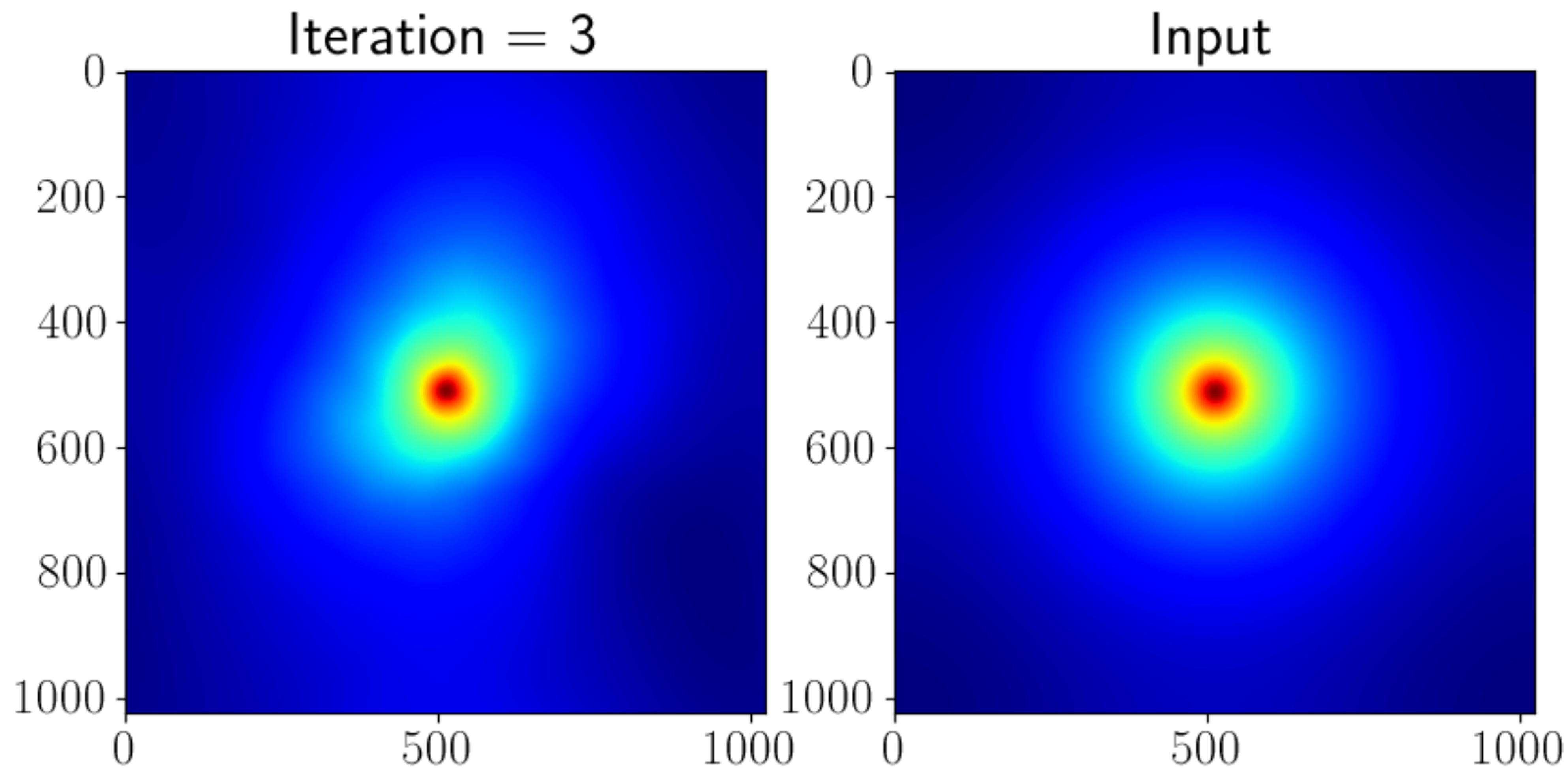
## AND THE MAGIC OF MAP ESTIMATOR...



