

# JOINT RECONSTRUCTIONS OF GROWTH AND EXPANSION HISTORIES FROM STAGE-IV SURVEYS

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Rodrigo CALDERÓN

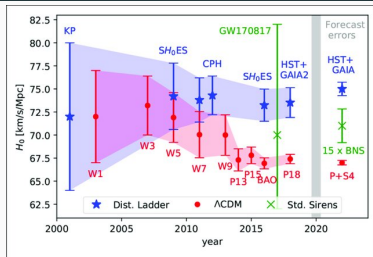
July 2023 - Cosmology From Home

Postdoc at the Korea Astronomy and Space Science Institute (KASI)

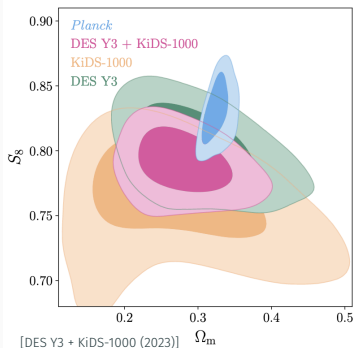
Based on: *Phys. Rev. D* (2022) 8, 083513 and 2301.00640 (To appear in PRD)

In Collab. with: B. L'Huillier, D. Polarski, A. Shafieloo, A. A. Starobinsky

# THE CONCORDANCE MODEL AND ITS LIMITATIONS



[Ezquiaga & Zumalacárregui (2018)]



[DES Y3 + KiDS-1000 (2023)]  $\Omega_m$

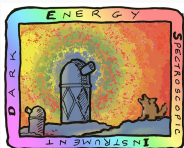
## Shortcomings:

- Smallness of  $\Lambda$  ( $> 0$ )
- Dark Matter: Cold/Warm, (Self) Interacting, PBH
- $H_0/S_8$ -tensions
- Small-scale Issues: Core-Cusp, Satellite

## Solutions:

- Systematics?
- New Physics?
- Both?

“Model-independent” approach



## DARK ENERGY SPECTROSCOPIC INSTRUMENT

U.S. Department of Energy Office of Science



Figure: Dark Energy Spectroscopic Instrument (DESI)

- Large-Scale Structure survey @ Mayall (4m) Telescope (Kitt-Peak, Arizona)
- Observe  $\sim 30$  M galaxies (obtain accurate redshift estimates)
- Accurate distance estimations!
- Probe the last  $\sim 11$  M years of the growth of structure and expansion history (DM  $\rightarrow$  DE domination)

# METHOD: GAUSSIAN PROCESS

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Sampling directly in the space of (continuous) functions!

$$y(x) \sim \mathcal{GP}(\mu = 0, k(\sigma_f = 0.5, \ell_f = 0.3))$$

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# METHOD: ANALYSIS

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## GOAL: RECONSTRUCT DE WITH MINIMAL ASSUMPTIONS

- (Flat) FLRW metric + Matter Dominated (EdS) Universe at high- $z$ .

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  - Redshift-Space Distortions (**RSD**) - DESI (14K deg<sup>2</sup>) survey :

$$f\sigma_8(z) \equiv f(z) \delta(z) \frac{\sigma_{8,0}}{\delta(z=0)} , \quad \sigma_{8,0}^{\text{fid}} = 0.81.$$

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- Jointly reconstruct Growth and Expansion histories

$$\ddot{\delta} + 2H\dot{\delta} = 4\pi G_{\text{eff}}(z) \rho \delta$$



## OUR APPROACH: FORWARD MODELING

$$\text{Model } f_{\text{DE}} \equiv \frac{\rho_{\text{DE}}(z)}{\rho_{\text{DE},0}} \sim \mathcal{GP}(\mu = 1, K(\sigma_f, \ell_f))$$

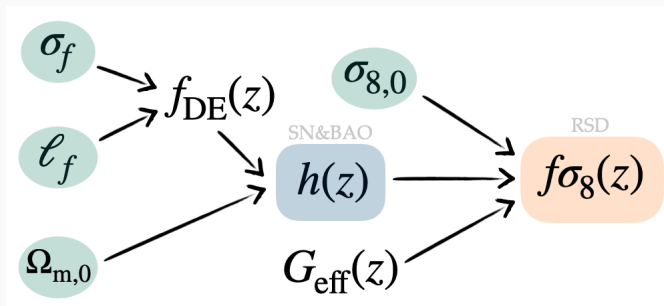


Figure: Schematic representation of our reconstruction method

→ Sample  $\theta = \{\Omega_m, \sigma_8, \sigma_f, \ell_f\}$  using MCMC methods!

