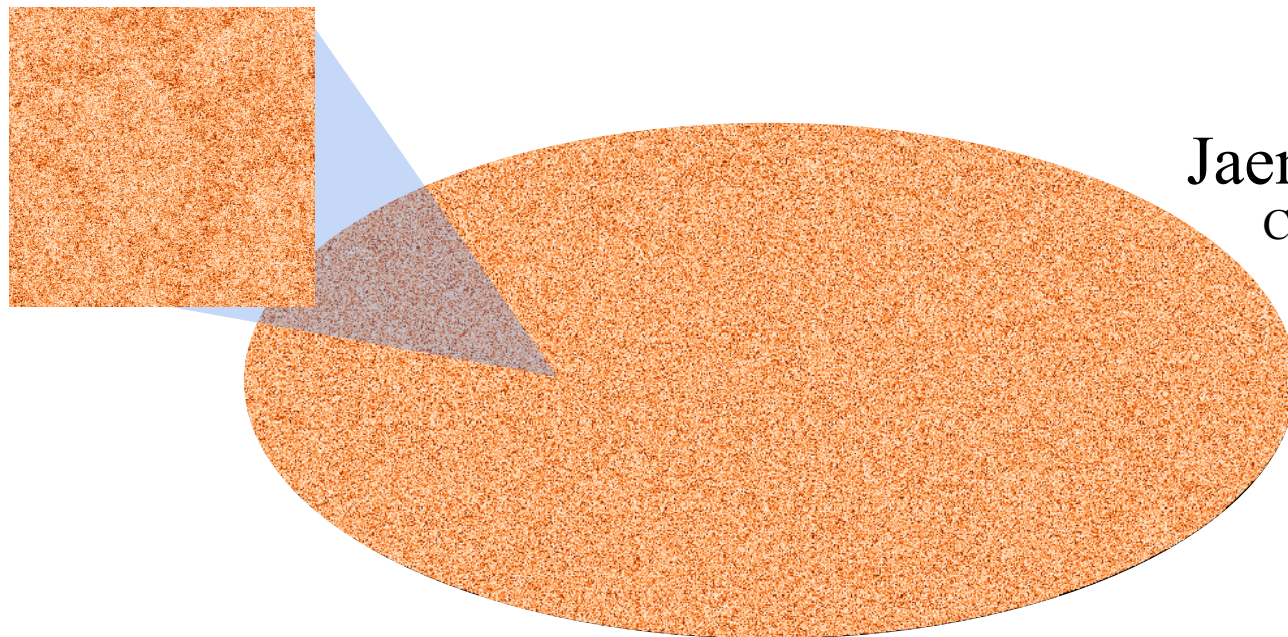


Exploring the Non-Gaussianity of the CIB & Its Gravitational Lensing



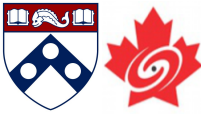
Open in Keynote for animations!



Jaemyoung (Jason) Lee
Cosmology from Home 2023

Collaborators: J. Richard Bond,
Pavel Motloch, Alexander van
Engelen, and George Stein

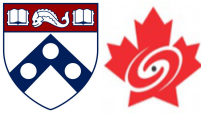
<https://arxiv.org/abs/2304.07283>



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- What is the CIB (Cosmic Infrared Background)?
- Websky Simulations

Introduction



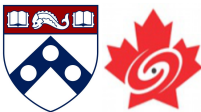
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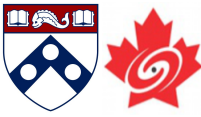
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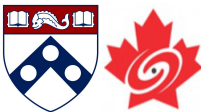
- **Statistics of the Websky CIB maps**
- **Effect of lensing on CIB statistics**
- **Beyond n-point statistics**
- Correlation of the CIB with CMB lensing
- (Galaxy) environmental effects on CIB statistics

Results

- Conclusion & Why we care

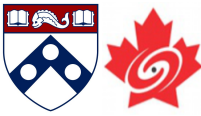


Introduction



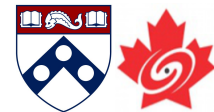
Cosmic Infrared Background (CIB)

- Emission of dust from star forming galaxies: traces galaxy formation, clustering, dark matter
- $z = 0$ to 4, Non-Gaussian (beyond power spectrum)



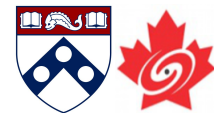
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- CIB 2-point and 3-point measured by *Planck*, SPT (South Pole Telescope), and ACT (Atacama Cosmology Telescope) at 150 GHz ~ 850 GHz
- CMB foreground



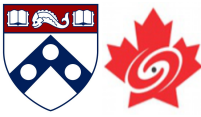
Websky Peak Patch Simulations

- Based on Peak Patch and 2LPT
- Flux of each galaxy calculated according to a CIB halo model - depends only on the mass and redshift of the (sub)halo
- Normalized so that CIB power spectrum at 545 GHz, $\ell = 500$ match *Planck's*



Websky Peak Patch Simulations

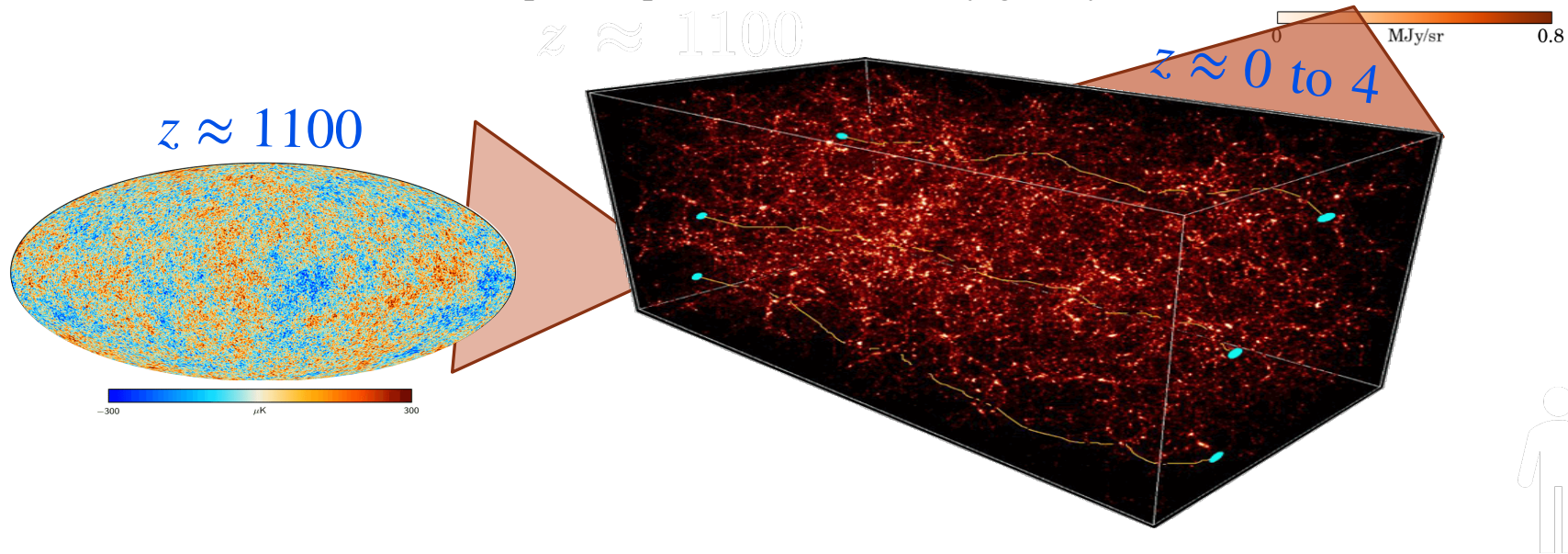
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- Normalized so that CIB power spectrum at 545 GHz, $\ell = 500$ match *Planck's*
- Lensing convergence (κ) maps - integrated over the appropriately weighted density field along line of sight
- Stein et al. (2020) - <https://iopscience.iop.org/article/10.1088/1475-7516/2020/10/012/pdf> , https://mocks.cita.utoronto.ca/index.php/WebSky_Extragalactic_CMB_Mocks for more info