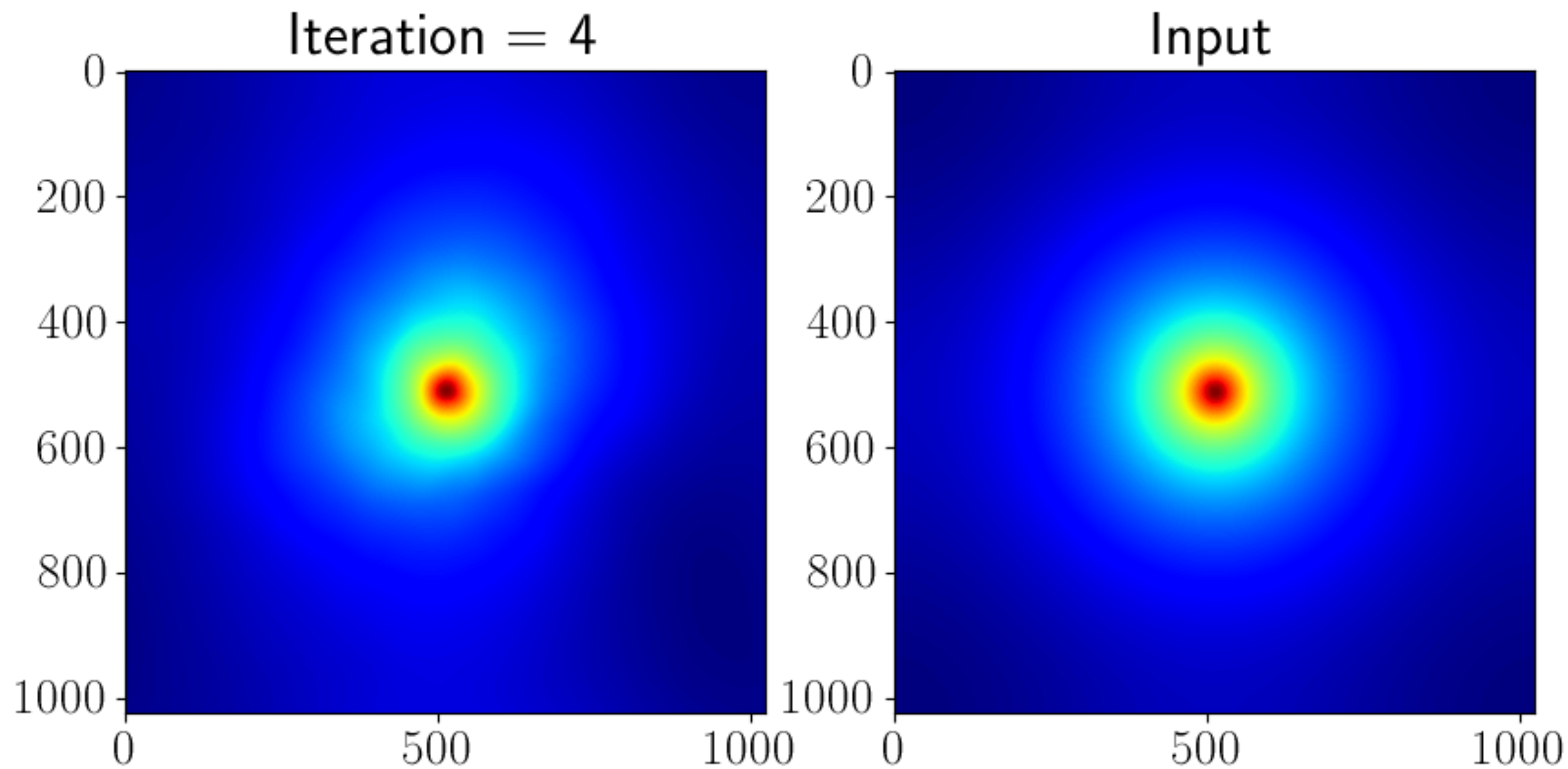
## AND THE MAGIC OF MAP ESTIMATOR...



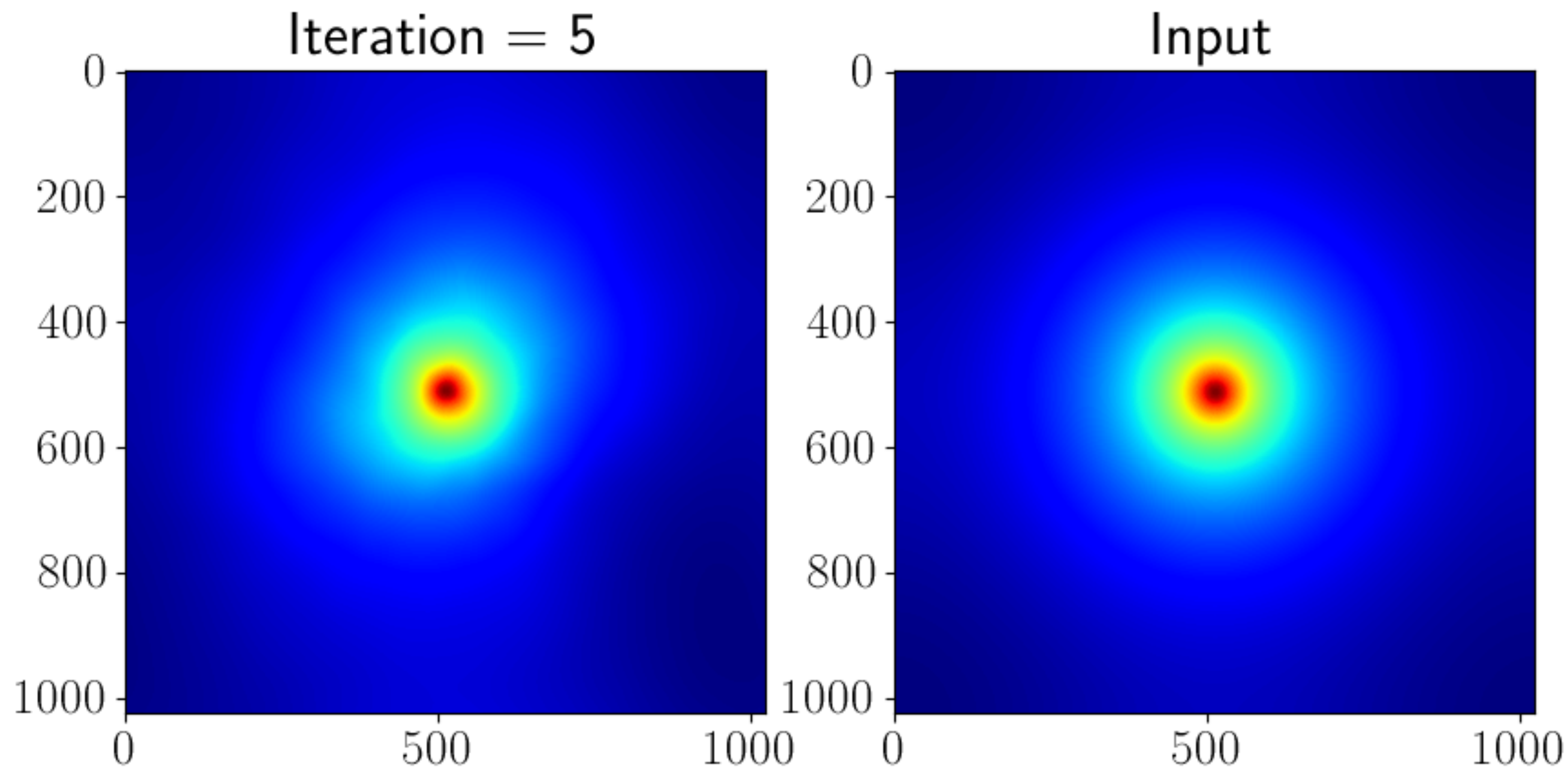
## AND THE MAGIC OF MAP ESTIMATOR...



