

# Probing Fuzzy dark matter with lensed Gravitational waves

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Shashwat Singh  
(Shashwat.SINGH@obspm.fr)



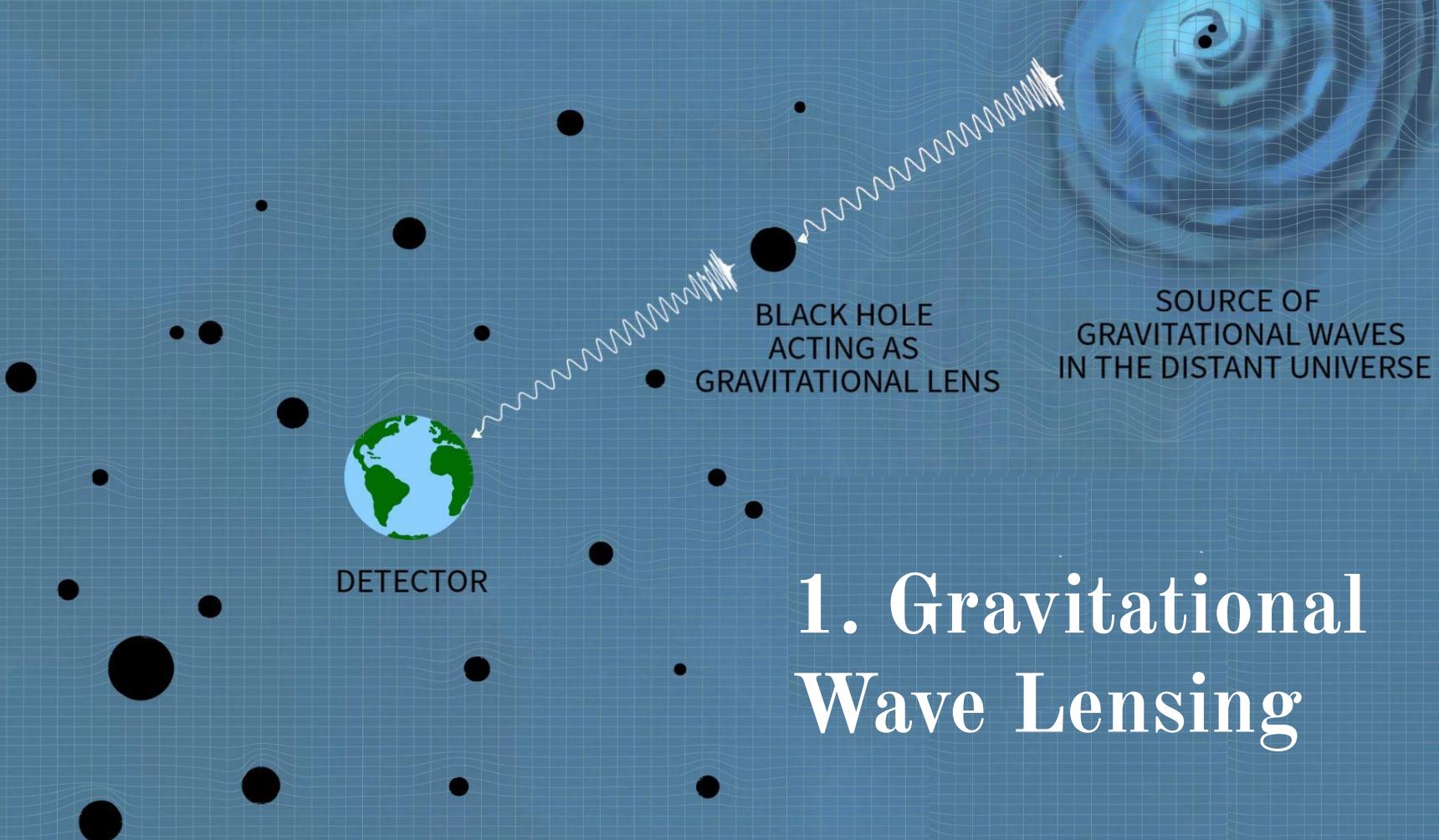
l'Observatoire de Paris – PSL

Collaborators : G. Brando, G. Tambalo, M. Zumalacárregui

Cosmology from Home 2023

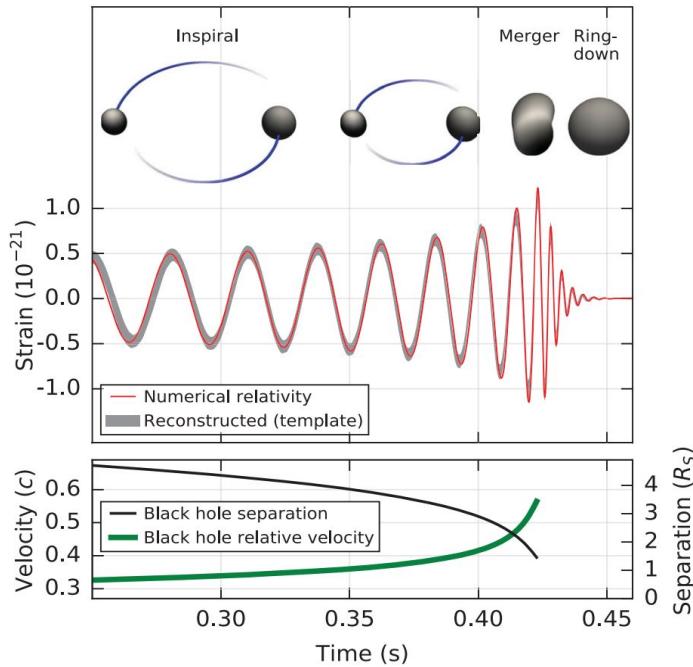
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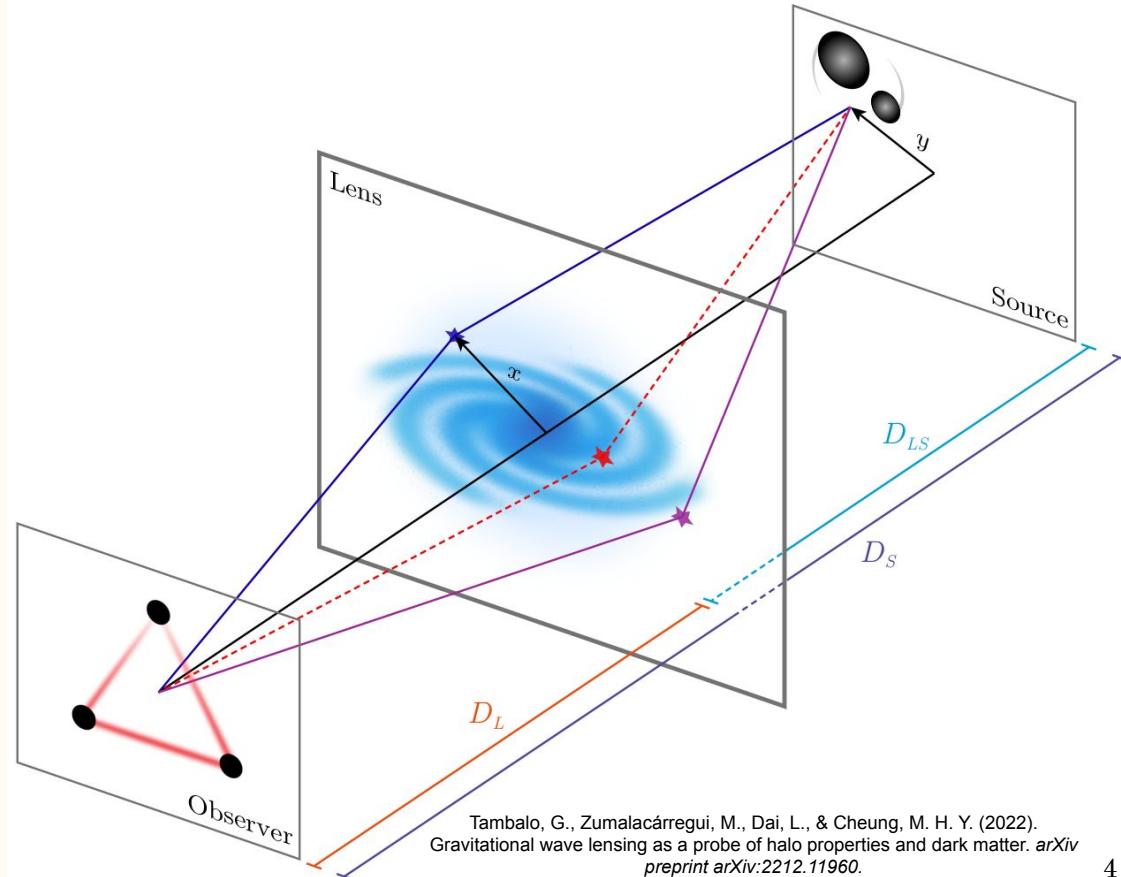


# 1. Gravitational Wave Lensing

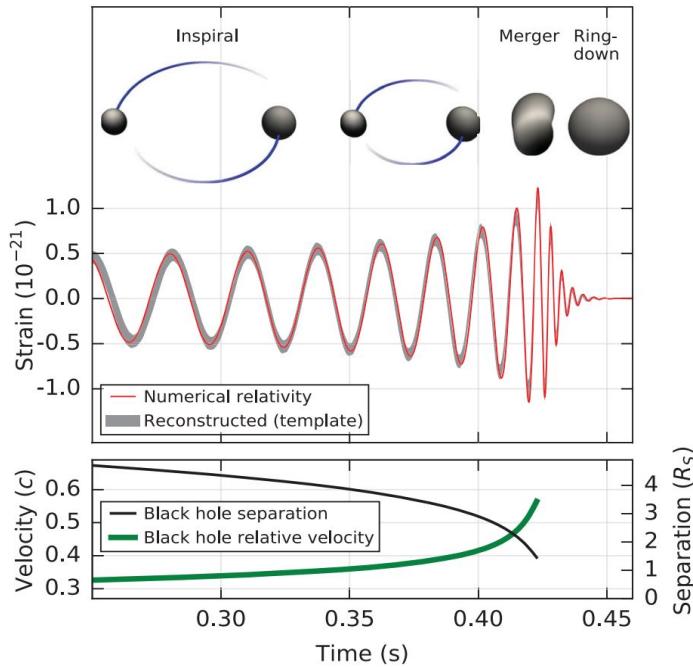
# Gravitational Wave Lensing



Abbott, B. P., Abbott, R., Abbott, T. D., Abernathy, M. R., Acernese, F., Ackley, K., ... & Cavalieri, R. (2016). Observation of gravitational waves from a binary black hole merger. *Physical review letters*, 116(6), 061102.