$$\chi_{\text{tot}}^2 = \chi_{\text{SN}}^2 + \chi_{\text{BAO}}^2 + \chi_{\text{RSD}}^2$$

RESULTS: GR

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$$h^2(z) = \Omega_{m,0}(1+z)^3 + (1 - \Omega_{m,0}) \cdot f_{DE}(z)$$

$$f_{DE} \sim \mathcal{GP}(\mu = 1, K(\sigma_f, \ell_f))$$

Minimal Assumptions:

- $f_{DE} \equiv$  DE+any additional (exotic) component!
- (Flat) FLRW + EdS  
(+ GR)

→ With given  $h(z)$ , can solve for the growth-rate  $f\sigma_8$  :

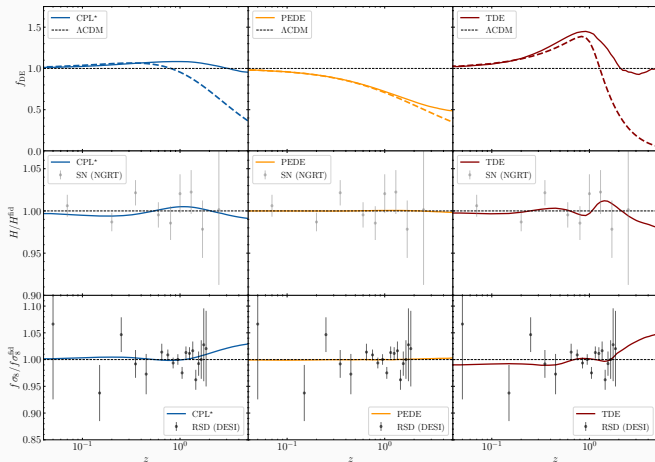
$$f' + \left( f + 2 + \frac{h'}{h} \right) f - \frac{3}{2} \Omega_m = 0$$

$$f \equiv \delta' / \delta, \quad \prime \equiv \frac{d}{d \ln a}$$

**Figure:** Samples of  $f_{DE}$  and their likelihood to DESI+Roman-like (mock) data

# RECONSTRUCTING FIDUCIAL COSMOLOGIES

Calderón, L'Huilier, Polarski, Shafieloo, Starobinsky '22 - Phys.Rev.D 106 (8), 083513



**Figure:** Reconstruction of *3 different* fiducial DE models (at 95% CL) using SN+BAO+RSD forecasted (Stage-IV) data

# BEYOND GENERAL RELATIVITY

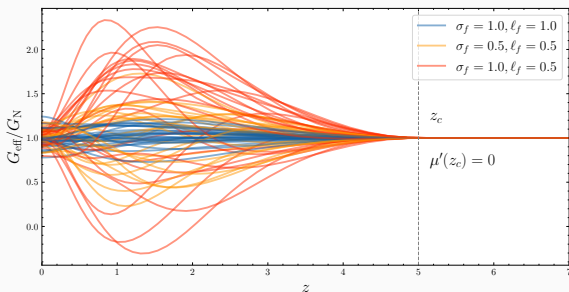
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$$-\frac{k^2}{a^2}\Phi = 4\pi G_{\text{eff}}(z, k)\delta\rho_m$$

We model  $G_{\text{eff}}(z)$  as a GP centered around Newton's constant  $G$ , such that  $\mu(z) \equiv G_{\text{eff}}/G$

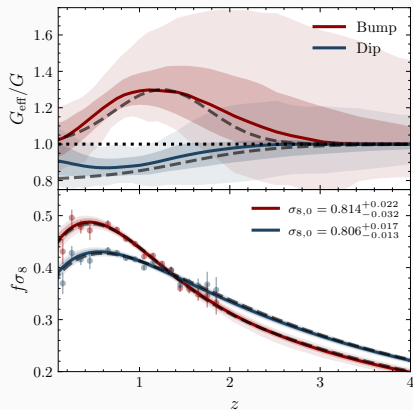
$$\mu(z; \sigma_f, \ell_f, z_c) = \begin{cases} \mathcal{GP}(\bar{f} = 1, k(\sigma_f, \ell_f)), & \text{for } z < z_c \\ 1, & \text{for } z \geq z_c. \end{cases} \quad (1)$$

with  $\mu'(z_c) = 0$ , so that we (smoothly) recover GR at large- $z$ .