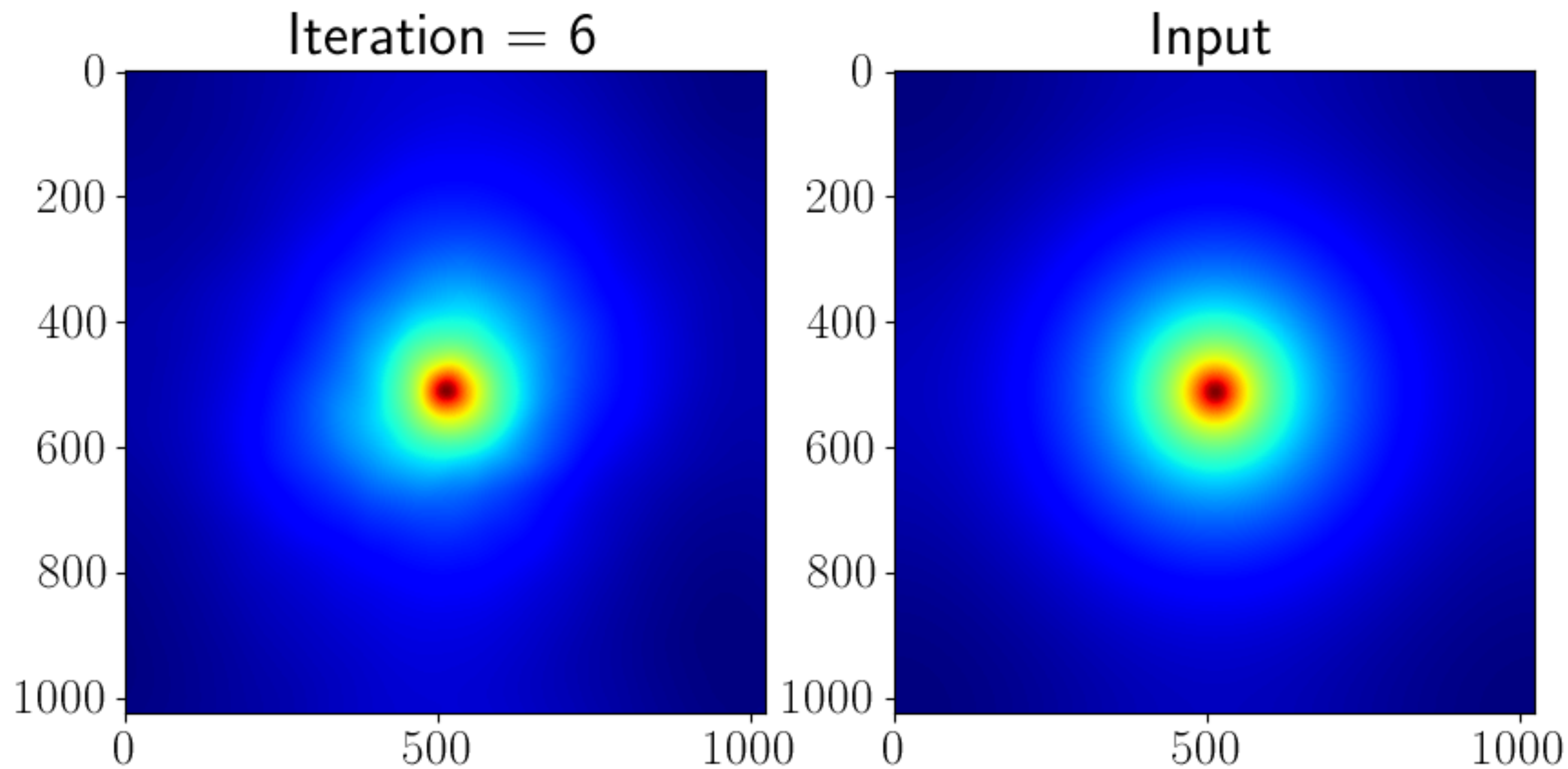
## AND THE MAGIC OF MAP ESTIMATOR...