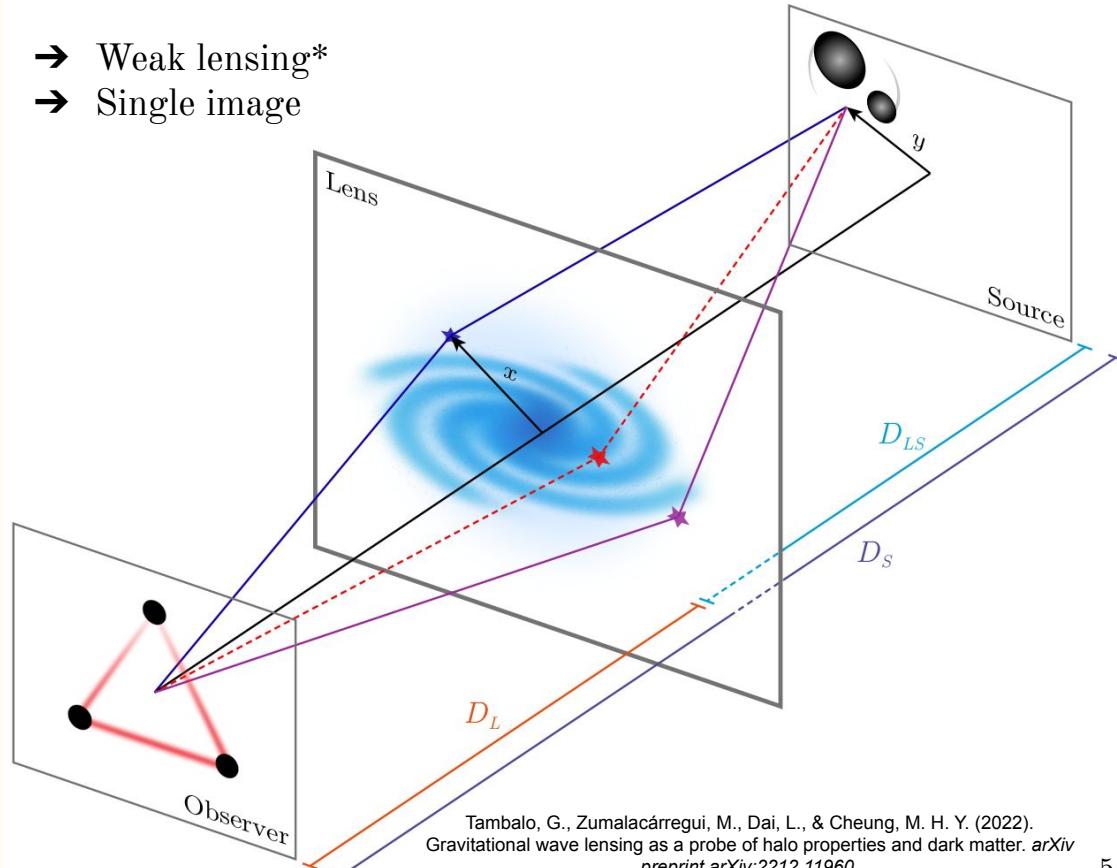
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\* Çalışkan, M., Ji, L., Cotesta, R., Berti, E., Kamionkowski, M., & Marsat, S. (2023). Observability of lensing of gravitational waves from massive black hole binaries with LISA. *Physical Review D*, 107(4), 043029.

- Weak lensing\*
- Single image



Tambalo, G., Zumalacárregui, M., Dai, L., & Cheung, M. H. Y. (2022). Gravitational wave lensing as a probe of halo properties and dark matter. *arXiv preprint arXiv:2212.11960*.

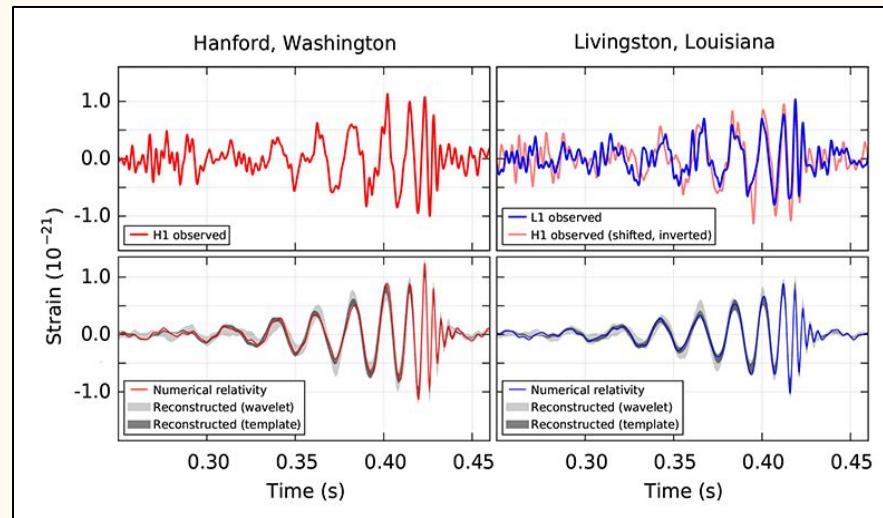
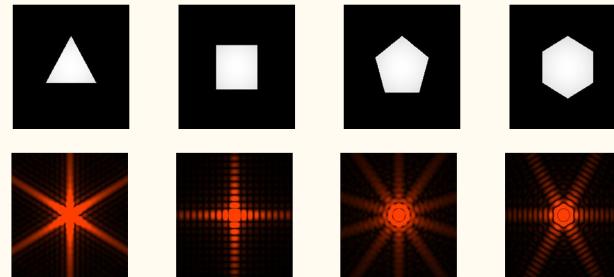
# Gravitational Wave Lensing – New cosmic messenger

Longer wavelength

Coherence of waves

Weakly coupled

accuracy of modeling



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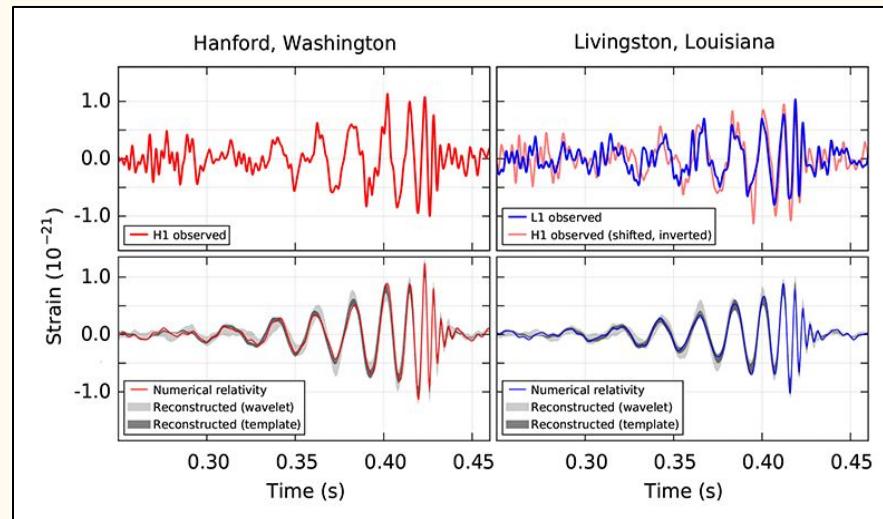
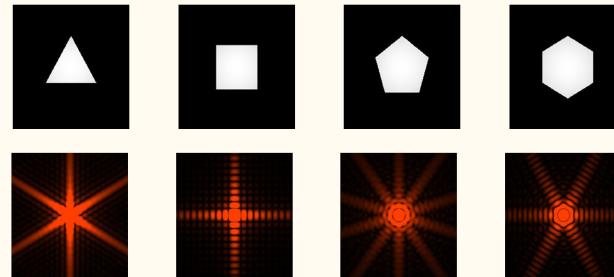
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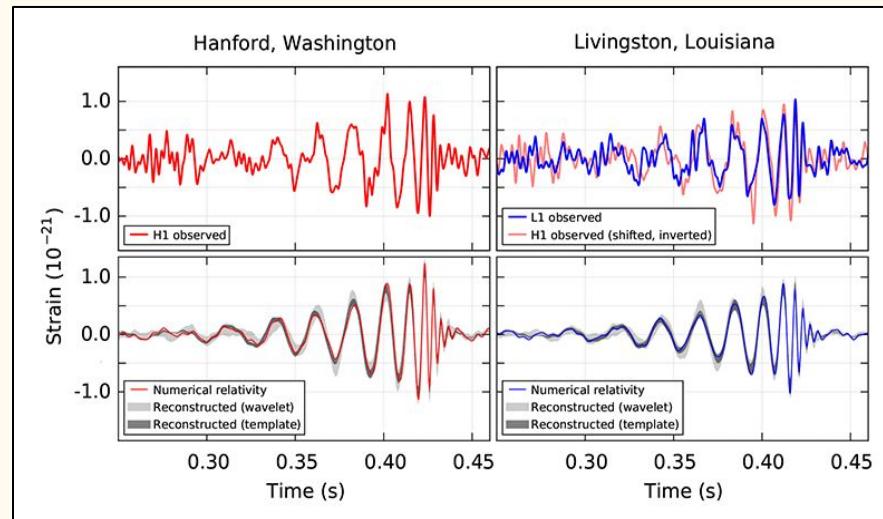
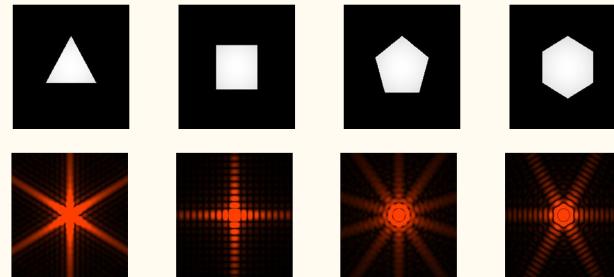
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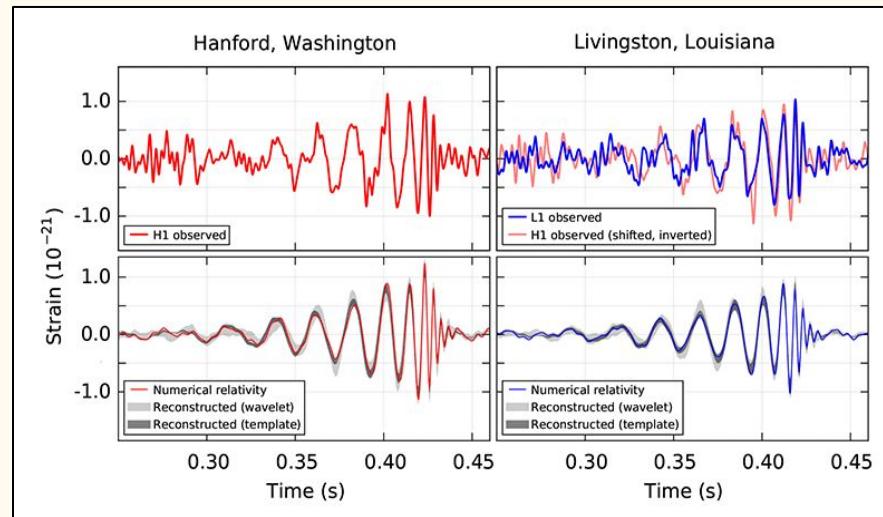
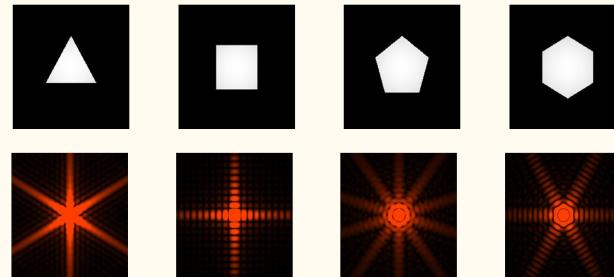
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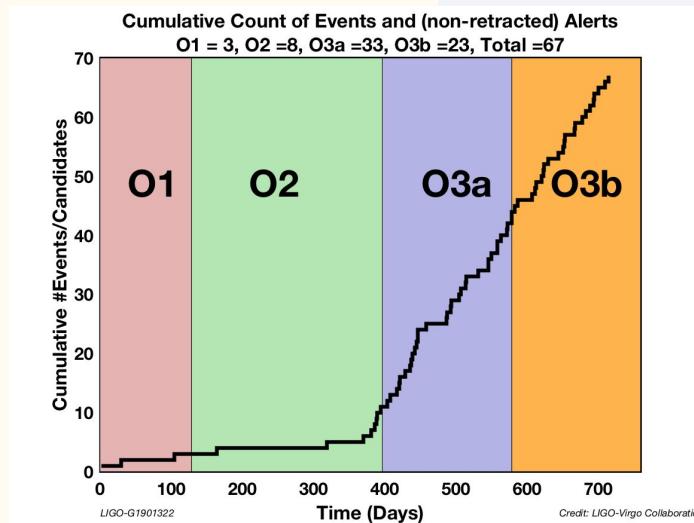