Methodology

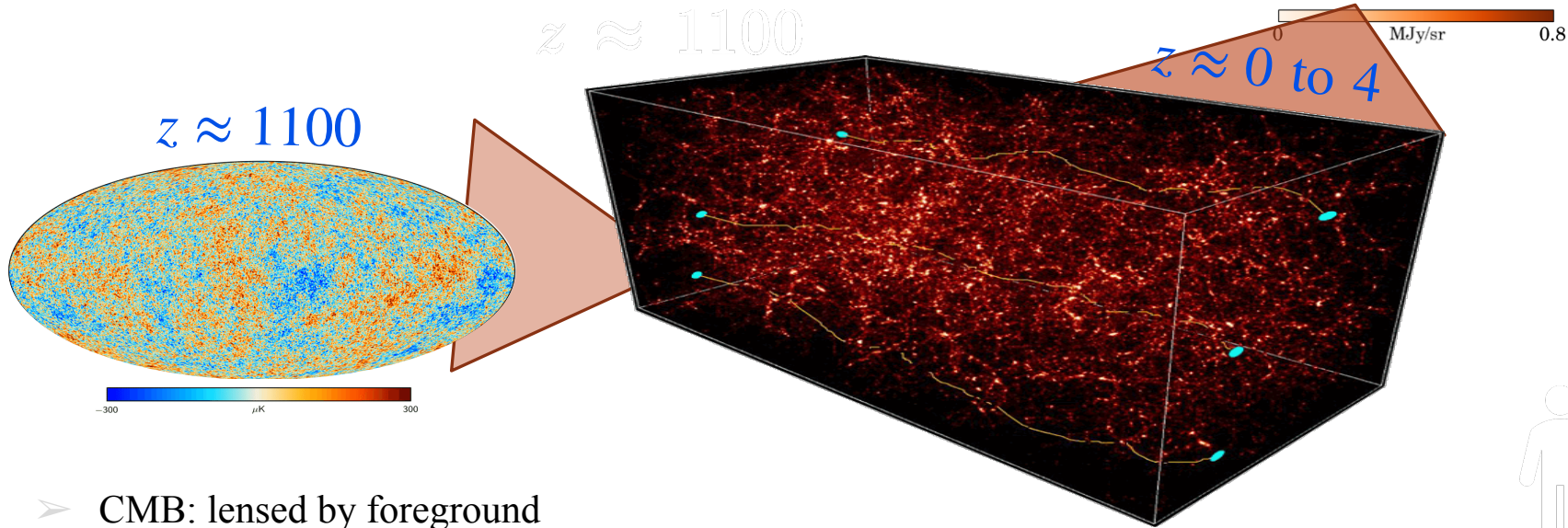
Lensing of the CIB

- Observed CIB distorted as photon paths are deflected by gravity

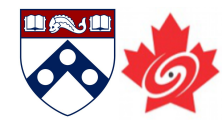


Lensing of the CIB

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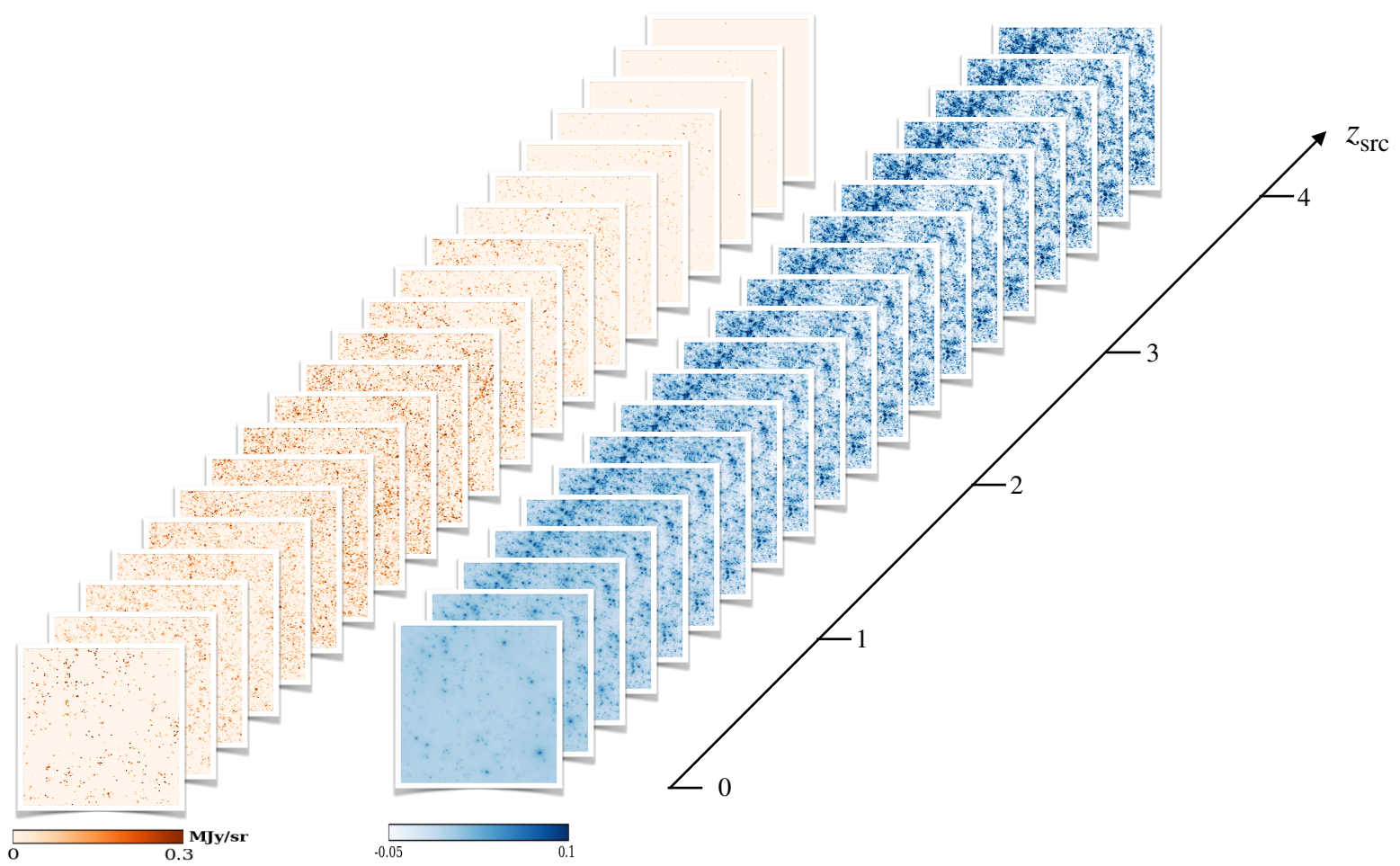


- CMB: lensed by foreground
- CIB: lensed by sources contributing to the CIB (self-lensing)
- Complicates CIB lensing analysis \Rightarrow motivation for simulation studies



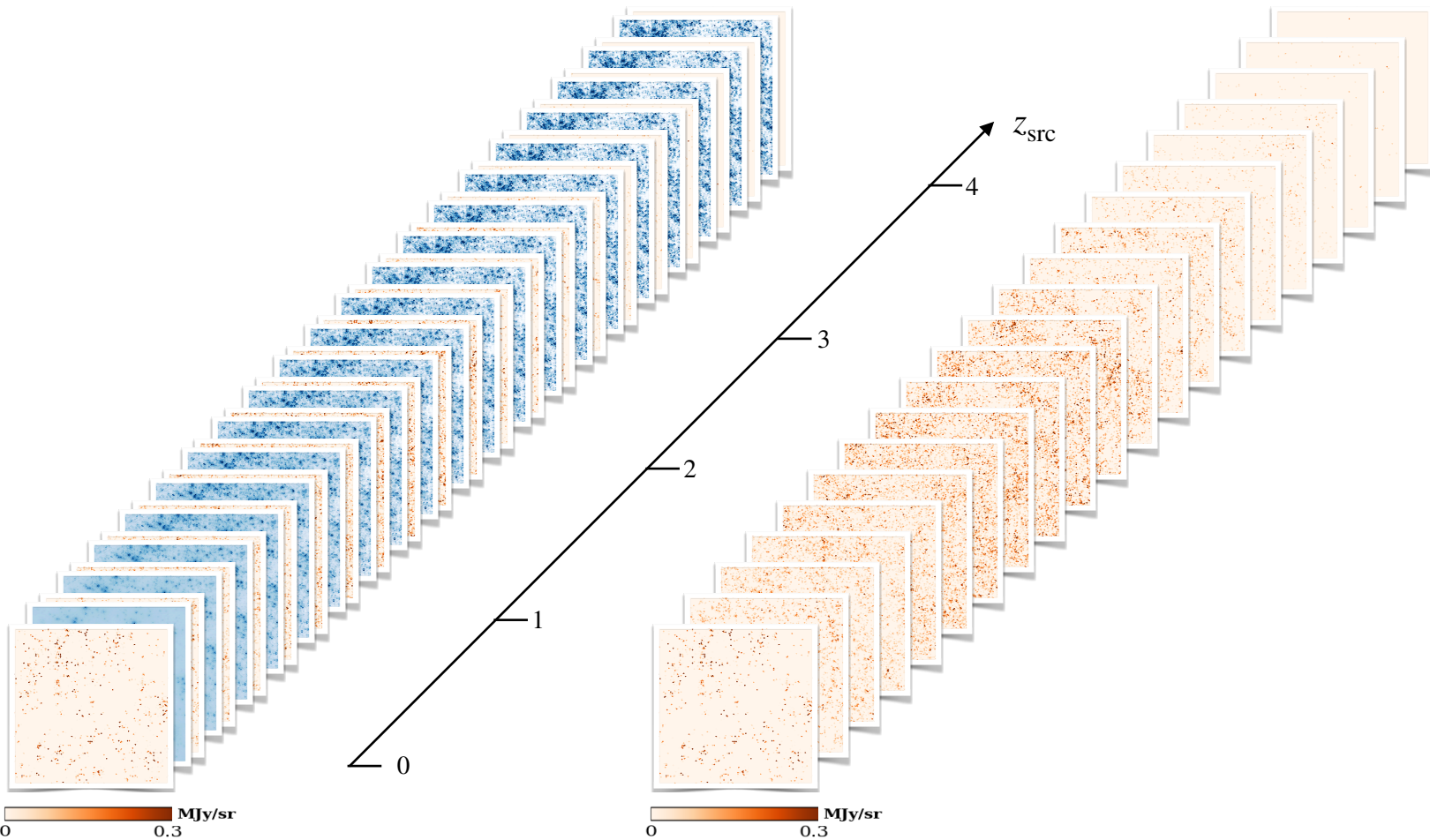
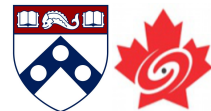
CIB Flux $I_{545\text{ GHz}}$

Lensing Convergence κ



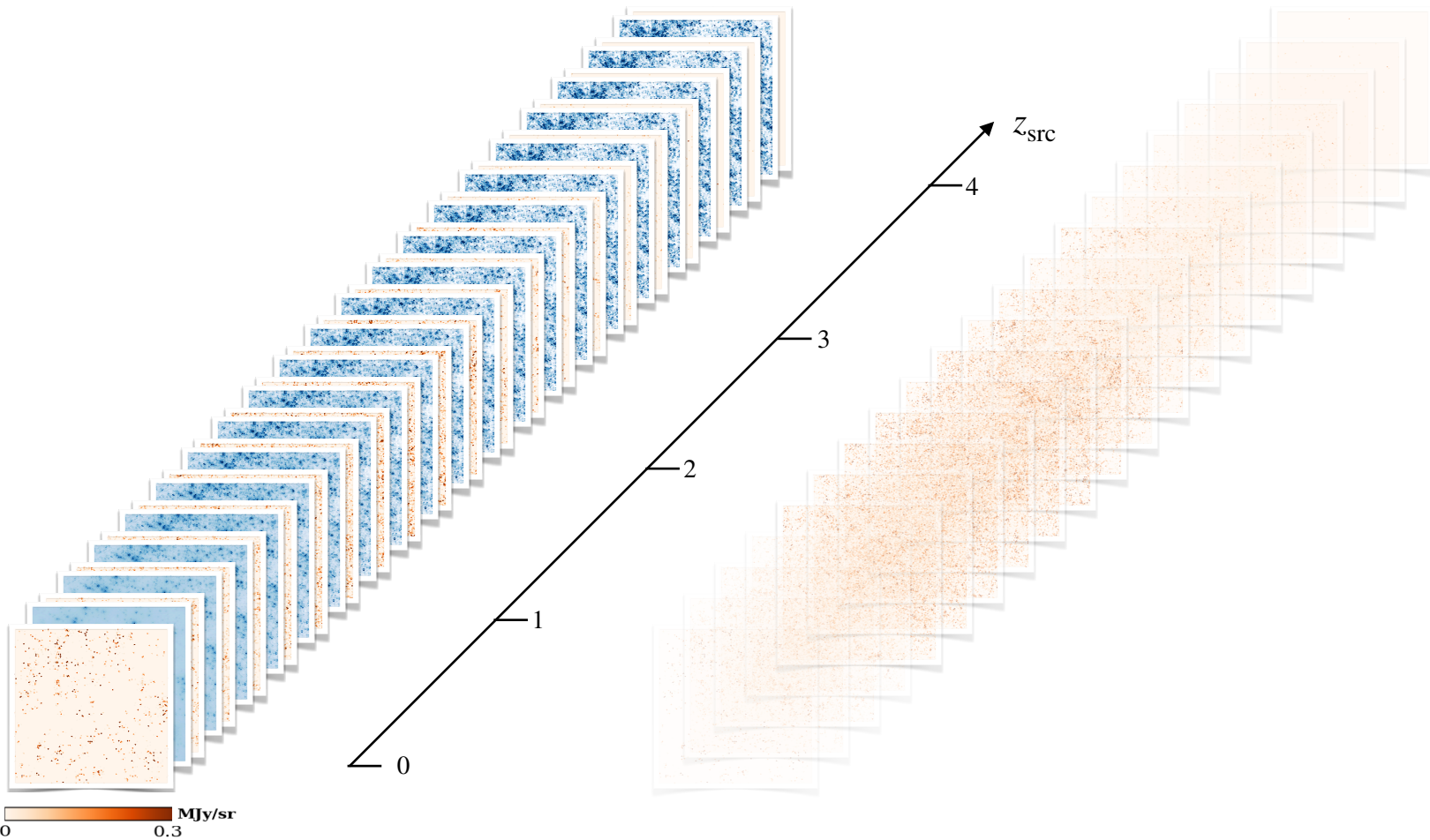
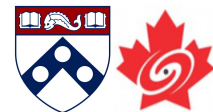
CIB Flux $I_{545\text{GHz}}$ + Lensing Convergence κ