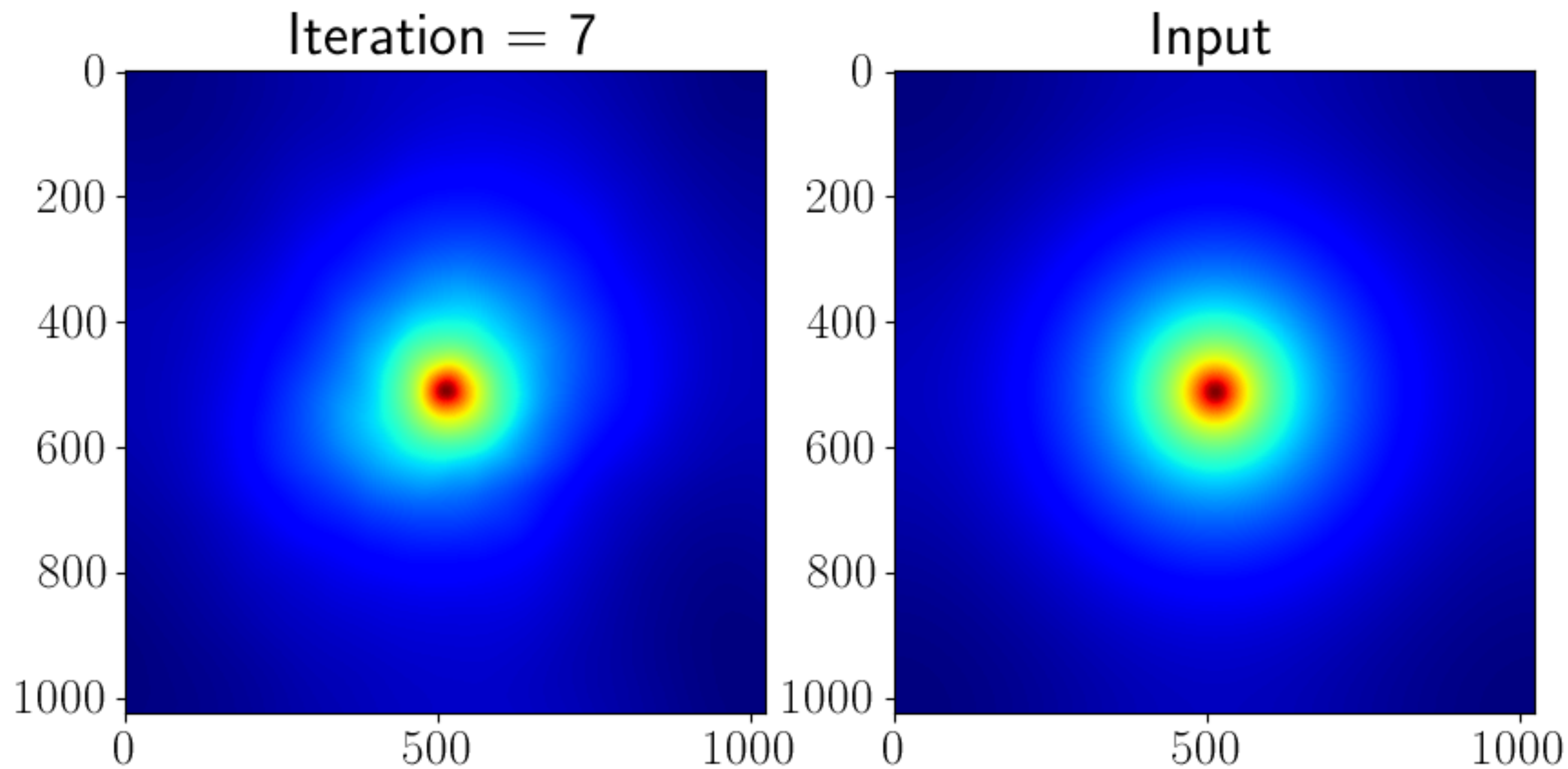
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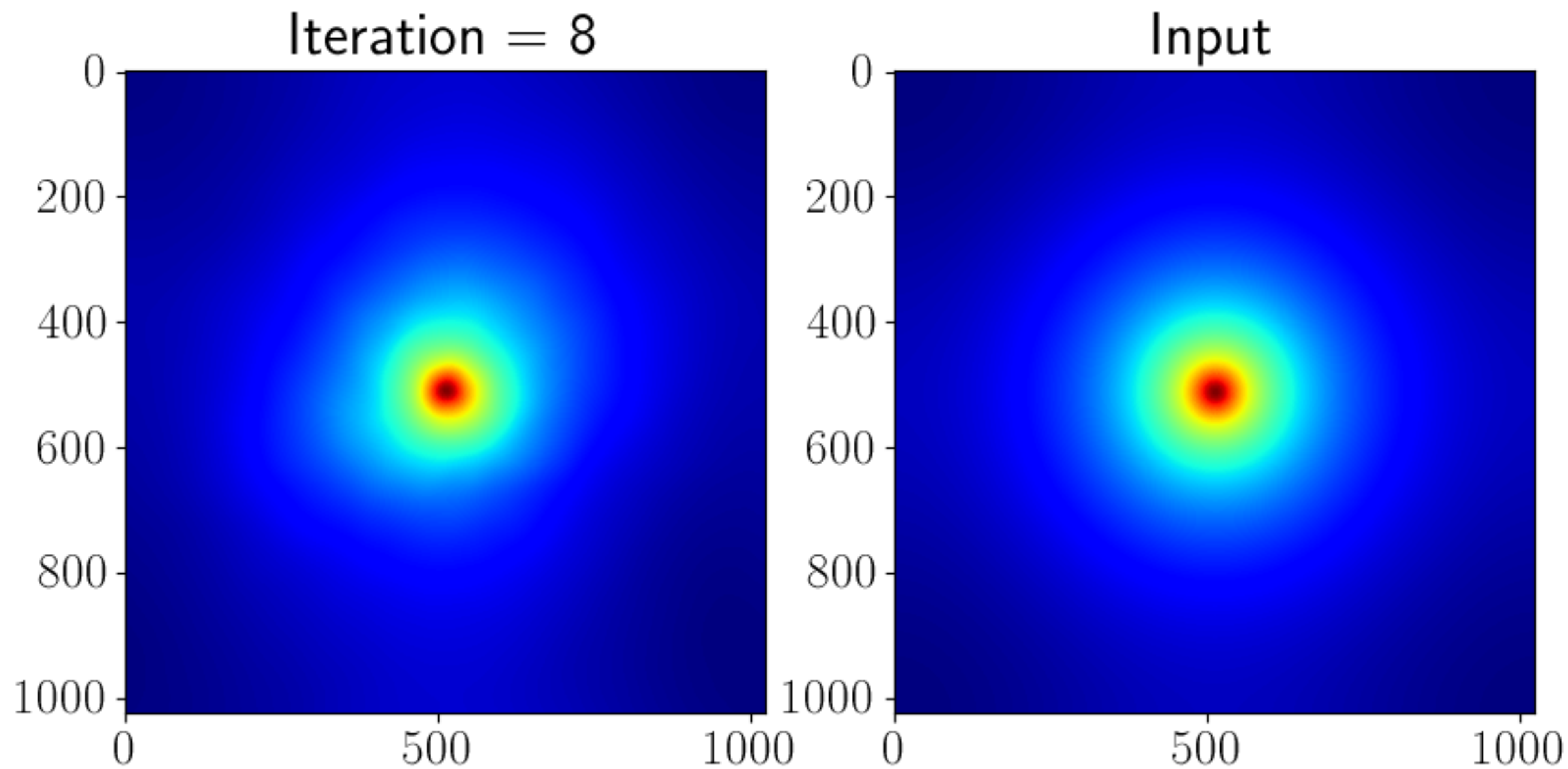