Image: <https://www.ligo.caltech.edu/news/ligo20200326>

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O4 Significant Detection Candidates: 6 (7 Total - 1 Re...

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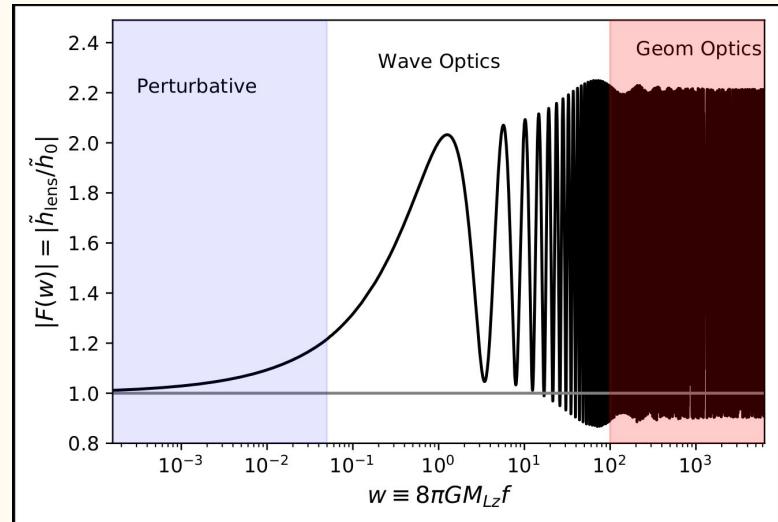
Show Significant Events Only

<https://gracedb.ligo.org/superevents/public/O4/>

# Oscillations in amplification factor

$$F(\omega) \equiv \frac{\tilde{h}}{\tilde{h}_0}$$

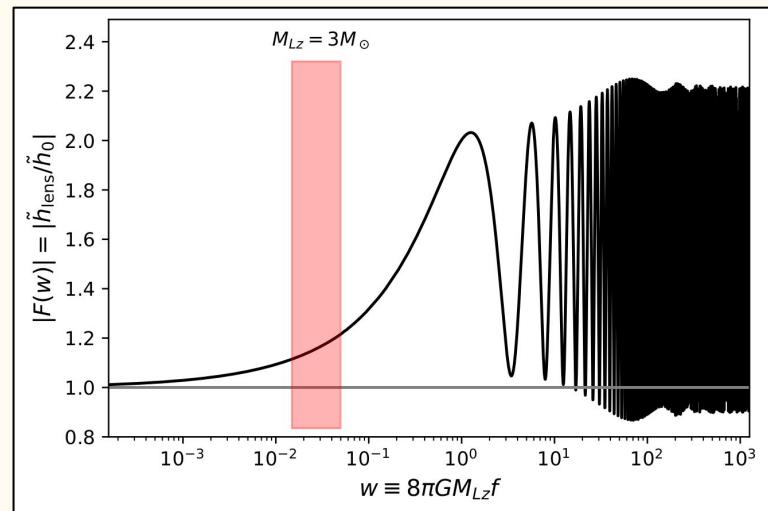
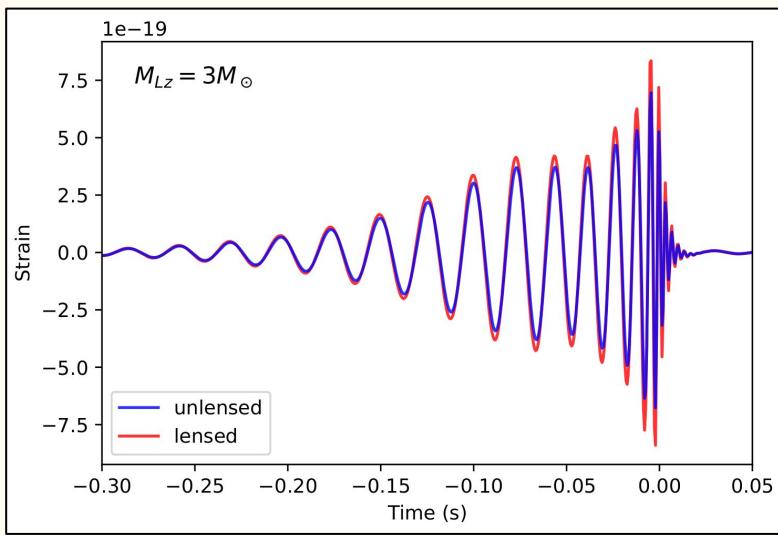
$$\omega \equiv 8\pi GM_{Lz}f \sim \left( \frac{M_{Lz}}{10^4 M_\odot} \right) \left( \frac{f}{Hz} \right)$$



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Perturbative regime

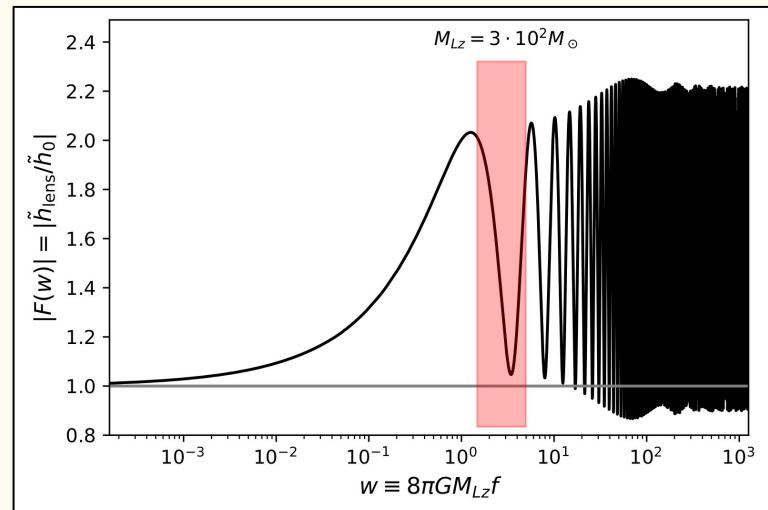
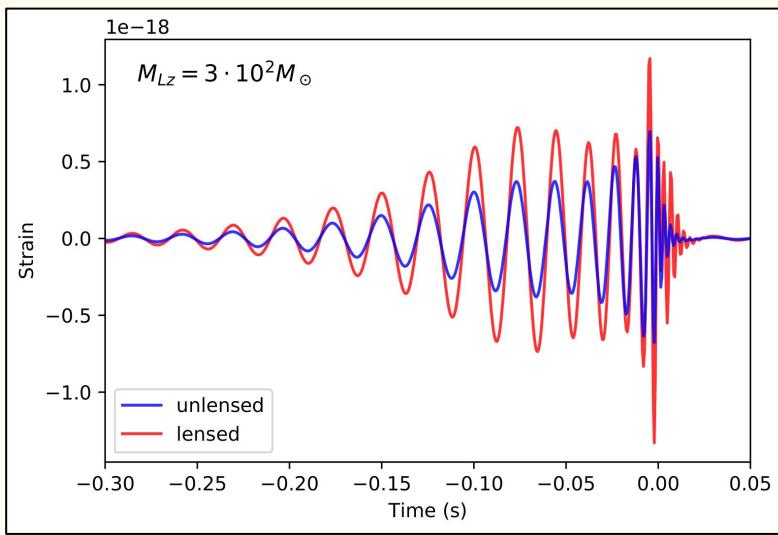
$$\omega \ll 1$$

$$F(\omega) \sim 1 + A\omega^\alpha$$

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$$F(\omega) \equiv \frac{\tilde{h}}{\tilde{h}_0}$$

$$\omega \equiv 8\pi GM_{Lz}f \sim \left( \frac{M_{Lz}}{10^4 M_\odot} \right) \left( \frac{f}{Hz} \right)$$