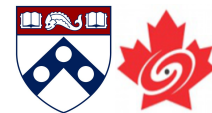
Lensed CIB $I_{545\text{GHz}}$



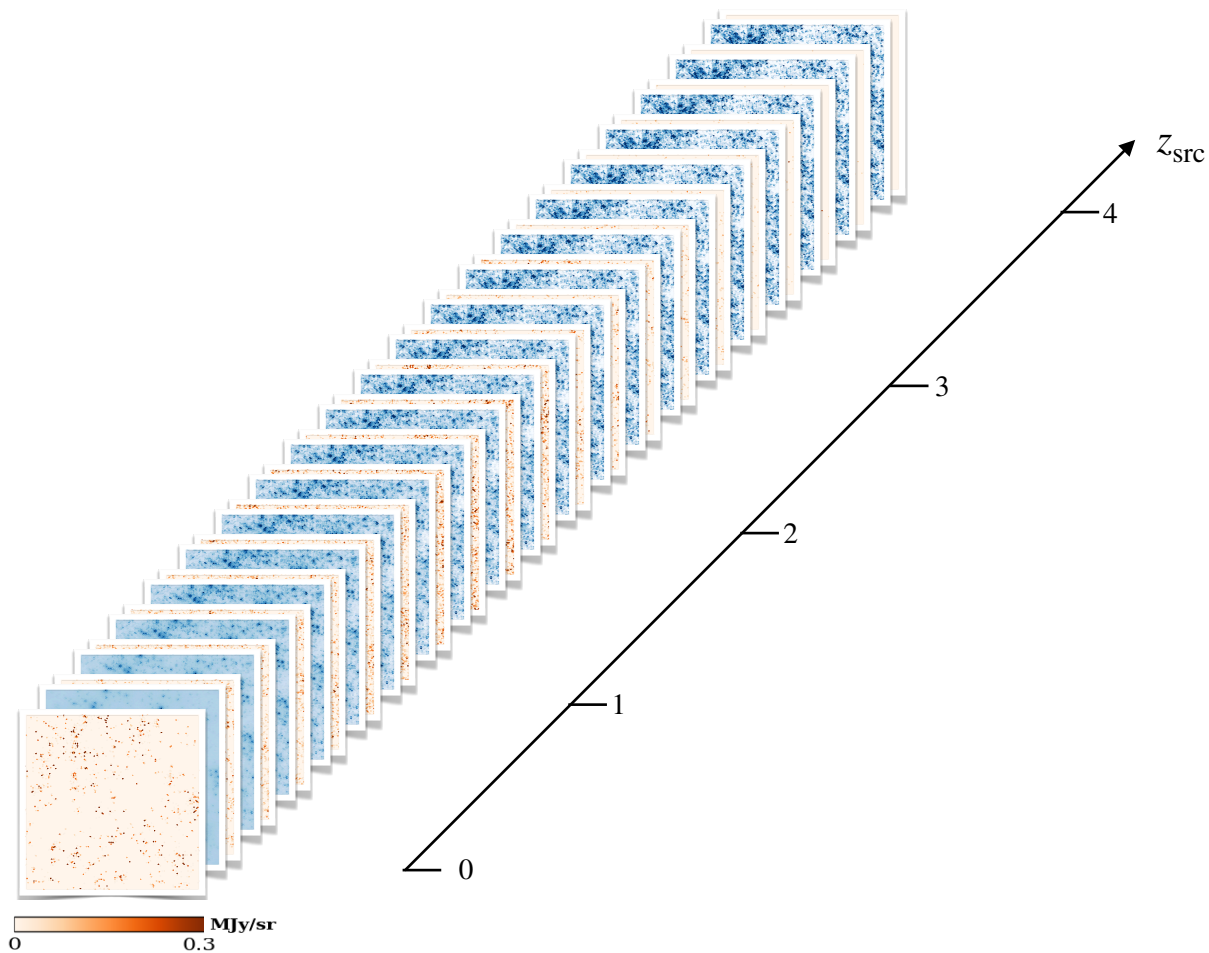
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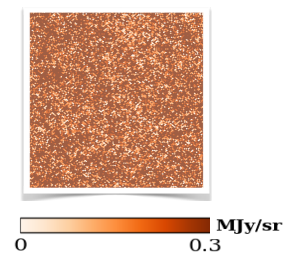


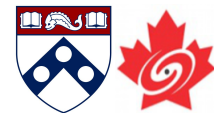


CIB Flux $I_{545\text{GHz}}$ + Lensing Convergence κ



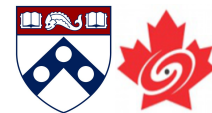
Total Lensed CIB $I_{545\text{GHz}}$





How we lens the CIB: Deflection-magnification method

- Smooth κ maps with a beam of $(\sqrt{3}N_{\text{SIDE}})^{-1}$
(pixel-size) to mitigate strong-lensing
- Galaxies deflected by an amount given by $\nabla\phi_{z_i}$
(Lewis 2005)

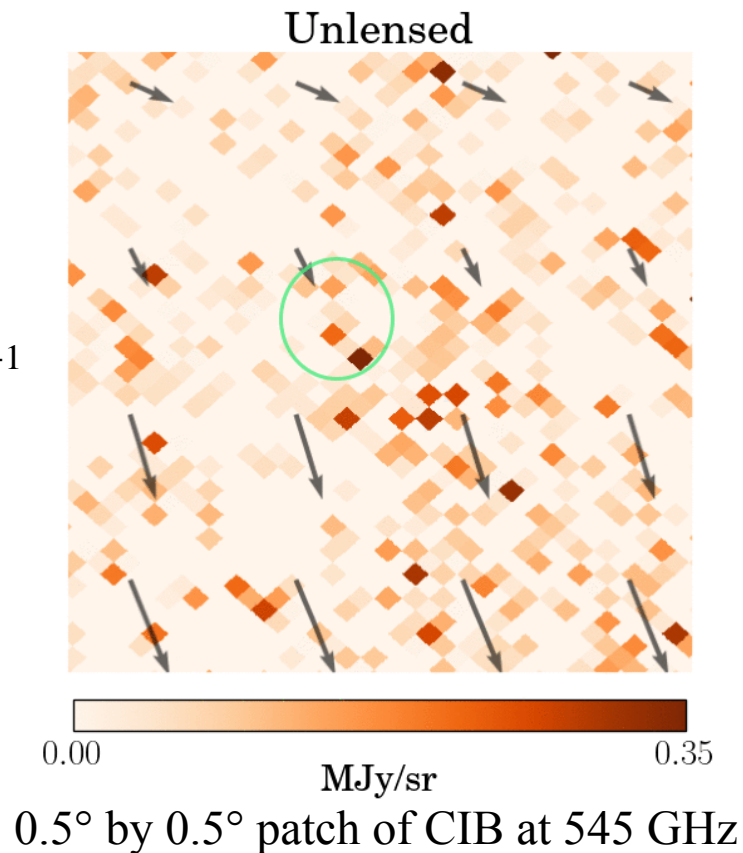


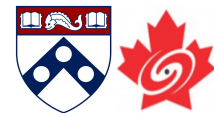
How we lens the CIB: Deflection-magnification method $\approx 1.0 \sim 1.2$

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- Galaxies then magnified by $\mu = [(1 - \kappa)^2 - \gamma^2]^{-1}$ rather than $(1 + 2\kappa)$
 - 3% difference at $\kappa = 0.1$
 - 30% difference at $\kappa = 0.3$

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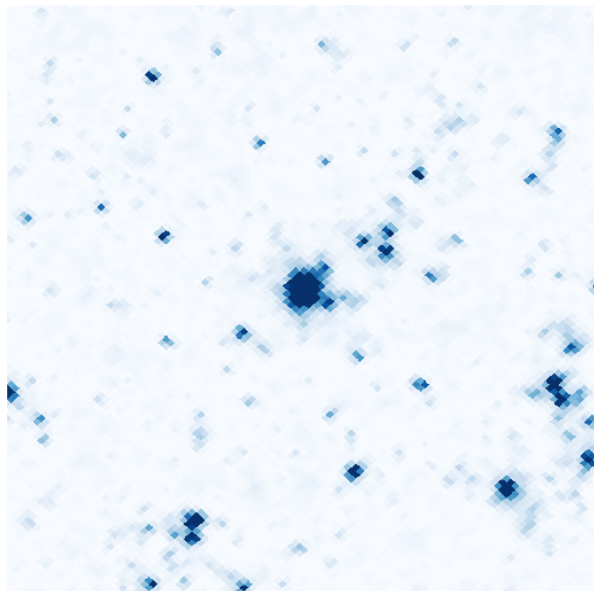