# RECONSTRUCTING $\mu(z)$

Calderón, L'Huillier, Polarski, Shafieloo, Starobinsky '23 - 2301.00640



**Figure:** Reconstructions of  $\mu \equiv G_{\text{eff}}/G$  from RSD mocks, assuming  $h(z)$  as determined by the SN+BAO chains.

We use the reconstructed expansion history  $h(z)$  from the SN+BAO chains

$$f' + \left( f + 2 + \frac{h'}{h} \right) f = \frac{3}{2} \Omega_m \mu(z).$$

→ Sample  $\theta = \{\sigma_8; \sigma_f, \ell_f, z_c\}$ !

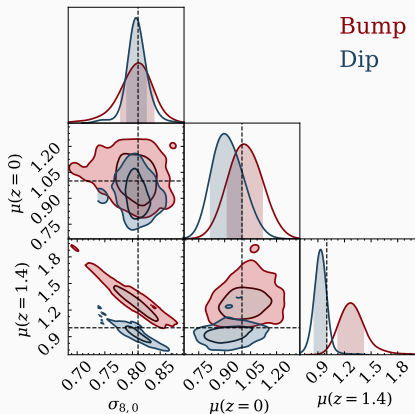
$$\sigma_{8,0}^{\text{fid}} = 0.81$$

Two profiles, purely phenomenological “Toy-models”

Can represent a large class of models!

# RECONSTRUCTING $\mu(z)$

Calderón, L'Huillier, Polarski, Shafieloo, Starobinsky '23 - 2301.00640



**Bump**  
**Dip**

We use the reconstructed expansion history  $h(z)$  from the SN+BAO chains

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→ Sample  $\theta = \{\sigma_8; \sigma_f, \ell_f, z_c\}$ !

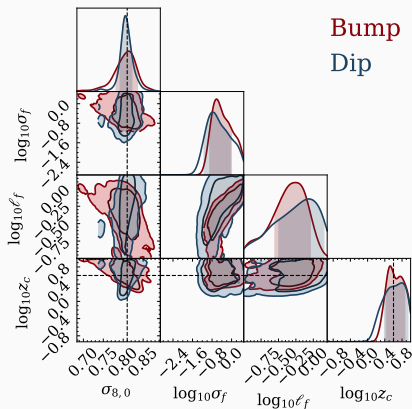
- **Unbiased** estimation of  $\sigma_{8,0}$ !
- At  $z = 1.4$ , DESI could distinguish the bump (in Red) from GR at  $\gg 2\sigma$ !

**Figure:** Reconstructions of  $\mu \equiv G_{\text{eff}}/G$  at two redshifts  $z = 0, 1.4$ , assuming  $h(z)$  as determined by the SN+BAO chains.



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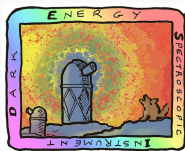
The posteriors of the hyperparameters indicate the underlying theory of gravity is **not consistent** with GR ( $\sigma_f \neq 0$ )!

**Figure:** Constraints on cosmo+hyper parameters from RSD mocks, assuming  $h(z)$  as determined by the SN+BAO chains.

# CONCLUSION

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- “Model-independent” approach to **jointly** reconstruct both **Growth** & **Expansion** Histories with **minimal** assumptions
  - (Flat) FLRW + EdS
- **Accurately** reconstruct the Dark Energy evolution  $f_{\text{DE}}(z)$  &  $G_{\text{eff}}(z)$
- **Unbiased** estimation of cosmological parameters:  $\Omega_m, \sigma_8$
- Assuming  $\Lambda$ CDM can **severely bias** our **interpretation** of the results
- DESI+Roman-like can potentially **detect deviations** from  $\Lambda$ +GR
  - Euclid, Rubin (LSST), CMB-S4, + many more...



## DARK ENERGY SPECTROSCOPIC INSTRUMENT

U.S. Department of Energy Office of Science

DESI is currently gathering data !  
(already has more than all previous galaxy surveys **combined**)

→ Stay tuned!

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Thank you for your attention