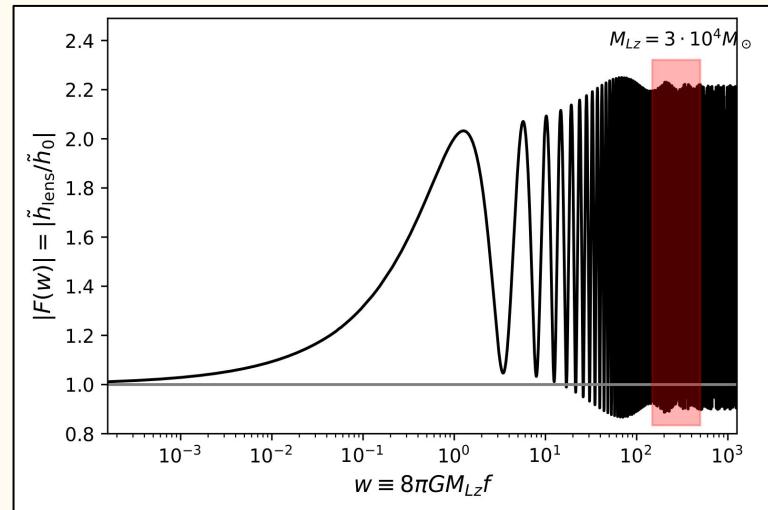
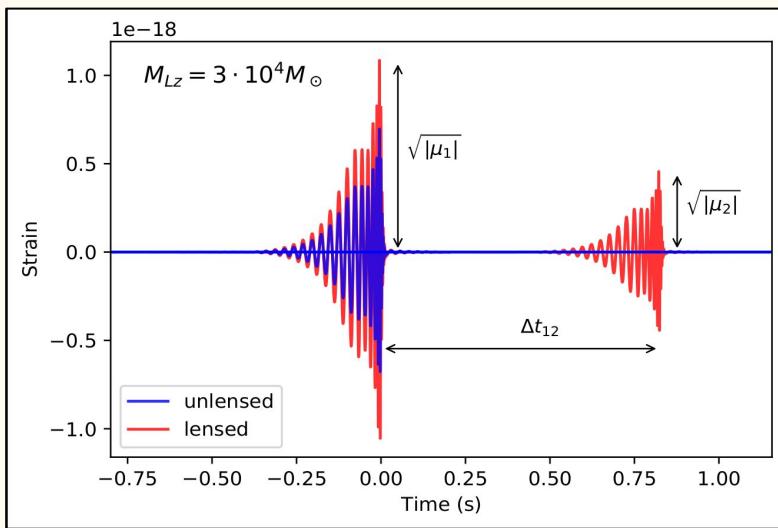
**Wave Optics (WO) regime**

$$F(\omega) = \frac{\omega}{2\pi i} \int d^2x e^{i\omega\phi(x,y)}$$

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$$F(\omega) \equiv \frac{\tilde{h}}{\tilde{h}_0}$$

$$\omega \equiv 8\pi GM_{Lz}f \sim \left( \frac{M_{Lz}}{10^4 M_\odot} \right) \left( \frac{f}{Hz} \right)$$



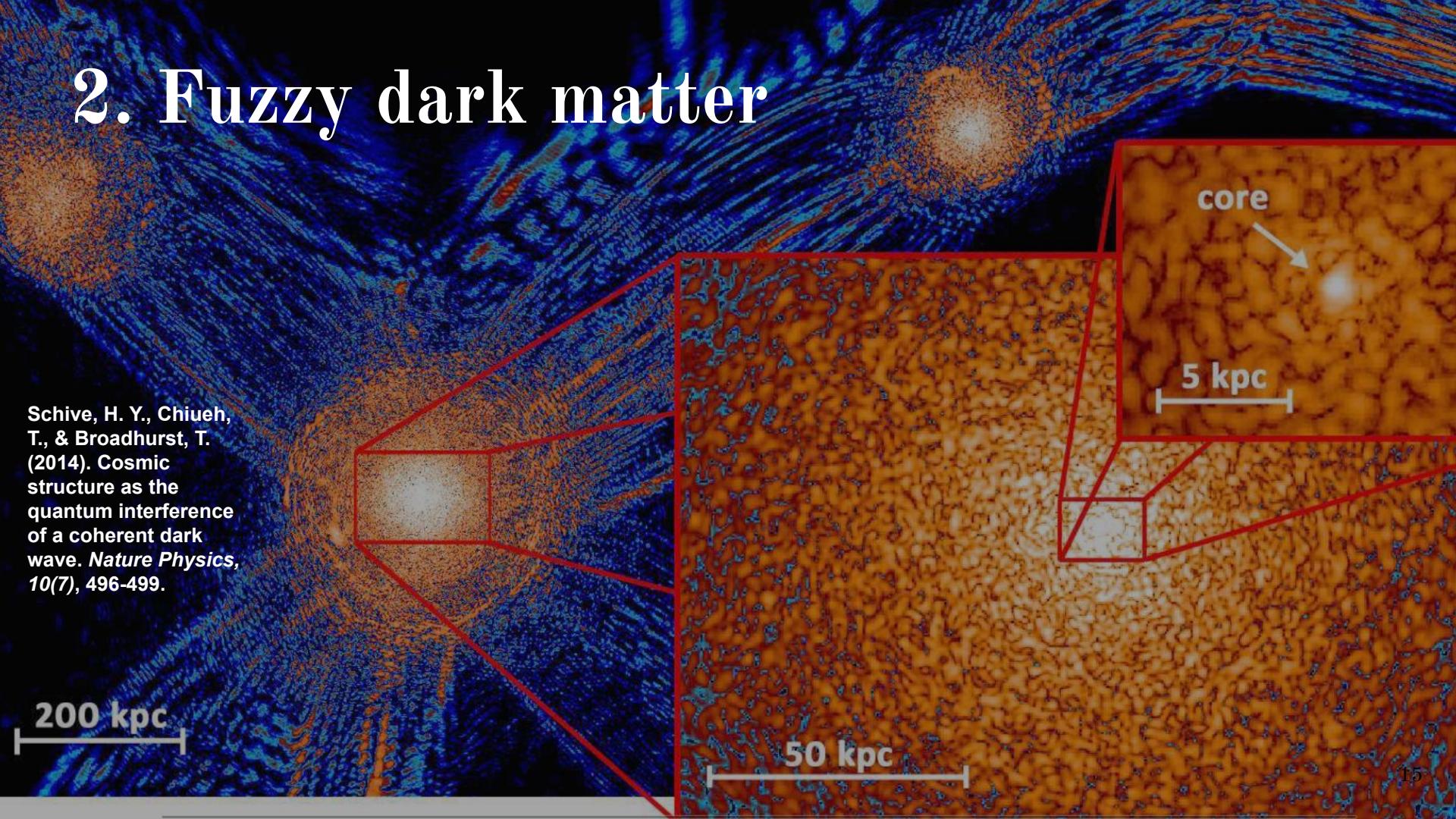
**Geometric optics (GO) regime**

$$\omega \gg 1$$

$$F(\omega) = \sum_J |\mu_J|^{1/2} e^{i\omega\phi_J - i\pi n_J}$$

## 2. Fuzzy dark matter

Schive, H. Y., Chiueh, T., & Broadhurst, T. (2014). Cosmic structure as the quantum interference of a coherent dark wave. *Nature Physics*, 10(7), 496-499.



# Cold dark matter: Issues on small scales

Core cusp  
problem

Too big to  
fail

Number  
density of  
halos

Earliest  
structure  
 $z \sim 50$

# Cold dark matter: Issues on small scales

Core cusp  
problem

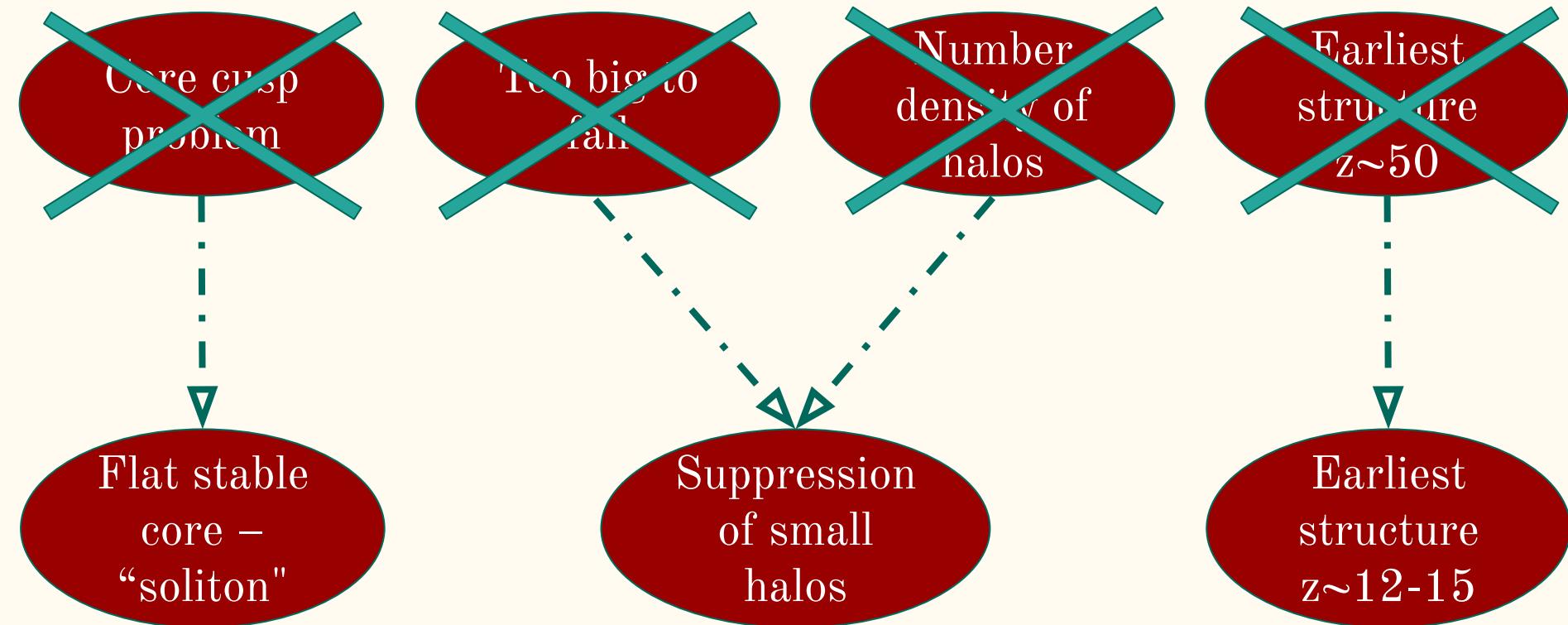
Too big to  
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Number  
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Earliest  
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 $z \sim 50$

very light bosons     $m_\phi \sim 10^{-22} - 10^{-23}$  eV

# Cold dark matter: Issues on small scales

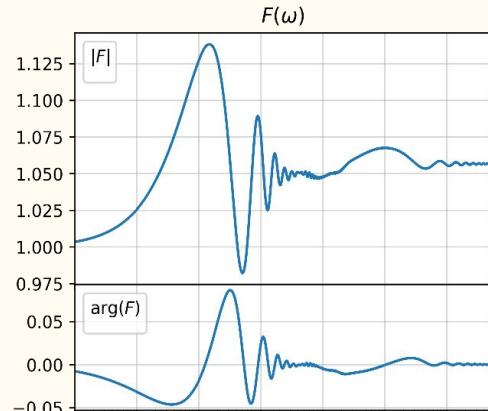
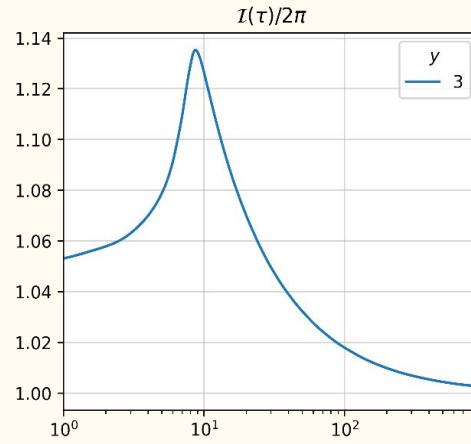
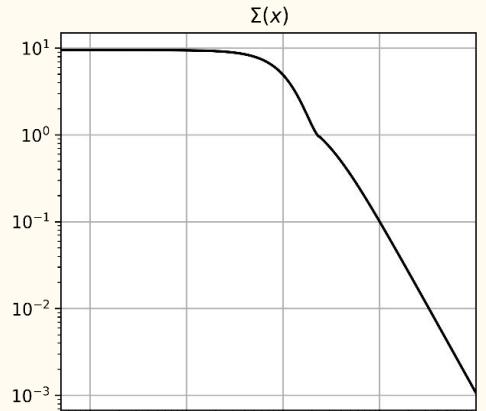