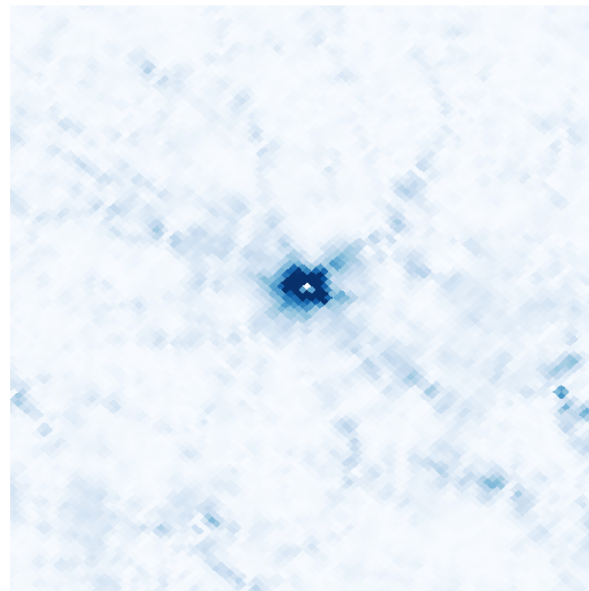
Lensing convergence and shear

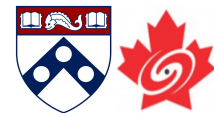
$$z = 1.0 \sim 1.2$$

$$\kappa^2$$

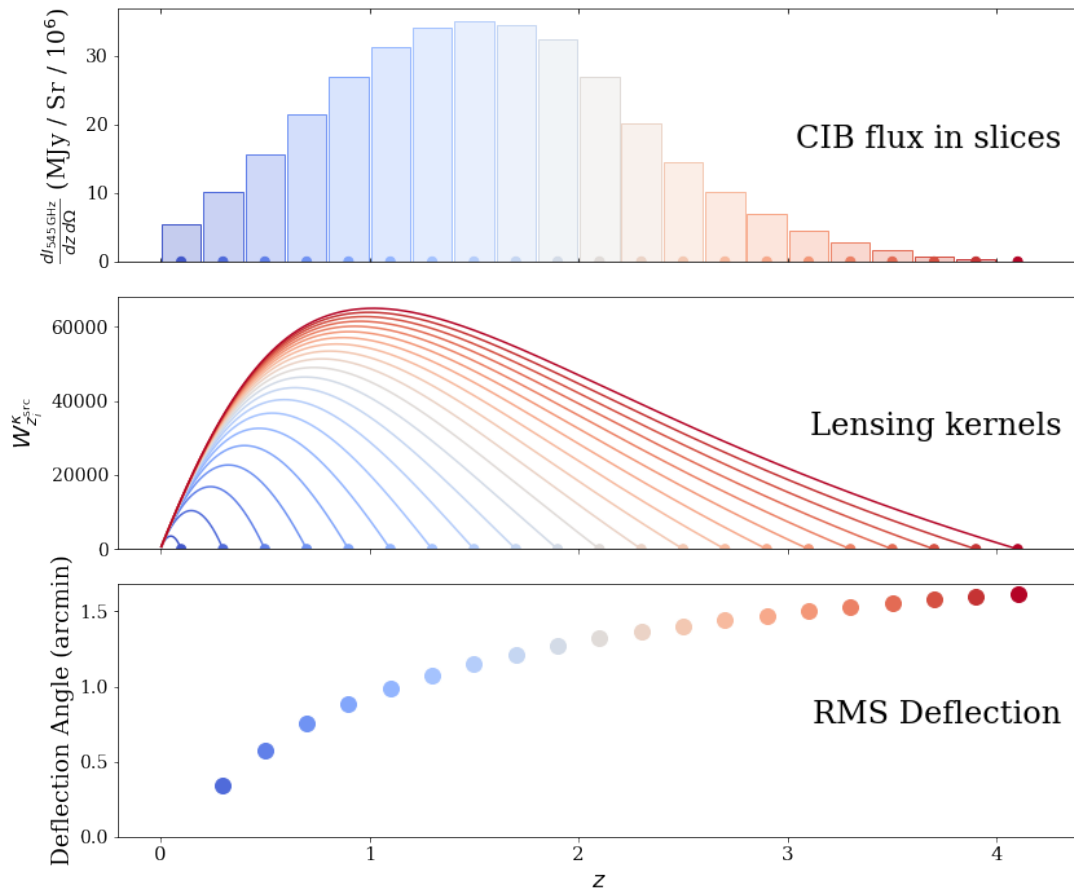


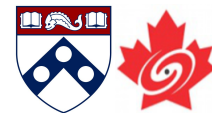
$$\gamma^2 = \gamma_1^2 + \gamma_2^2$$





Websky CIB





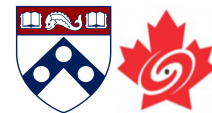
Filtered Statistics

➤ Variance: $S_2^{\ell_c} = \langle (\Delta T^{\ell_c}(x))^2 \rangle$ $F_\ell = \frac{C_{\ell_c}}{C_\ell}$

➤ Skewness: $S_3^{\ell_c} = \langle (\Delta T^{\ell_c}(x))^3 \rangle$

➤ Kurtosis: $S_4^{\ell_c} = \langle (\Delta T^{\ell_c}(x))^4 \rangle - 3 (S_2^{\ell_c})^2$

➤ ℓ_c : ℓ - band center
 ℓ_c ℓ -



Filtered Statistics

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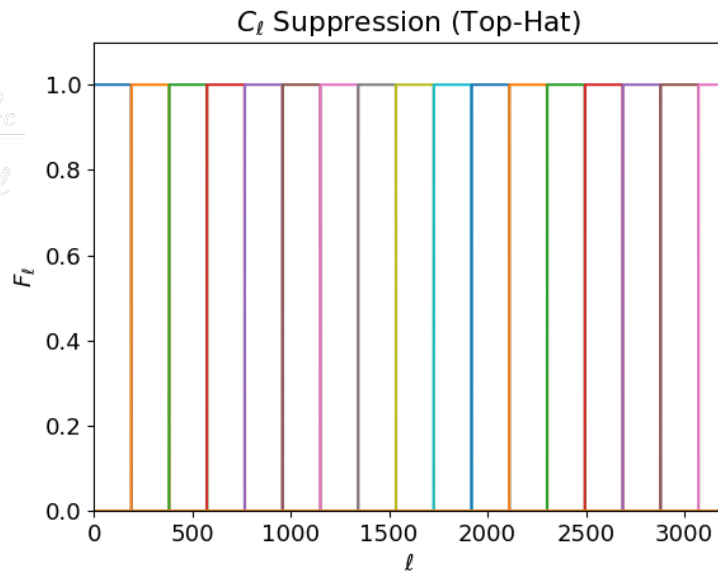
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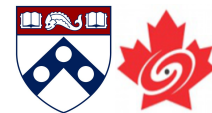
➤ Kurtosis: $S_4^{\ell_c} = \langle (\Delta T^{\ell_c}(x))^4 \rangle - 3 \left(S_2^{\ell_c} \right)^2$

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ℓ_c ℓ -

$$F_\ell = \frac{C_{\ell_c}}{C_\ell}$$





Filtered Statistics to poly-spectra

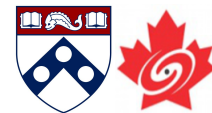
➤ (Roughly) equilateral configuration

$$\text{➤ } C_{\ell_c} \approx S_2^{\ell_c} \left(\sum_{\ell_c - \Delta\ell/2}^{\ell_c + \Delta\ell/2} \frac{2\ell + 1}{4\pi} \right)^{-1}, \quad \because S_2^{\ell_c} = \sum_{\ell_c - \Delta\ell/2}^{\ell_c + \Delta\ell/2} \frac{2\ell + 1}{4\pi} C_\ell$$

$$\text{➤ } b_{\ell_c, \ell_c, \ell_c} \approx 2\sqrt{3}\pi^3 S_3^{\ell_c} (\Delta\ell)^{-3} \ell_c^{-1} \propto S_3^{\ell_c} \ell_c^{-1}$$

$$\text{➤ } t_{\ell_c, \ell_c, \ell_c, \ell_c} \propto S_4^{\ell_c} \ell_c^{-2}$$

$$t_{\ell_c, \ell_c, \ell_c, \ell_c} \propto S_4^{\ell_c} \ell_c^{-2}$$



Filtered Statistics to poly-spectra

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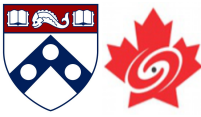
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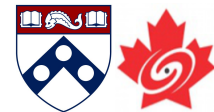
$$t_{\ell_c, \ell_c, \ell_c, \ell_c} \propto S_4^{\ell_c} \ell_c^{-2}$$

➤ Binning: $\Delta\ell = 640$ (default), $\Delta\ell = 128$ (vs. *Planck*)

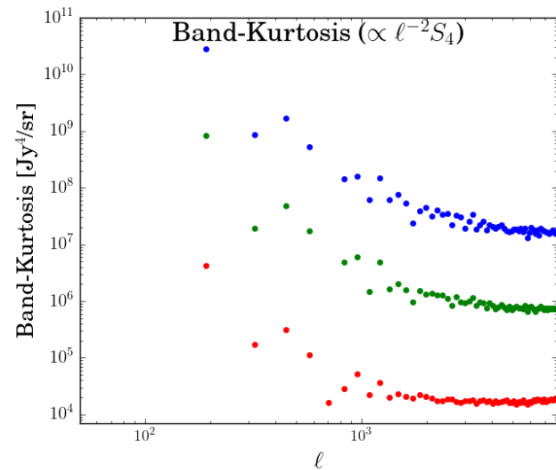
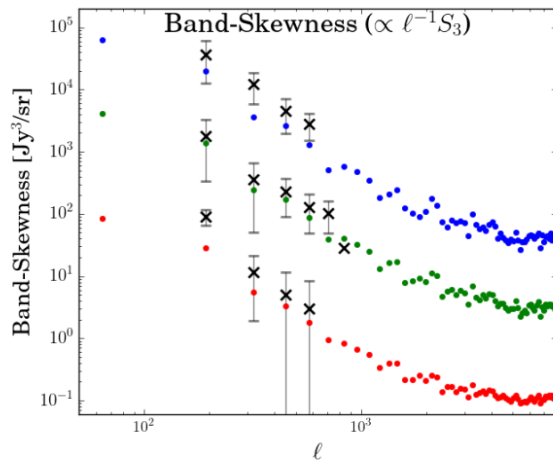
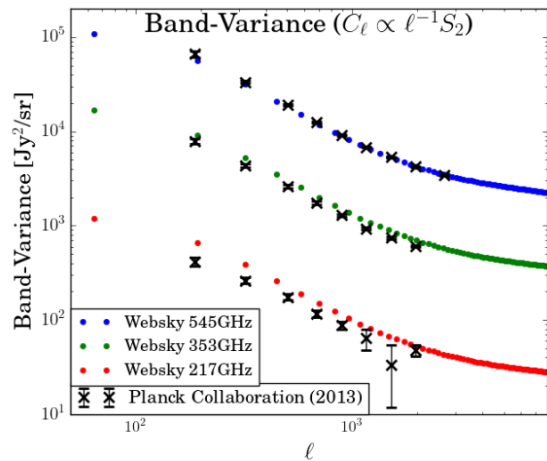
➤ 8 minutes on Niagara cluster for $N_{\text{SIDE}} = 4096$, default binning (about 20 bins)