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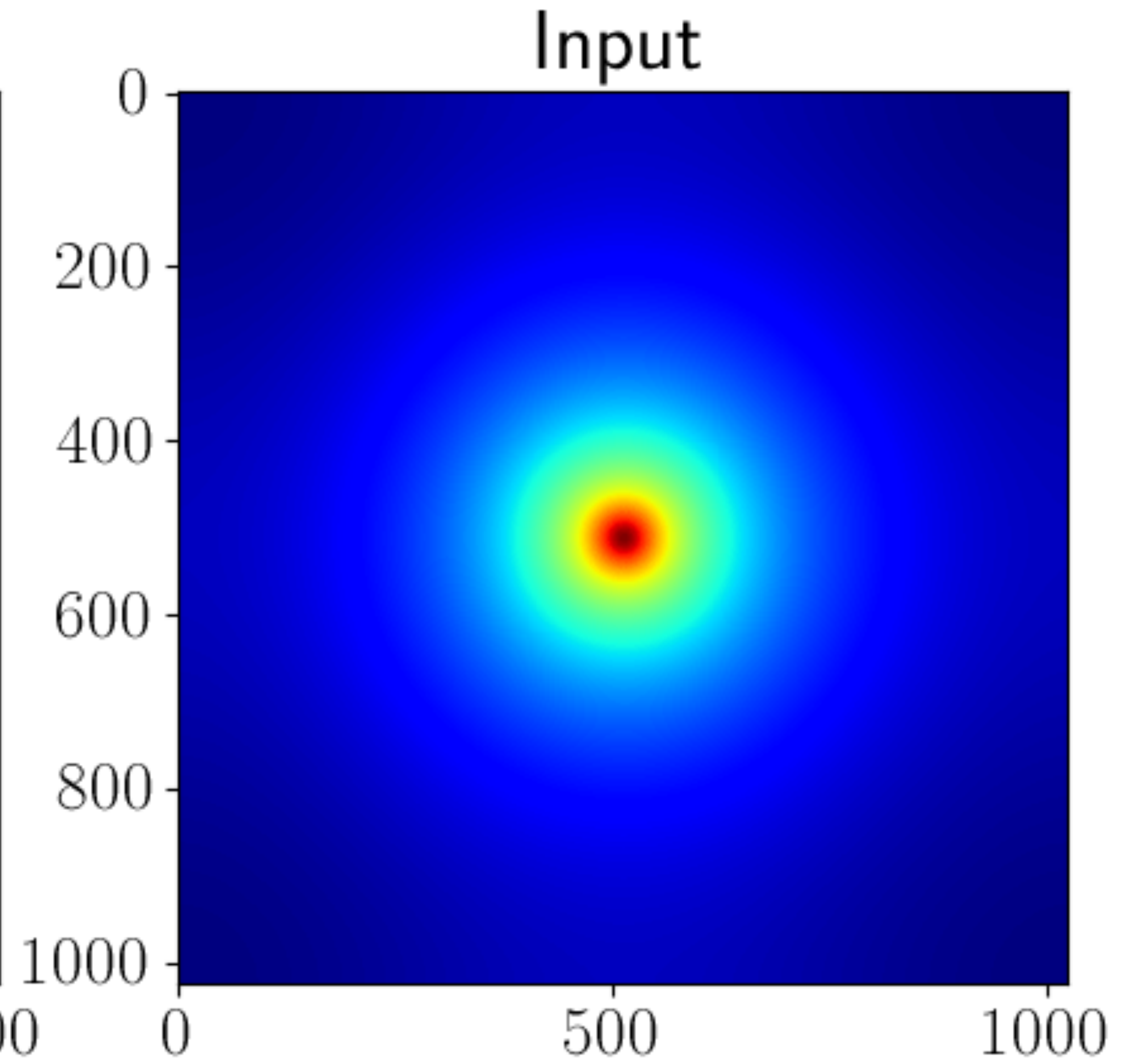
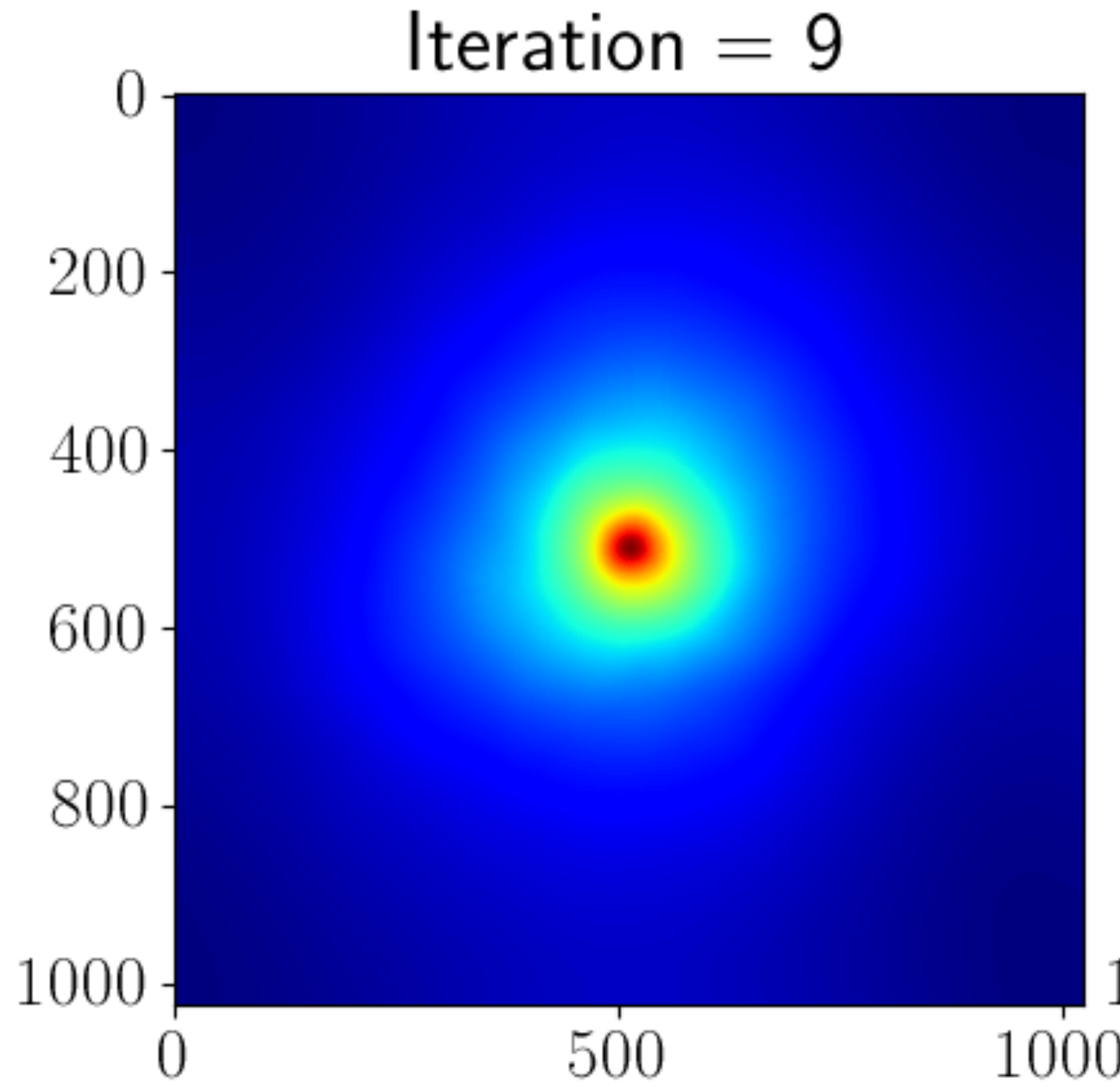