# 3. Lensing Features

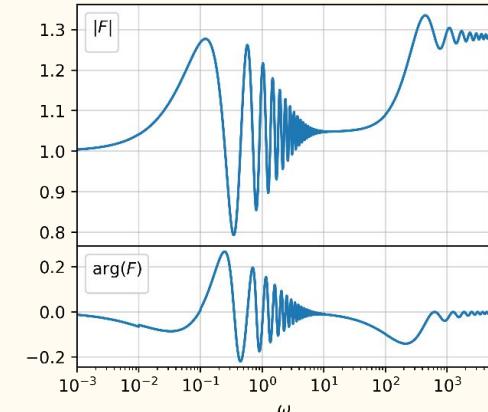
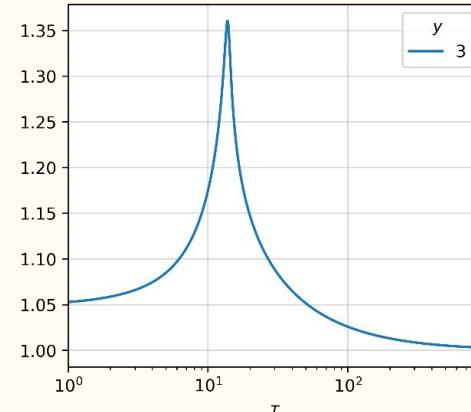
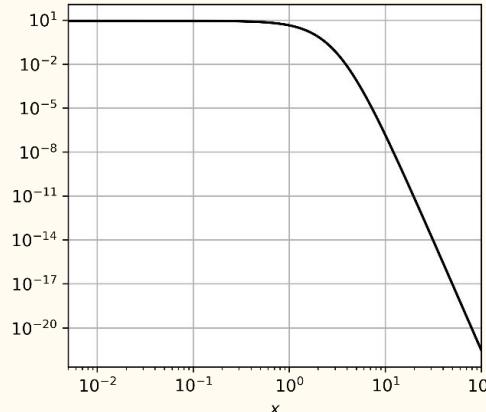
Einstein Rings of LRG 3-757 taken with the Hubble Space Telescope's Wide Field Camera 3.  
Image : <https://apod.nasa.gov/apod/ap111221.html>

# Lensing Features

FDM

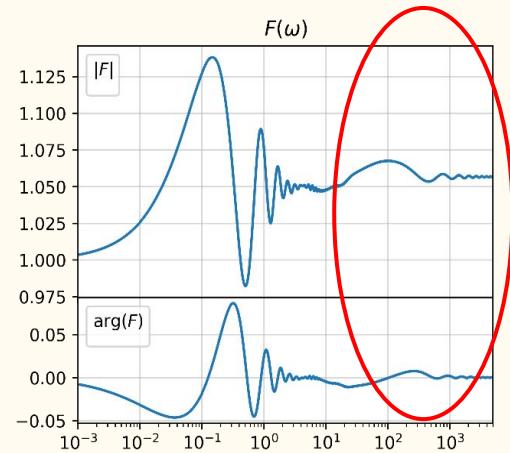
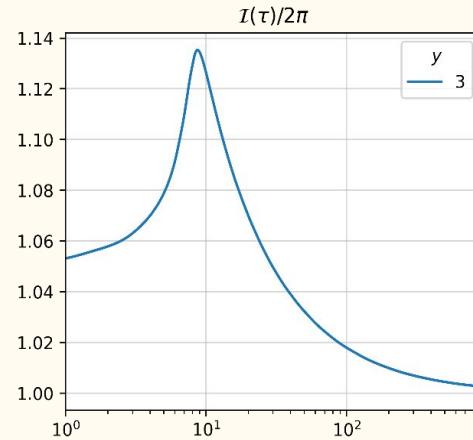
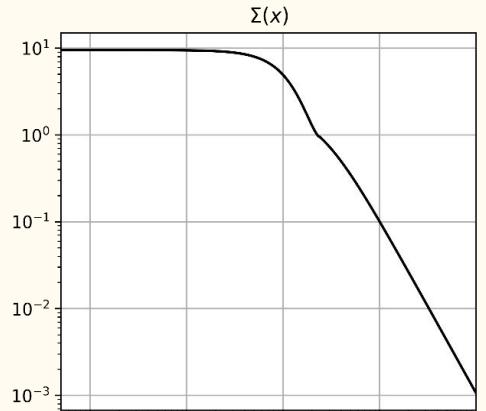


SC

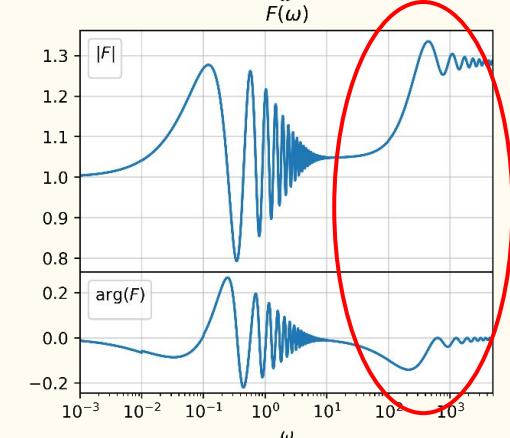
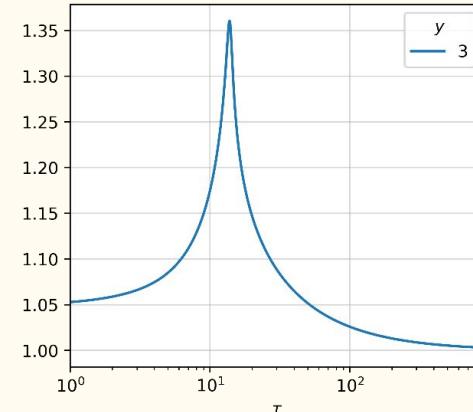
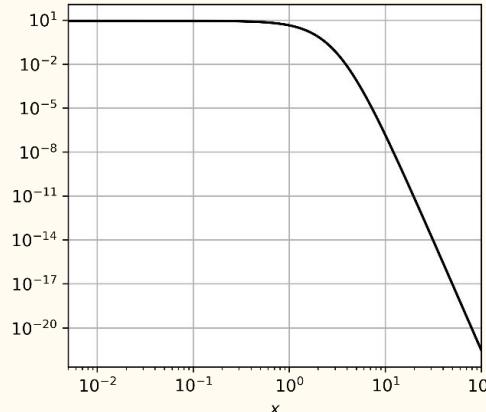


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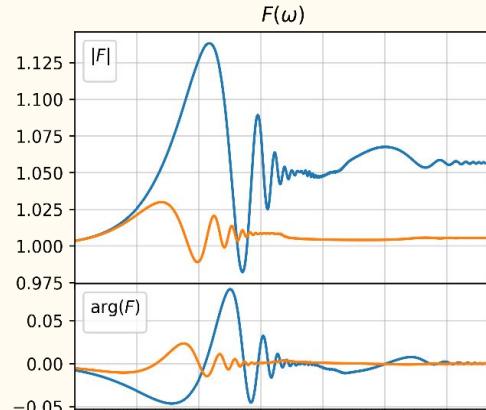
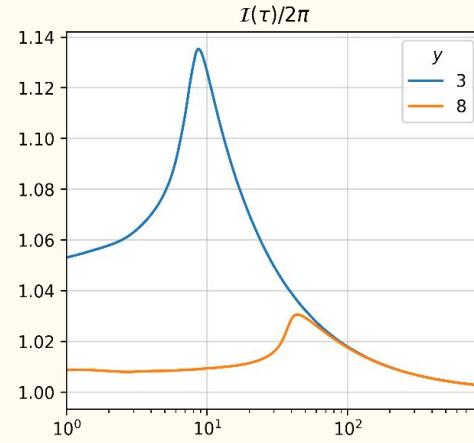


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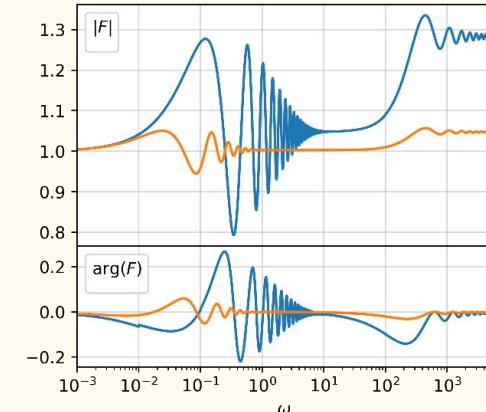
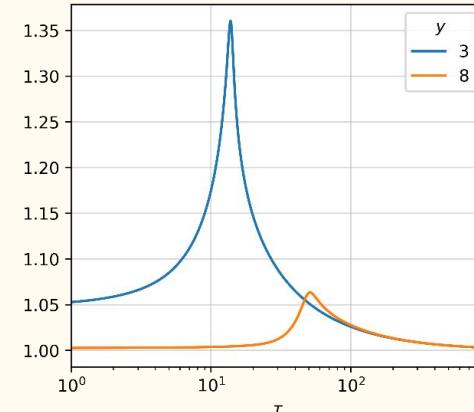
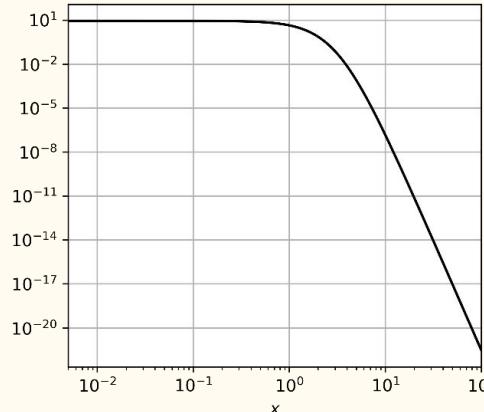