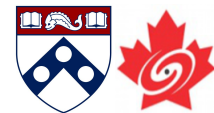


Results

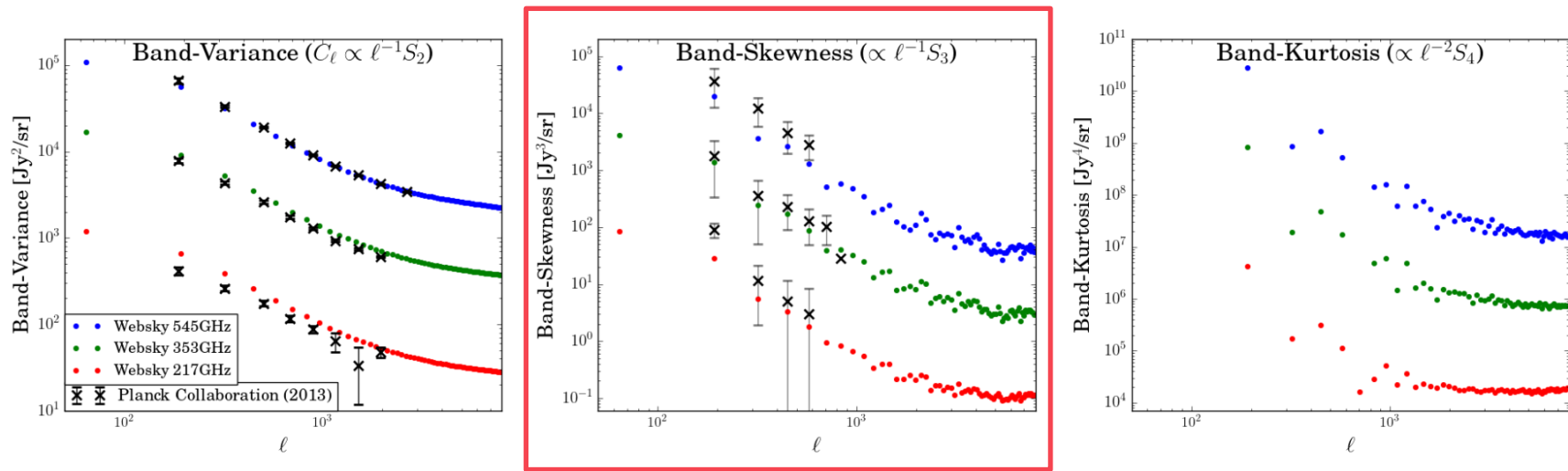


Websky CIB statistics (vs. *Planck*)

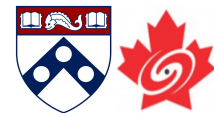




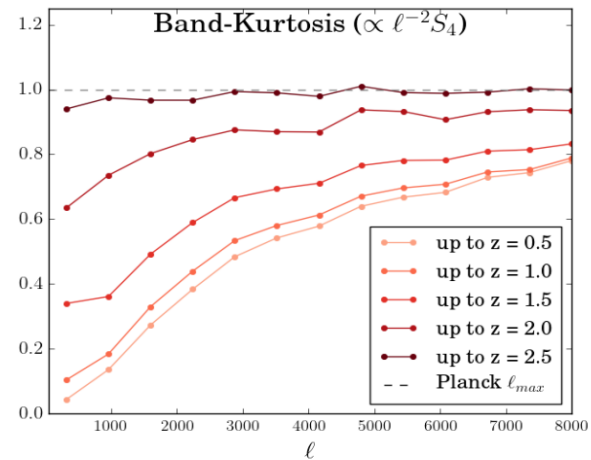
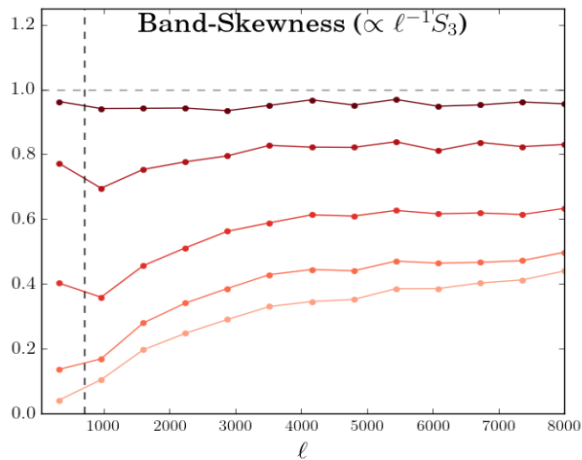
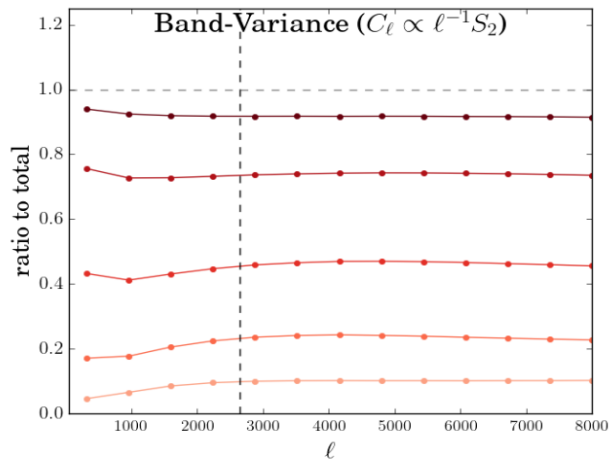
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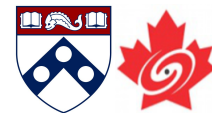


- To exclude very bright, nearby sources, flux cuts applied (same as *Planck* values)
- Websky CIB bispectra are generally within *Planck* error bars => nontrivial!!

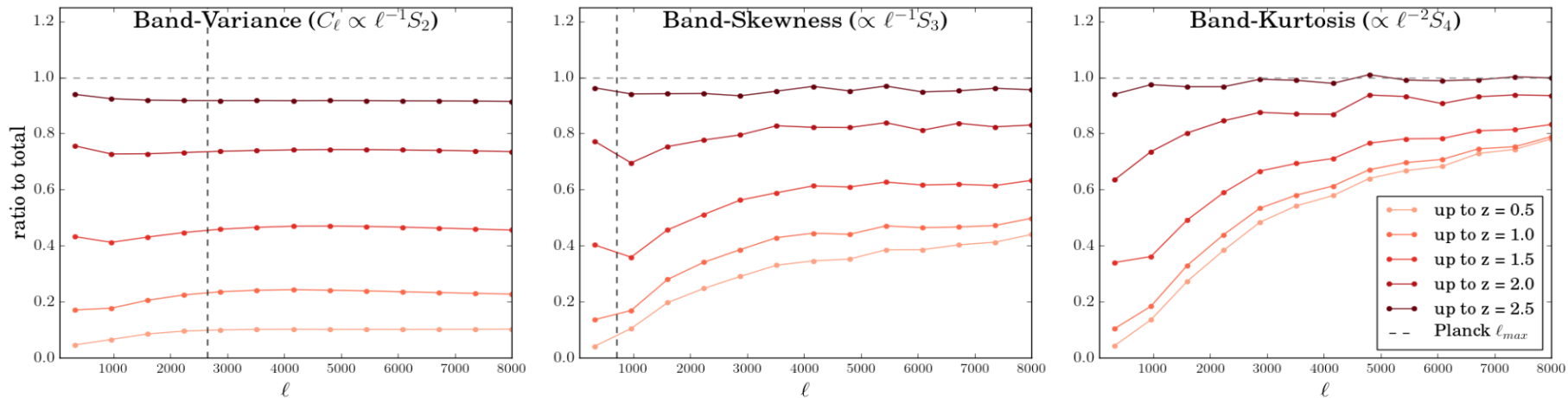


Websky CIB statistics (redshift breakdown)

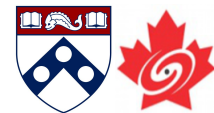




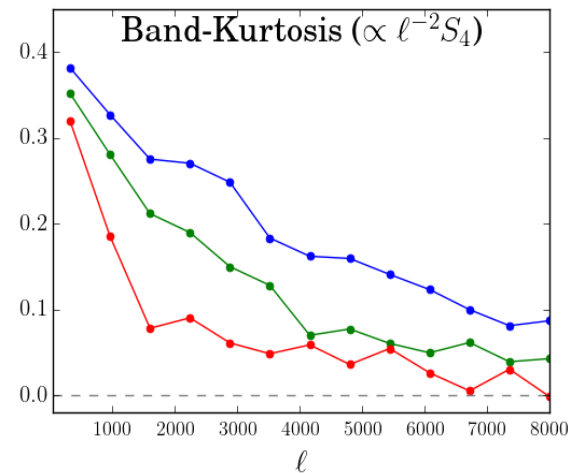
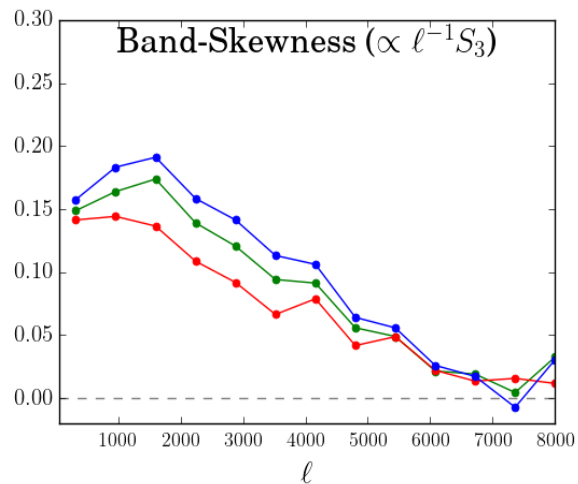
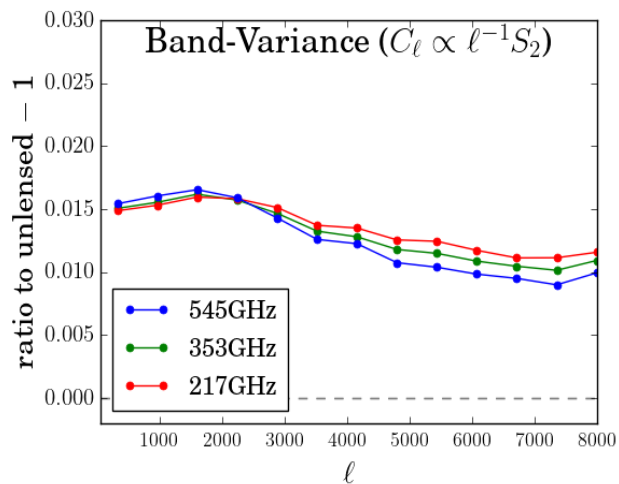
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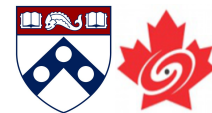


- Most of the CIB statistics come from $z < 2.5$
- For 3-point and 4-point, large contribution from low- z , especially at high- ℓ
- Bright, nearby sources (flux cuts) important for the change in 3-point and 4-point due to lensing