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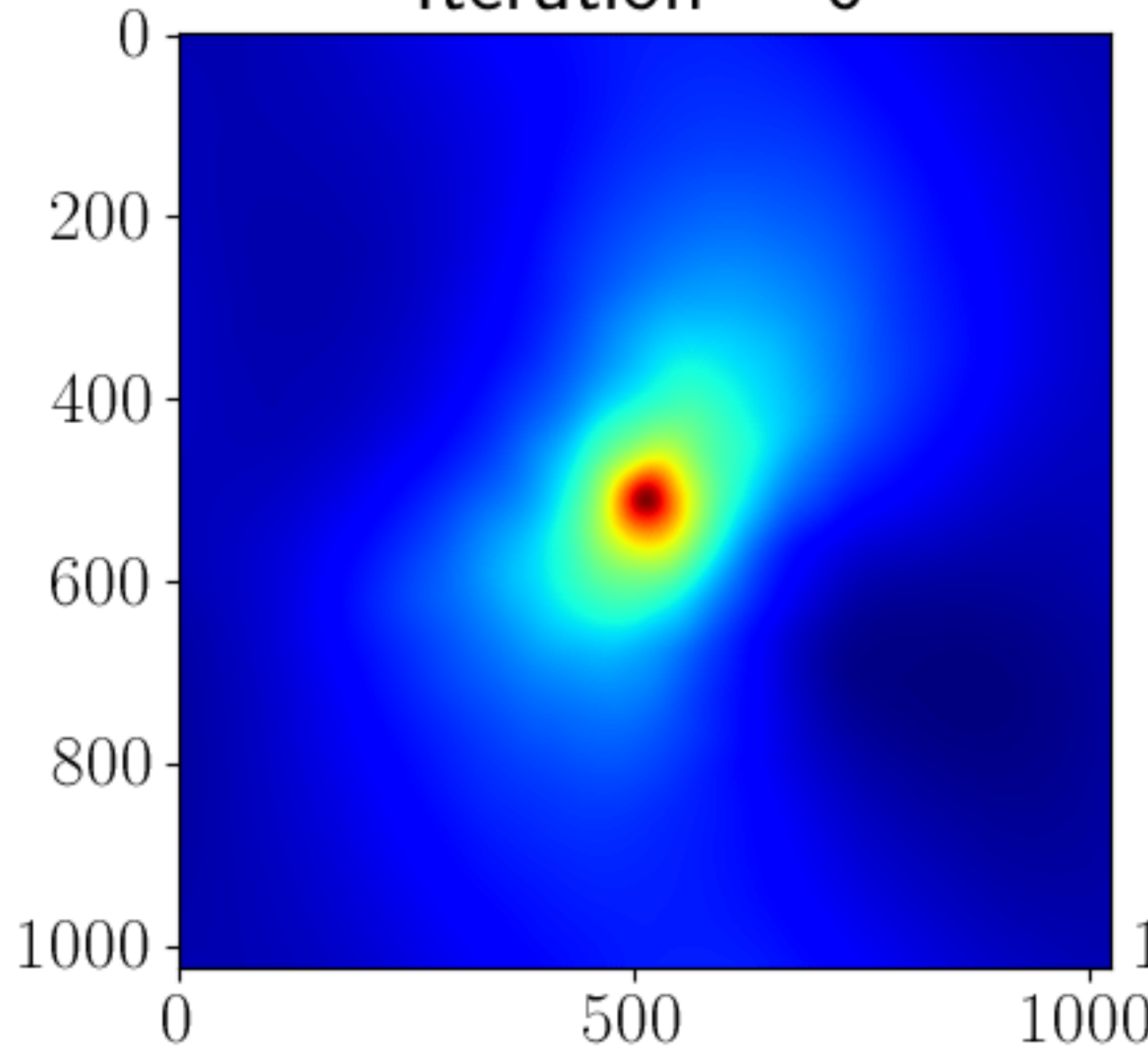
# AND THE MAGIC OF MAP ESTIMATOR...