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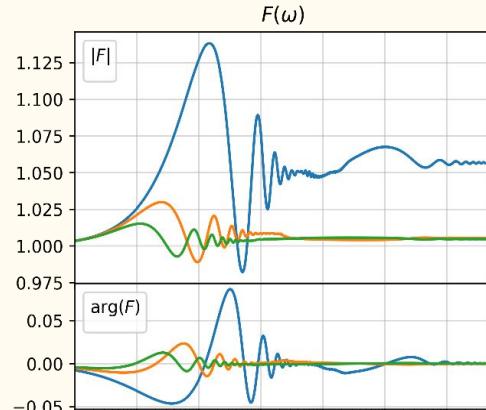
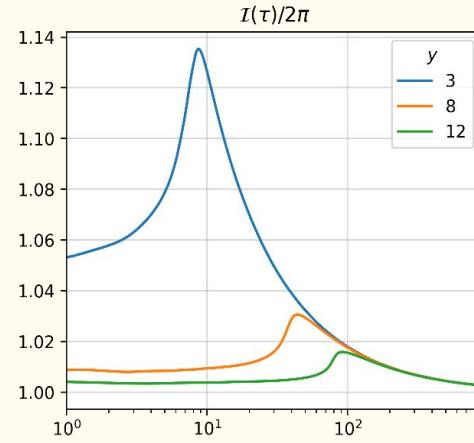
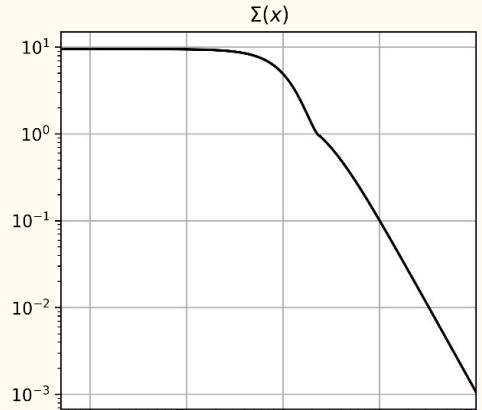


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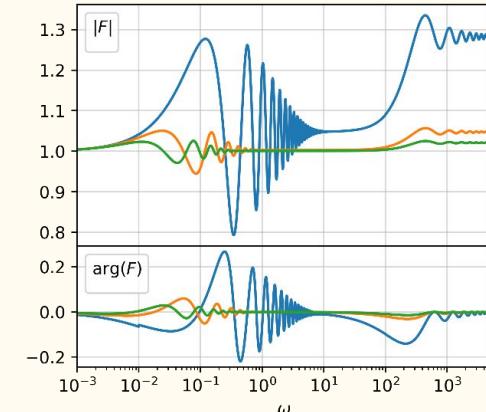
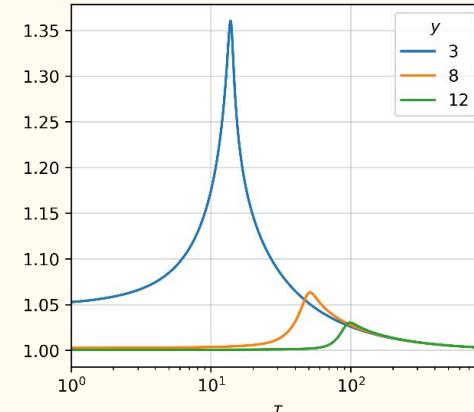
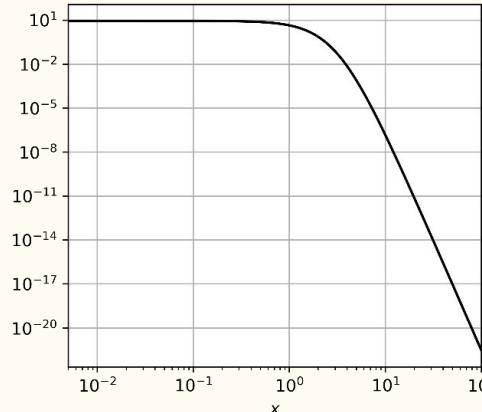


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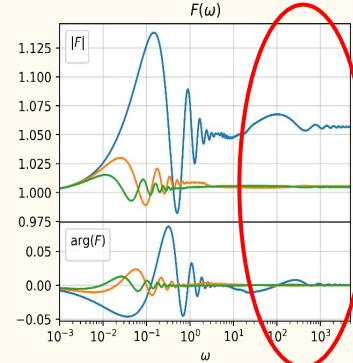
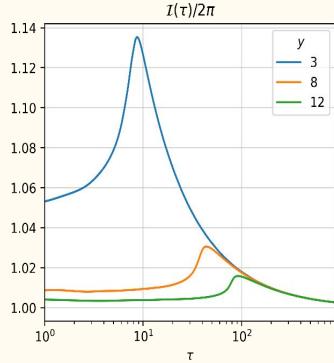
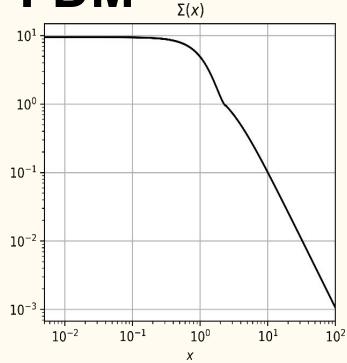


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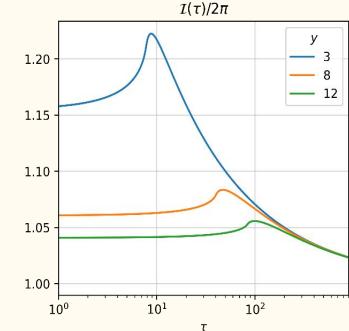
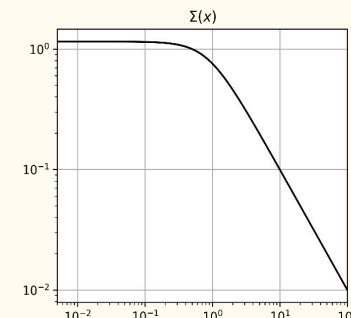


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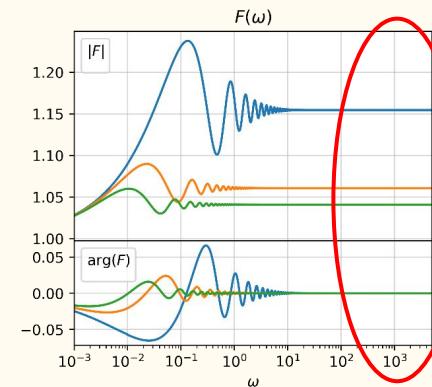
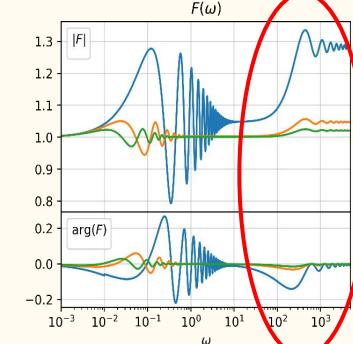
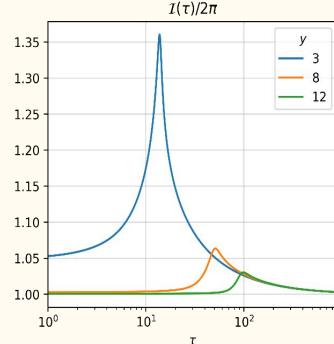
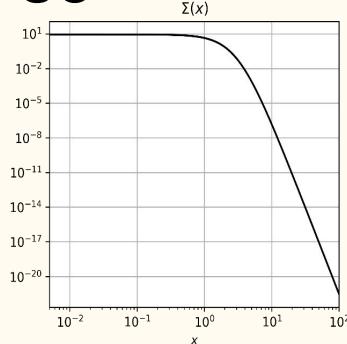
**FDM**



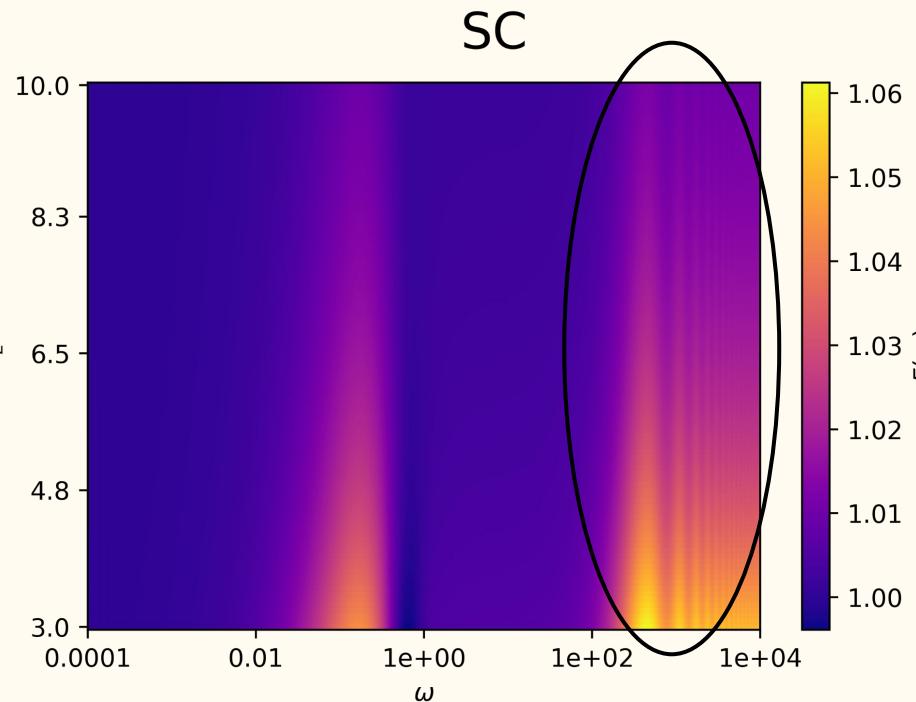
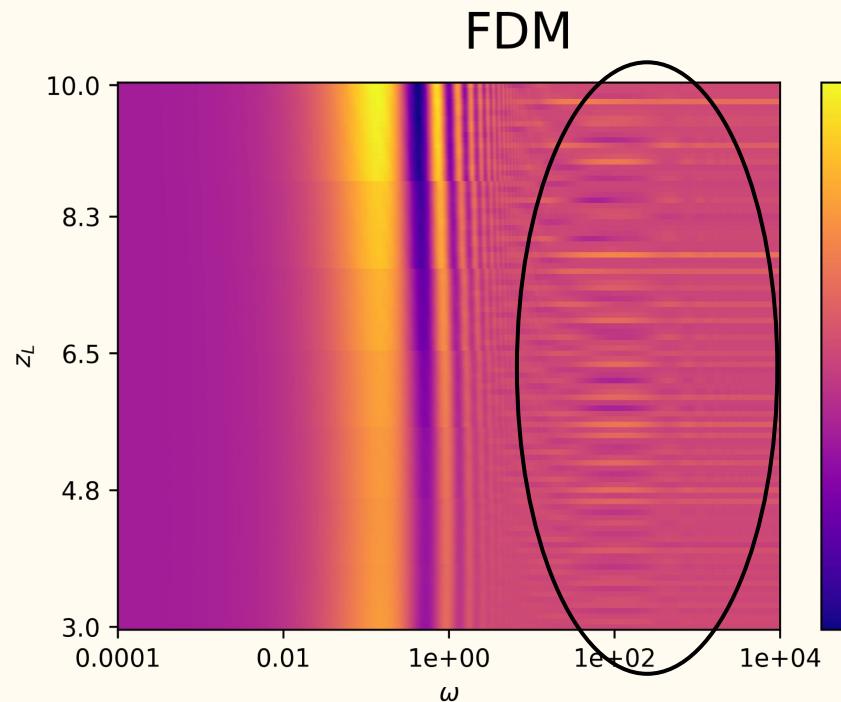
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**SC**