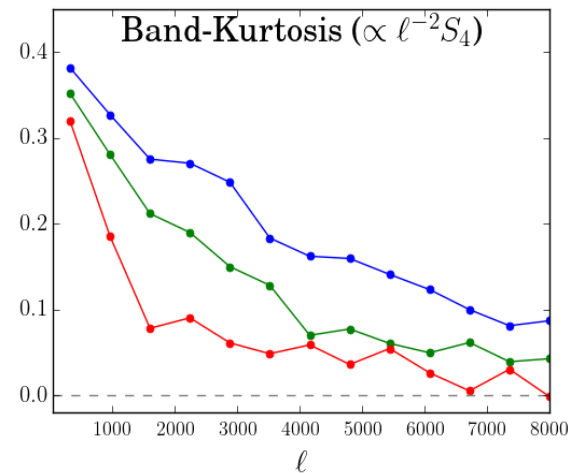
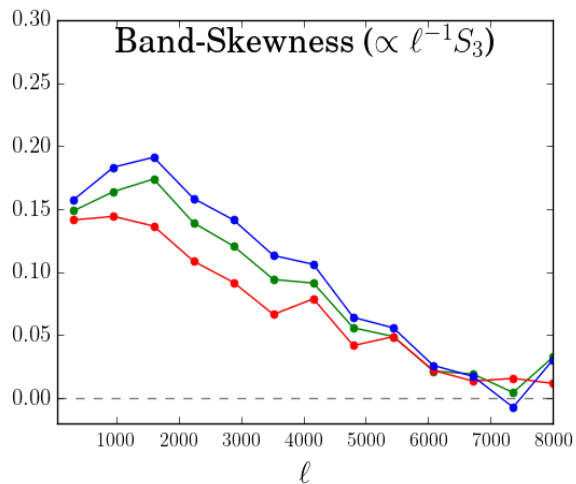
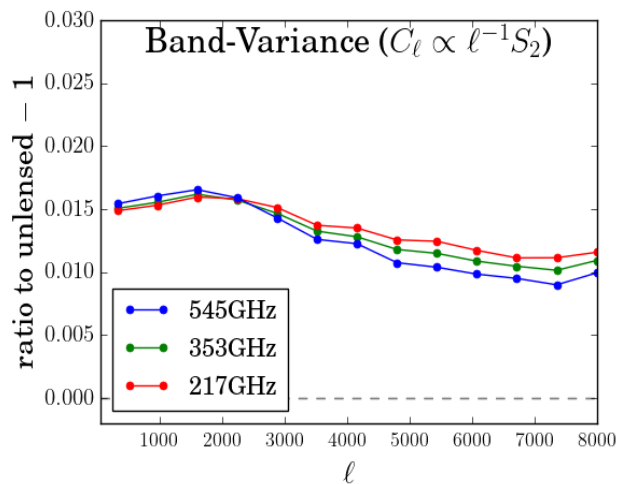


Effect of lensing on CIB statistics

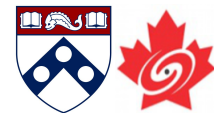




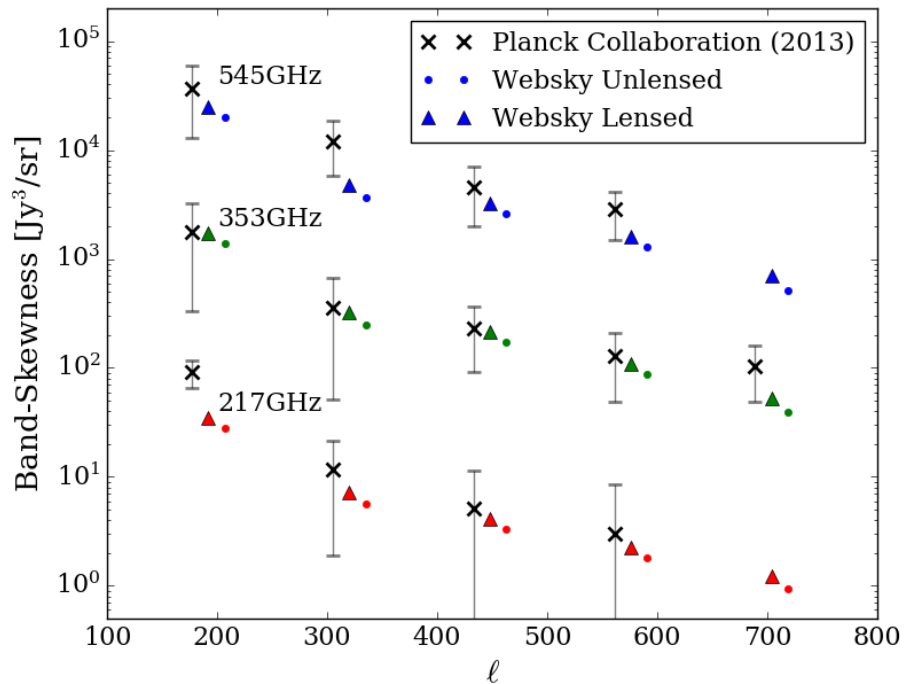
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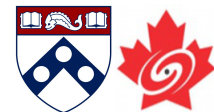


- Small power spectrum increase ($\sim 1.5\%$) as expected by Schaan et al. (2018), while 3-point and 4-point increases substantially at large scales
- More frequency dependence for the 3-point and 4-point (due to flux cut choices)

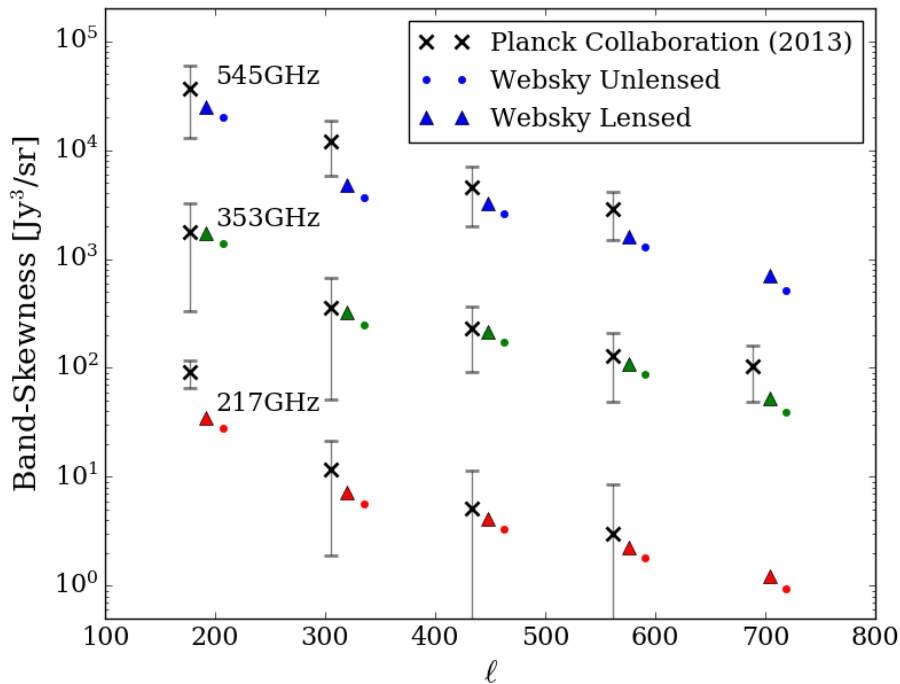


Effect of lensing on CIB statistics (3-point revisited)

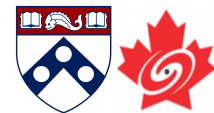




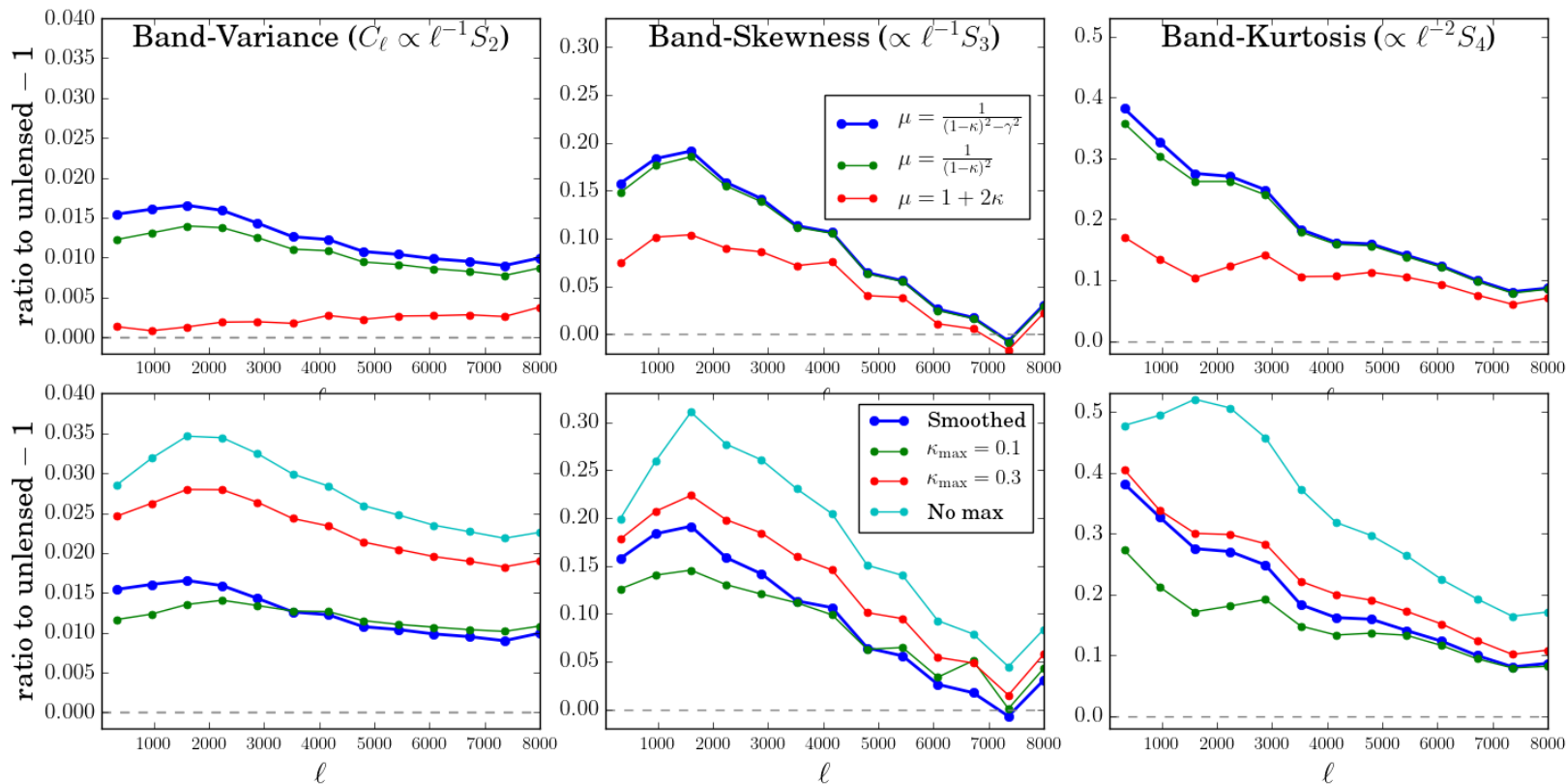
Effect of lensing on CIB statistics (3-point revisited)



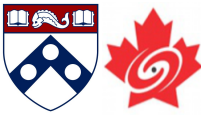
- Websky lensed values closer to *Planck* values
- Lensing could be partially explain why unlensed Websky bispectra values are lower than *Planck's*

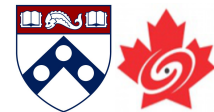


Effect of lensing on CIB statistics (different methods)