MAP

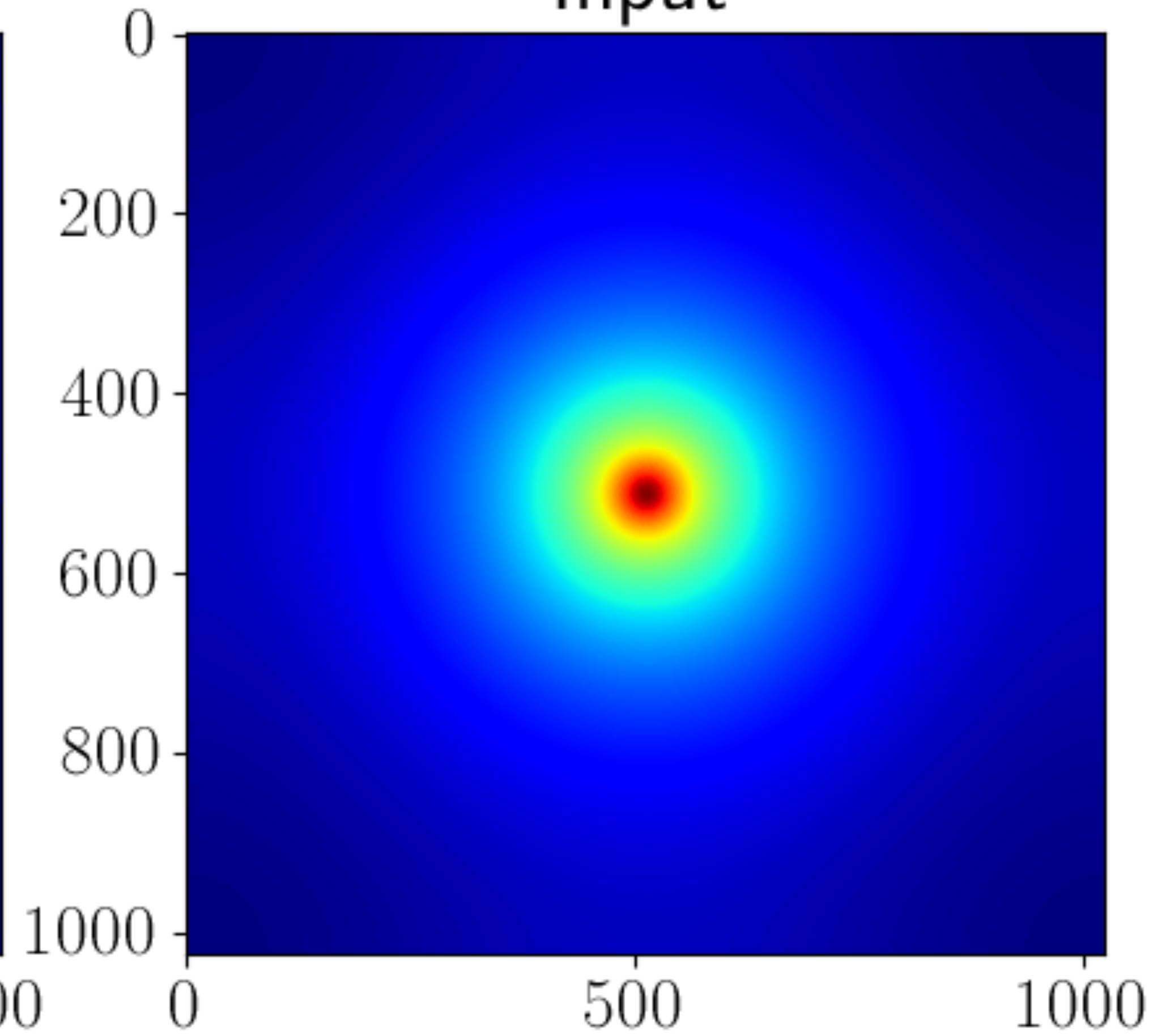


# AND THE MAGIC OF MAP ESTIMATOR...

Iteration = 0



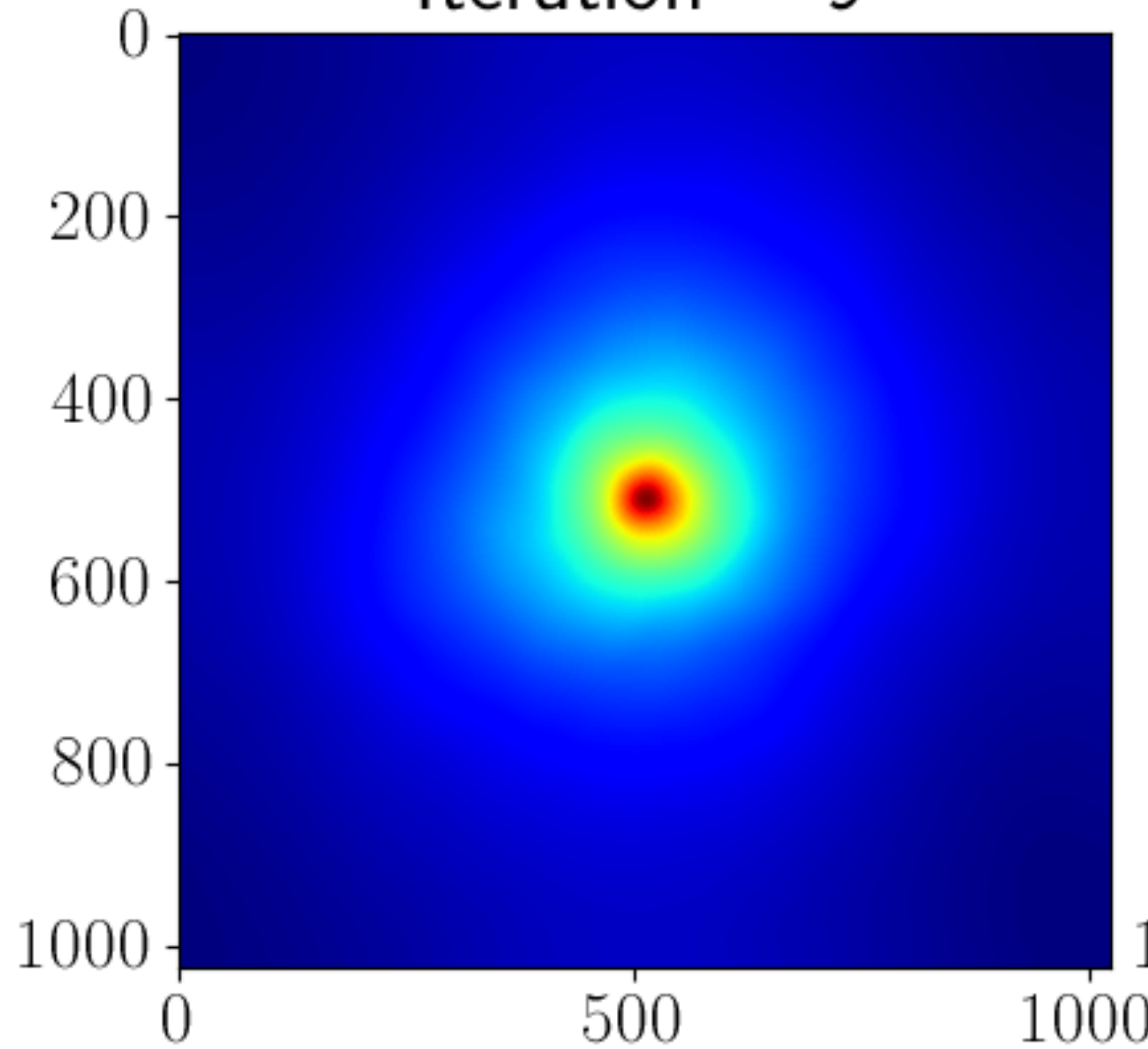
Input



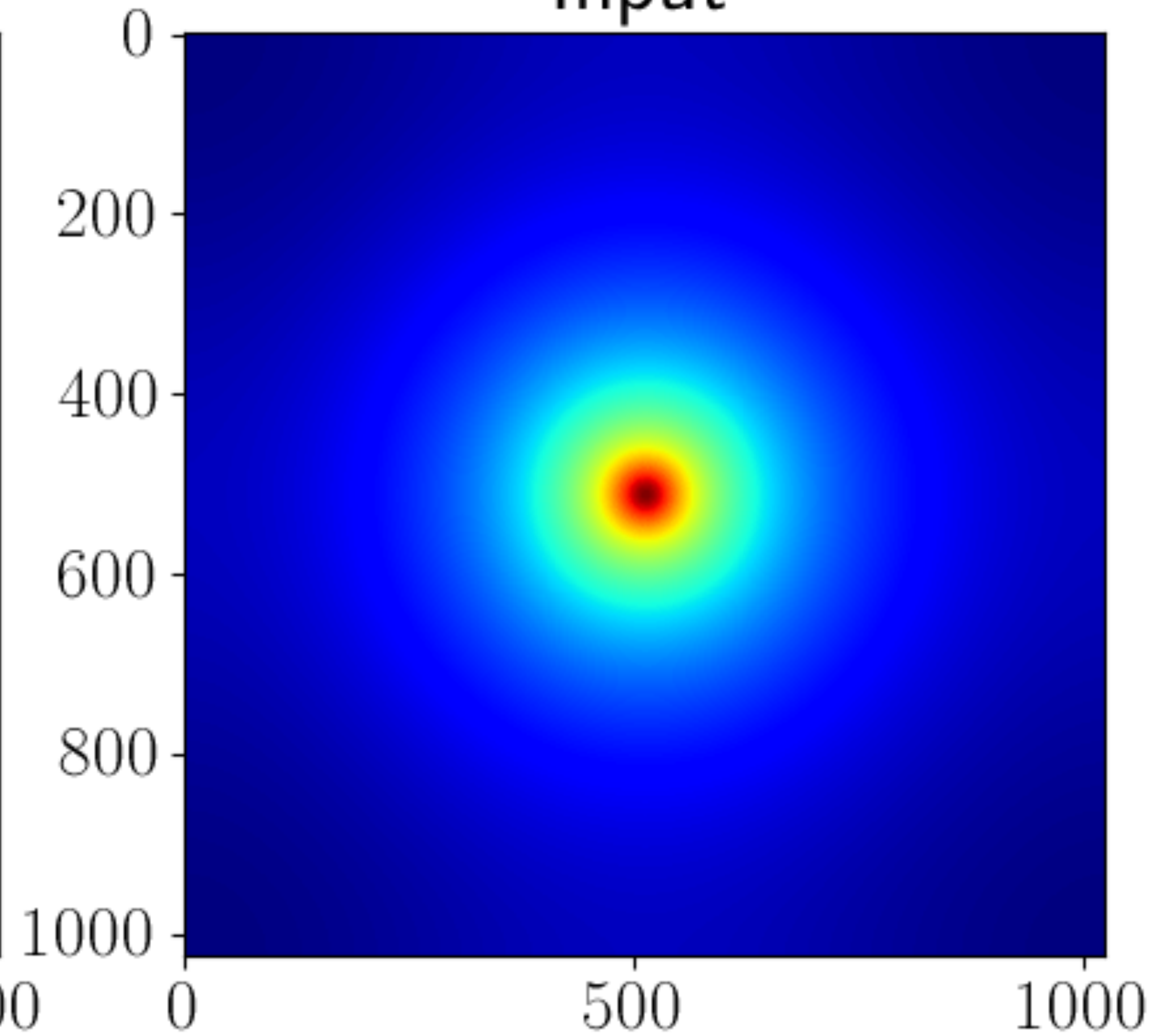
QE

# AND THE MAGIC OF MAP ESTIMATOR...

Iteration = 9



Input



MAP

# THANK YOU



Lensit



Website



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