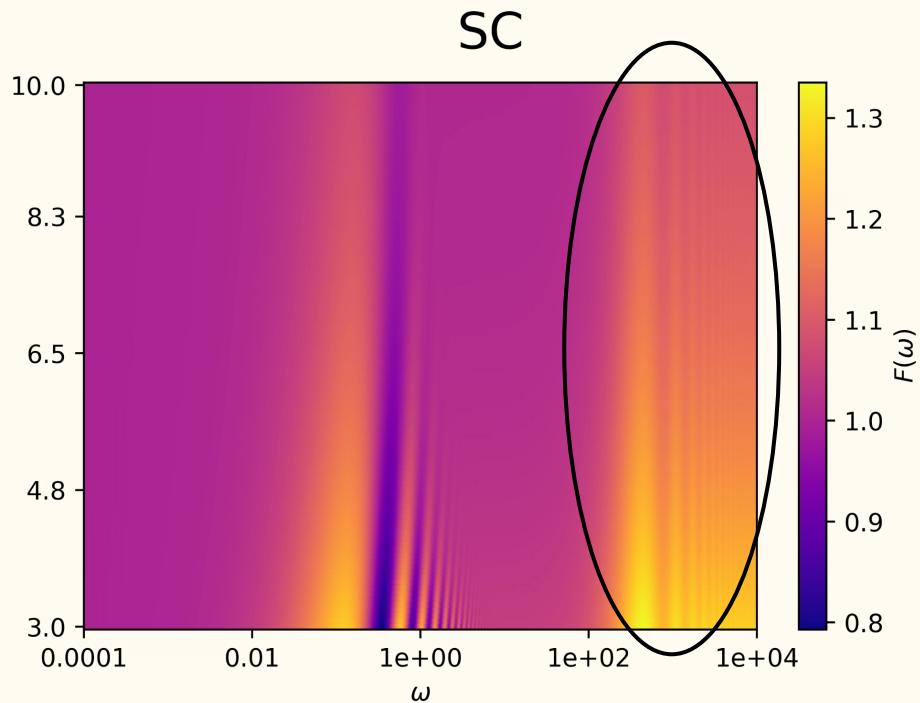
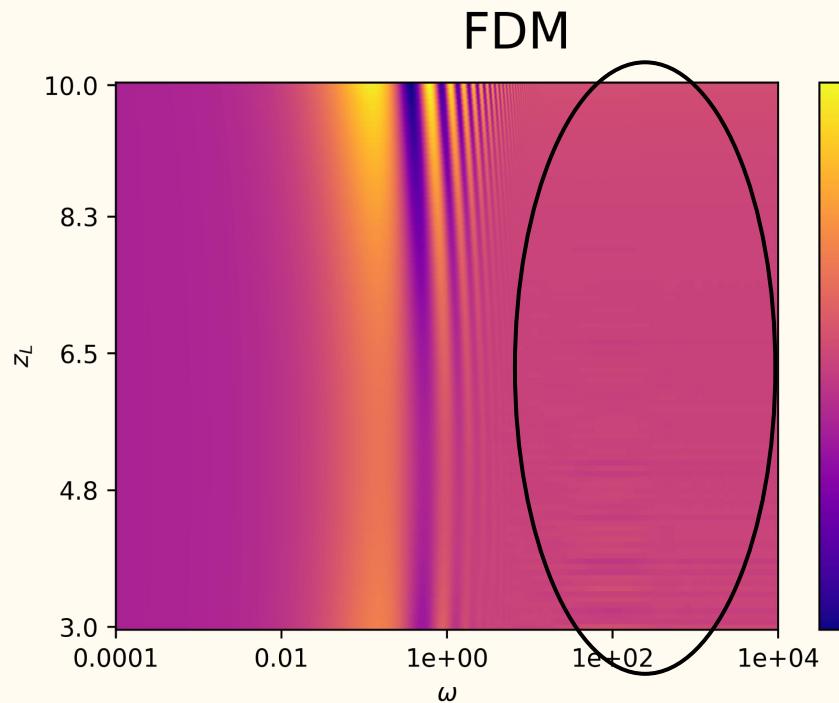


# Lensing Features



$$M_L = 10^8 M_\odot$$

# Lensing Features



$$M_L = 10^9 M_\odot$$

# Lensing Features

$$\omega \equiv 8\pi G M_{Lz} f \sim \left( \frac{M_{Lz}}{10^4 M_\odot} \right) \left( \frac{f}{Hz} \right)$$

$$M_L = 10^8 M_\odot$$

$$M_L = 10^9 M_\odot$$

# Lensing Features

$$\omega \equiv 8\pi G M_{Lz} f \sim \left( \frac{M_{Lz}}{10^4 M_\odot} \right) \left( \frac{f}{Hz} \right)$$

$$M_L = 10^8 M_\odot \quad \xrightarrow{\text{dashed arrow}} \quad \boxed{\omega \sim 10^{3-4}}$$

$$M_L = 10^9 M_\odot$$

# Lensing Features

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$$M_L = 10^8 M_\odot$$

$$M_L = 10^9 M_\odot$$

$$\boxed{\omega \sim 10^{3-4}}$$

$$f \sim 0.1 - 1 Hz$$

$$f \sim 0.01 - 0.1 Hz$$

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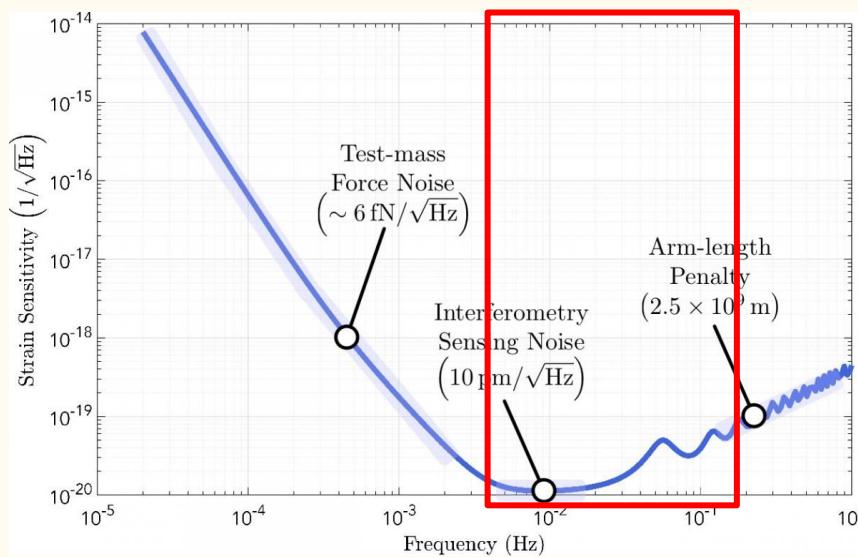
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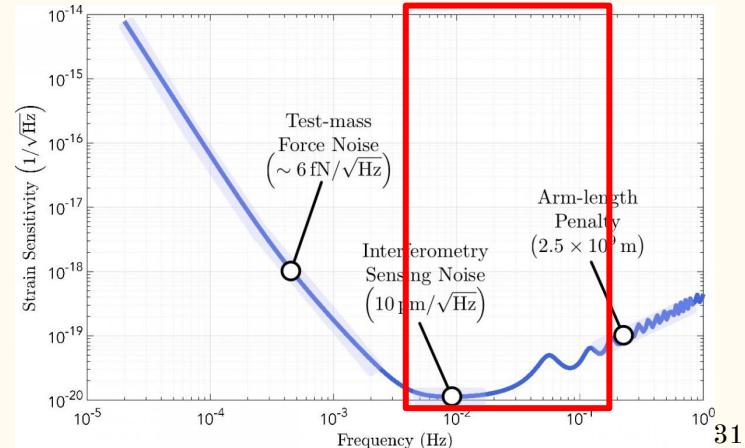
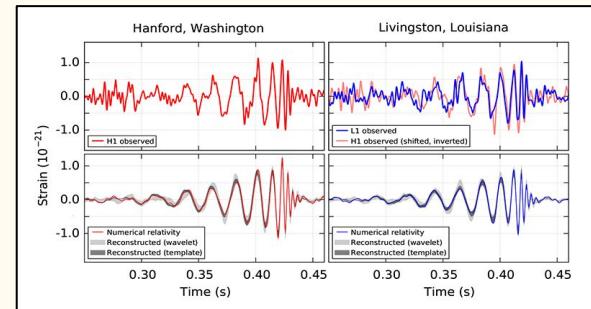
$$f \sim 0.01 - 0.1 Hz$$



LISA sensitivity :  
0.1 mHz to 1 Hz

# Conclusion

- GWs complement EM lensing
  - ◆ ability to probe lens features
- Fast and accurate method to evaluate lensing features\*
- Features of FDM detectable
  - ◆ within the sensitivity of LISA
- Next steps
  - ◆ interference pattern
  - ◆ probing lens parameters<sup>†</sup>