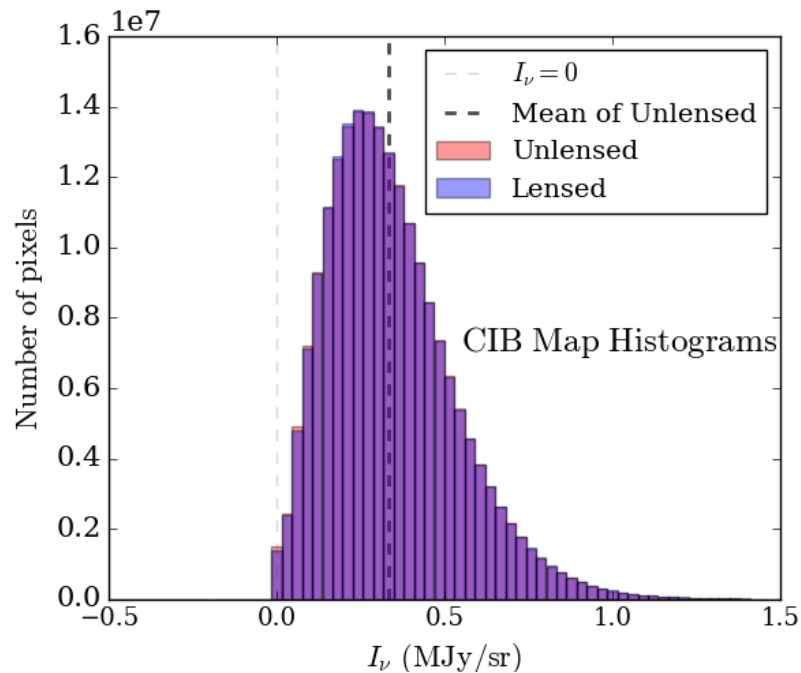


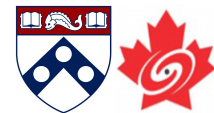
Beyond n-point statistics



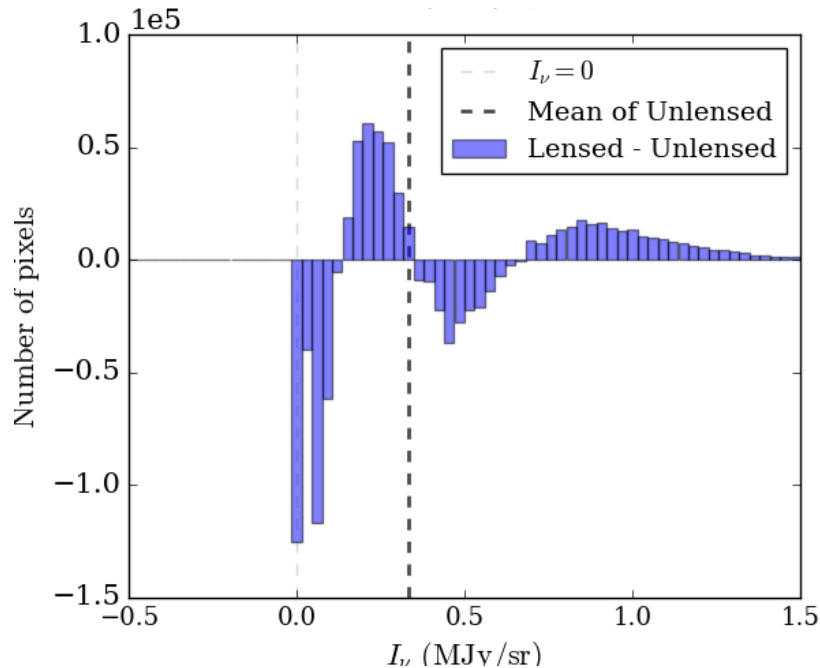
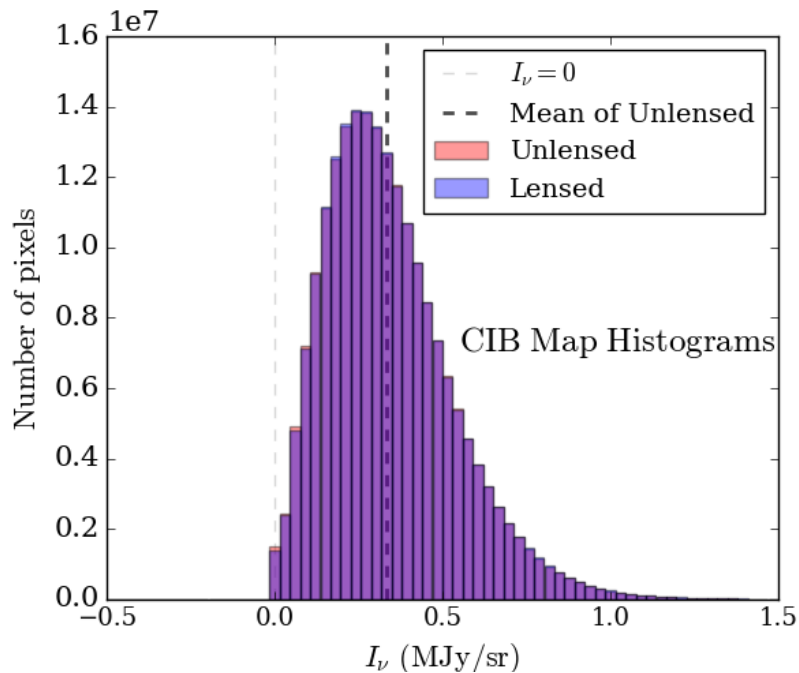


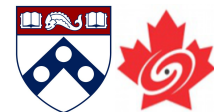
Beyond n-point statistics (Histograms!)





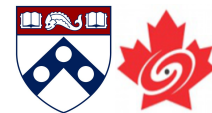
Beyond n-point statistics (Histograms!)



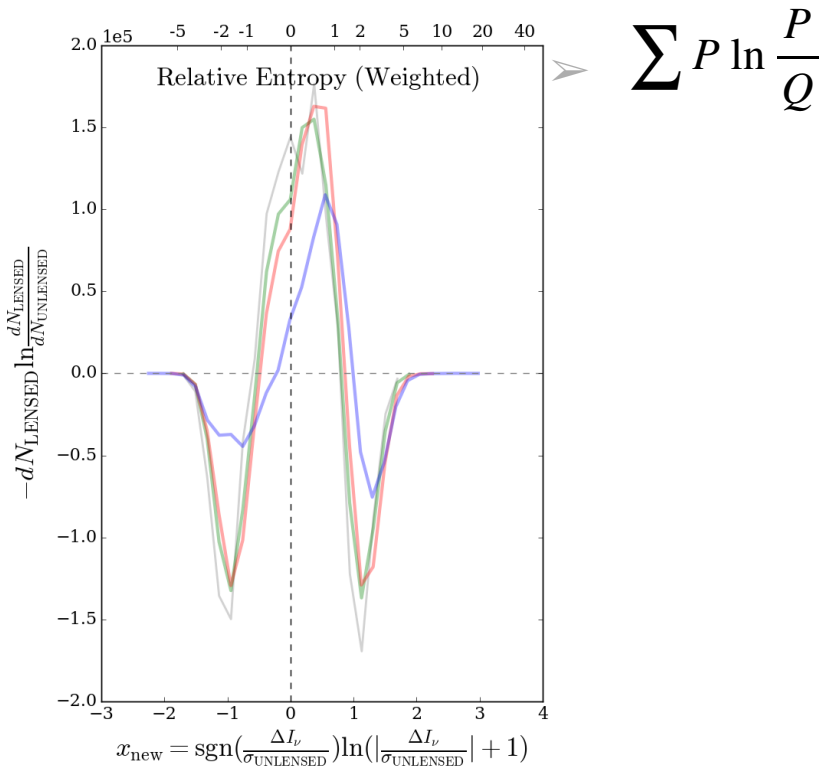
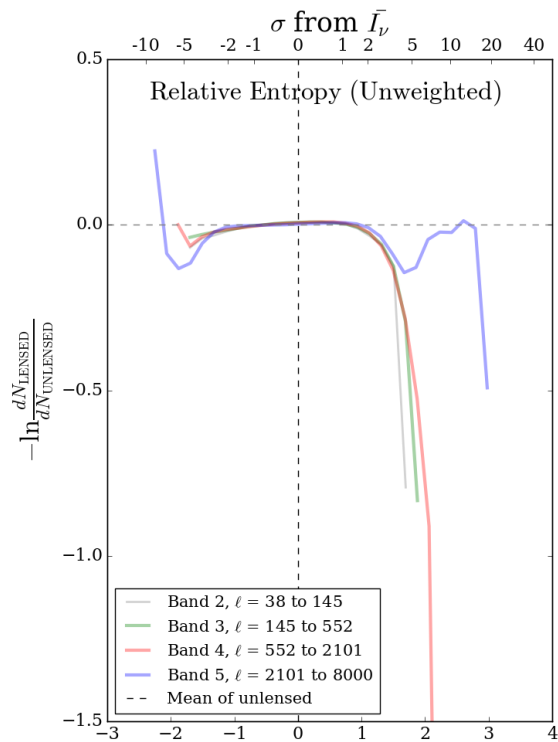


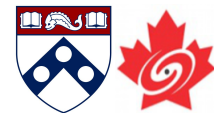
Beyond n-point statistics (Relative Entropy)

➤ Motivated from KL-divergence - $\sum P \ln \frac{P}{Q}$ (P, Q : PDFs)

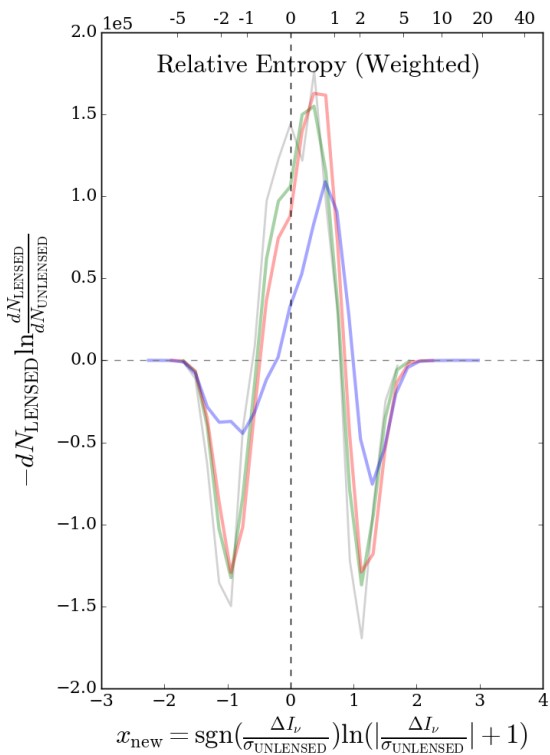
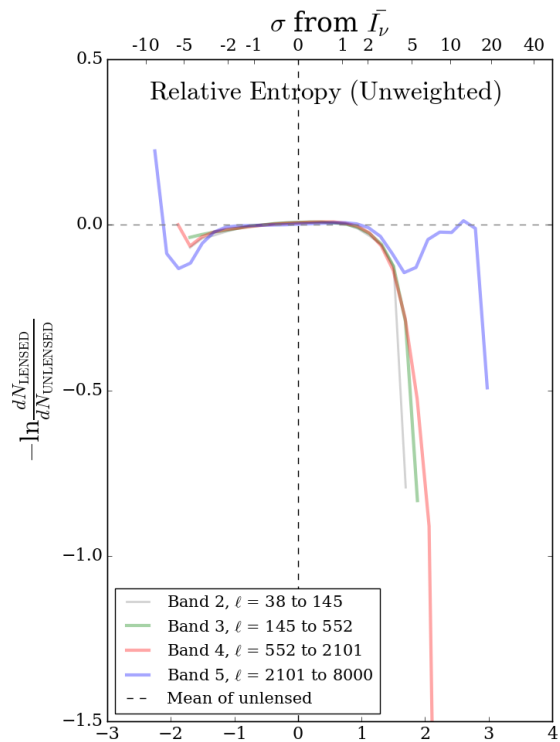