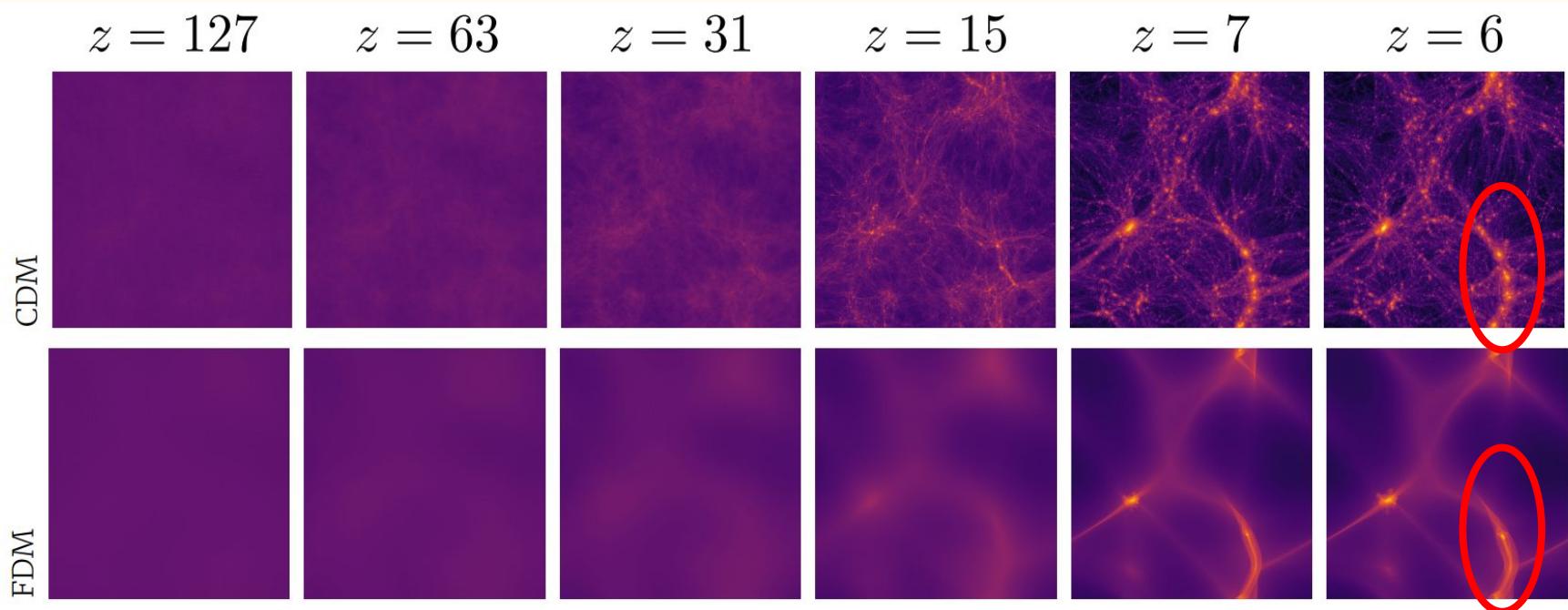
\* <https://arxiv.org/abs/2306.05282>

† <https://arxiv.org/abs/2212.11960>

**Thanks !!**

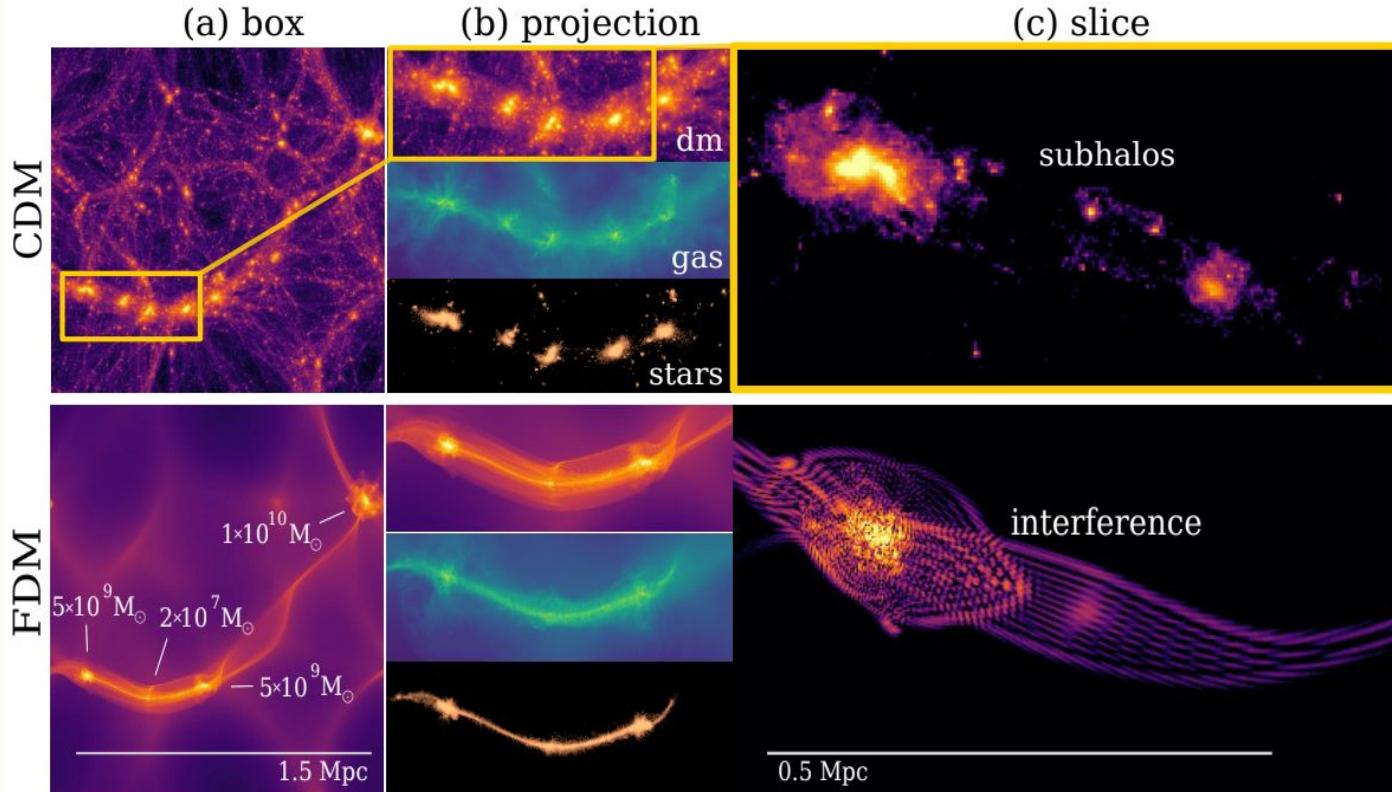
# Extra Slides ..

# A view of fuzzy Universe

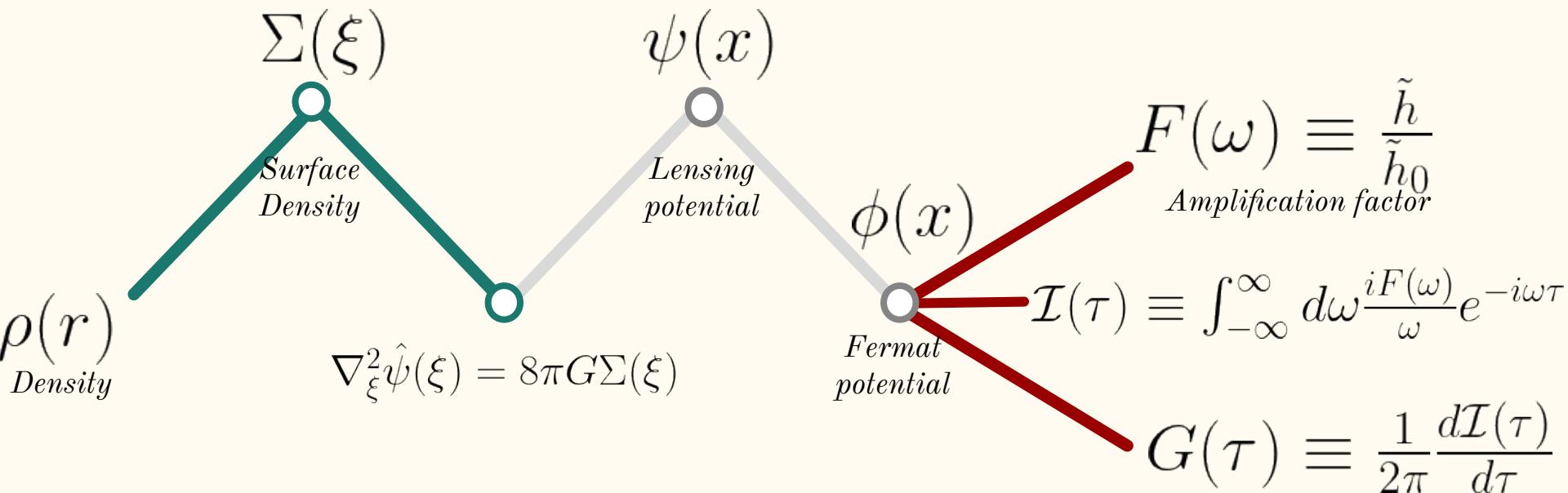


Pmocz, A. (2019). Fuzzy dark matter: overview. Retrieved from [https://indico.neic.no/event/101/contributions/366/attachments/154/245/pmocz\\_2019\\_09\\_30\\_reykjavic.pdf](https://indico.neic.no/event/101/contributions/366/attachments/154/245/pmocz_2019_09_30_reykjavic.pdf)

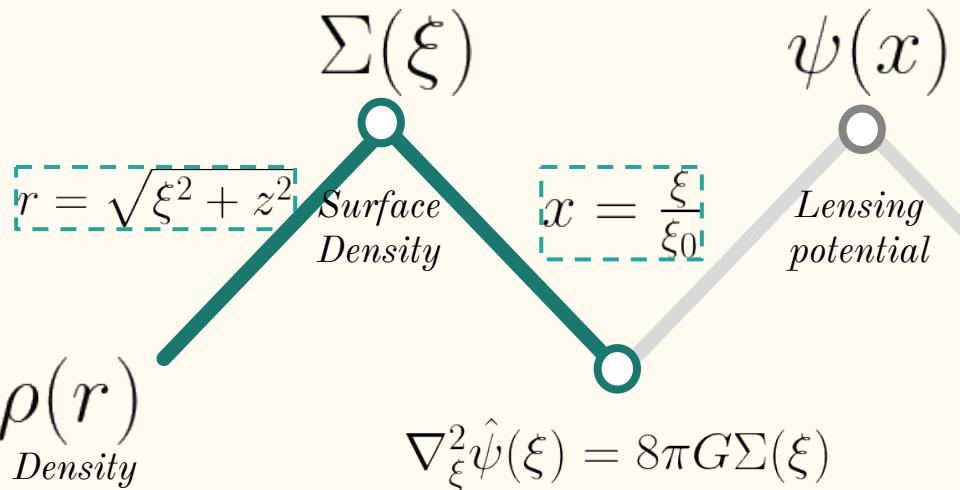
# A view of fuzzy Universe



# Gravitational Wave Lensing – Theory



# Gravitational Wave Lensing – Theory



The diagram shows a triangle with vertices at  $\phi(x)$  (top),  $\mathcal{I}(\tau)$  (bottom-left), and  $G(\tau) \equiv \frac{1}{2\pi} \frac{d\mathcal{I}(\tau)}{d\tau}$  (bottom-right). A red line connects  $\phi(x)$  to  $\mathcal{I}(\tau)$ . The text "Fermat potential" is written below the triangle.

$$\omega \equiv 8\pi GM_{Lz}f$$
$$F(\omega) \equiv \frac{h}{\tilde{h}_0}$$

*Amplification factor*

$$\mathcal{I}(\tau) \equiv \int_{-\infty}^{\infty} d\omega \frac{iF(\omega)}{\omega} e^{-i\omega\tau}$$
$$G(\tau) \equiv \frac{1}{2\pi} \frac{d\mathcal{I}(\tau)}{d\tau}$$

$$M_{Lz} \equiv \frac{\xi_0^2}{4Gd_{\text{eff}}}$$