Beyond n-point statistics (Relative Entropy)





Beyond n-point statistics (Relative Entropy)

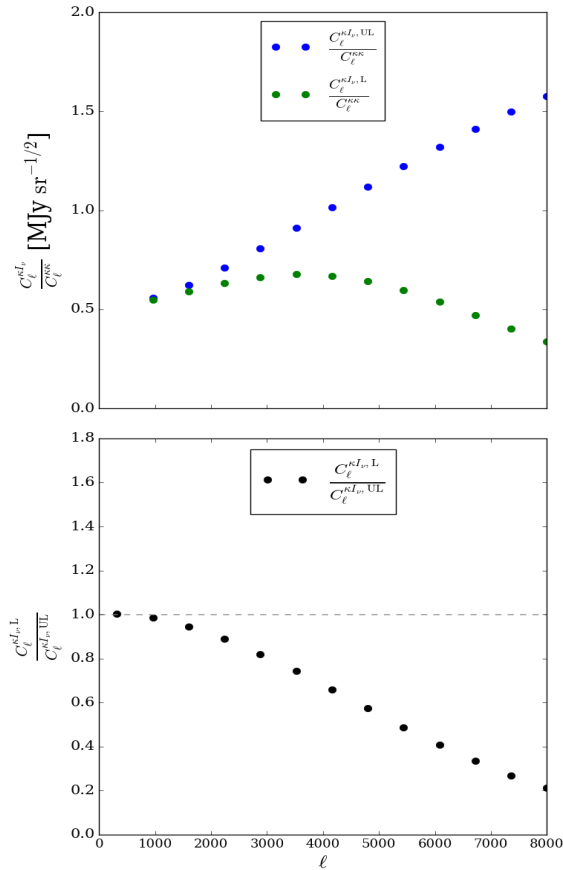
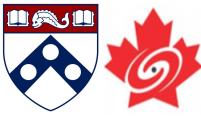


$$\sum P \ln \frac{P}{Q}$$

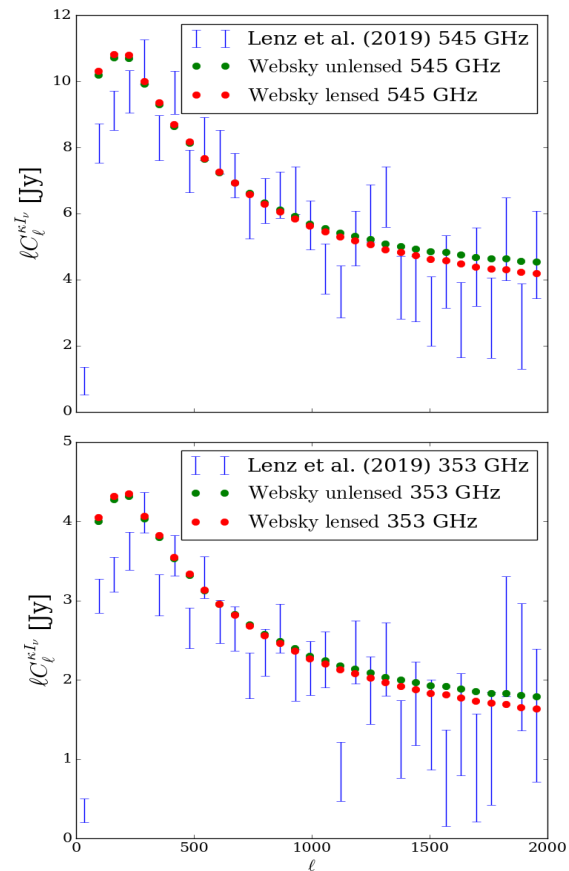
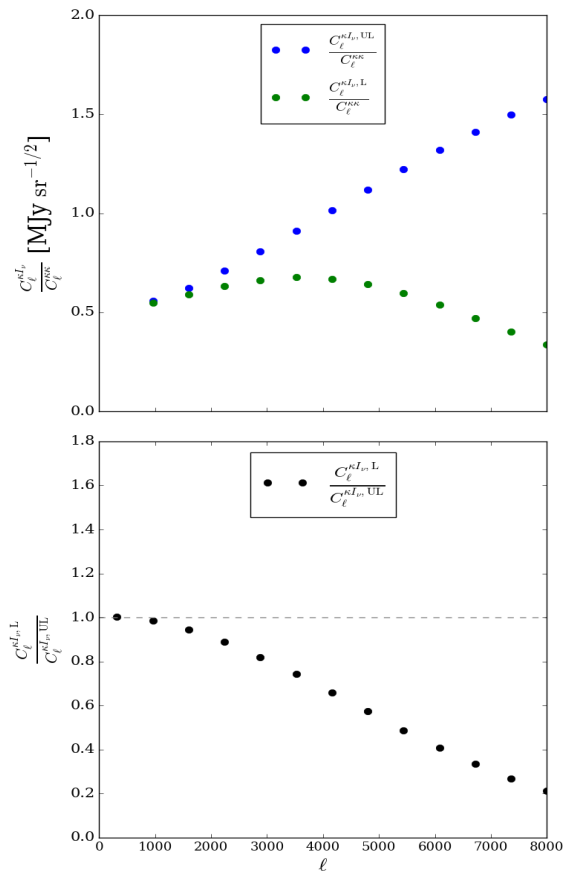
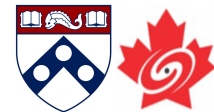
$$[\ln dN_{\text{UNLENSED}} - \ln dN_{\text{LENSED}}]_{\ell\text{-band}} = q_{\text{lens, CIB}} \times [\text{Template}_{\text{UNWEIGHTED}}]_{\ell\text{-band}}$$

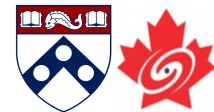
Can plot a *spectra* of $q_{\text{lens, CIB}}$ -
tweak parameters and iterate until
flat to constrain parameters

Correlation between CIB and CMB κ



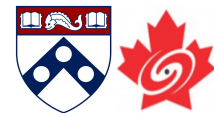
Correlation between CIB and CMB κ





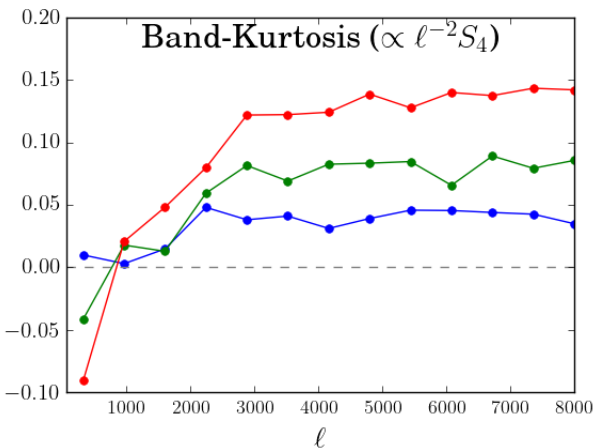
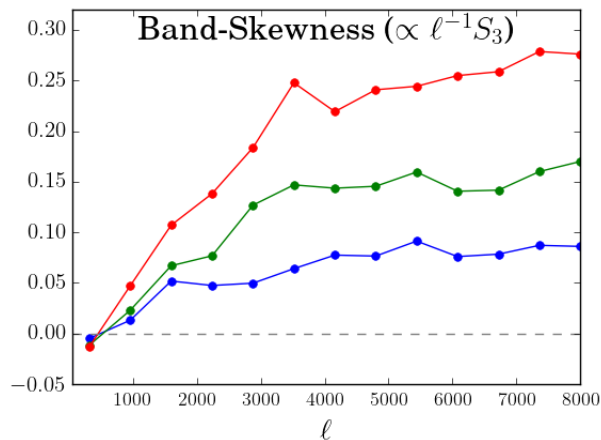
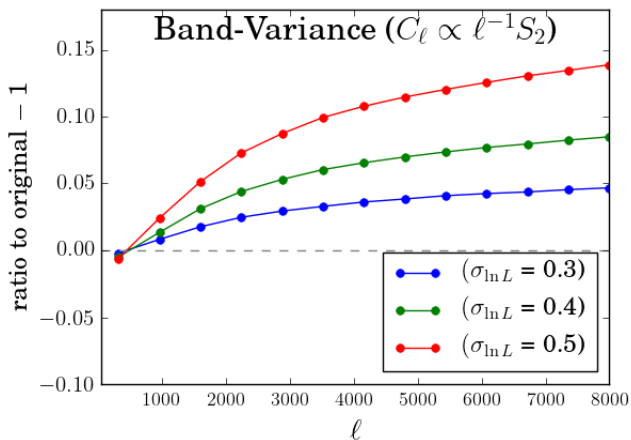
Environmental Effects on CIB statistics

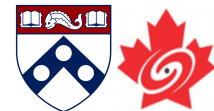
- Galaxy luminosity only depends on mass in the halo model (approximation)
- To model environmental effects, multiplied flux of a galaxy by $\exp[\mathcal{N}(0, \sigma_{\ln L})]$
- Normalized map so that the power spectrum matches Websky at $\ell = 500$



Environmental Effects on CIB statistics

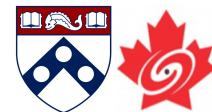
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Conclusion & Why we care

- Websky CIB maps capture equilateral bispectra reasonably well
- CIB lensing increases power spectrum by $\sim 1.5\%$ and the 3-point and 4-point by 10~20% or more
- Relative entropy can be used to probe both intrinsic CIB parameters and lensing
- CIB lensing could potentially be detected through cross-correlation with CMB lensing
- Induced stochasticity can change CIB statistics



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-
- CIB non-Gaussianity provides extra information on top of power spectrum
 - Lensing pipeline can be used for any 3-D intensity fields (21cm, Lyman-alpha, mm-wave intensity fields)
 - CIB non-Gaussianity affects detection of primordial non-Gaussianity
 - Change in CIB-non-Gaussianity due to lensing could be important for next-generation surveys

Thank you very much!
Questions/Comments?